

Structural aspects of B *K* edge XANES of minerals

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Outline

- Introducing XANES technique

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- Spectra of minerals with pure BO_3 or BO_4 coordinations

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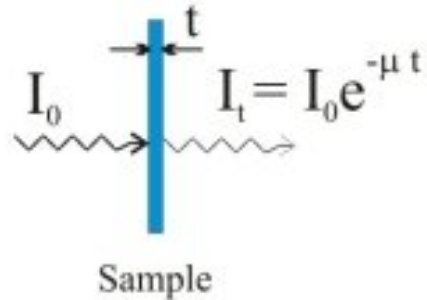
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- Minerals with boron in both BO_3 and BO_4 units
- Search for markers of BO_3 and BO_4 coordinations in XANES spectra
- Explore influence of technical parameters (scattering potential, core hole, size of cluster)
- Inspect prospective use of B K edge XANES in quantitative studies of structure of glasses

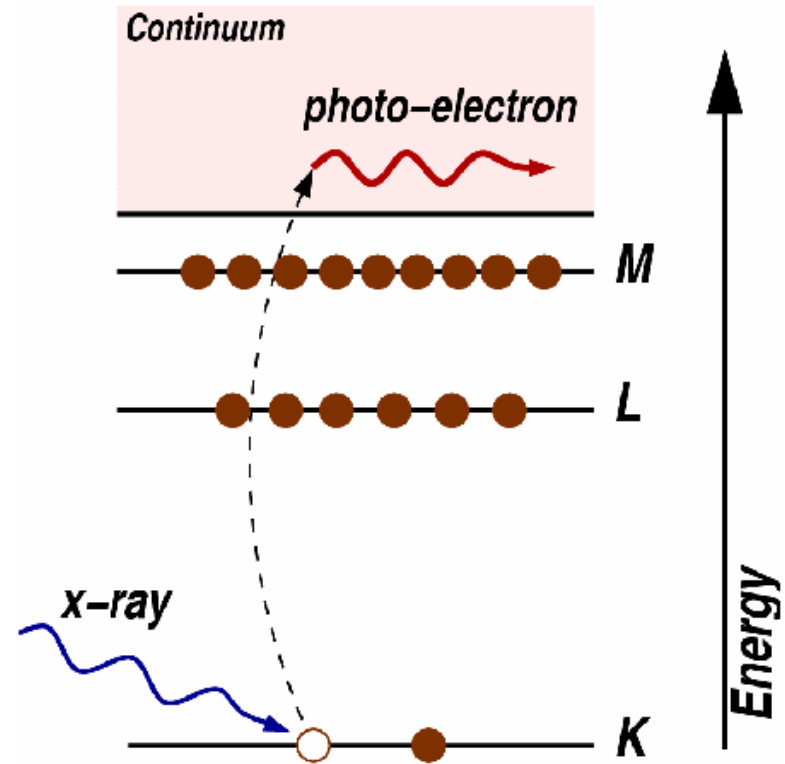
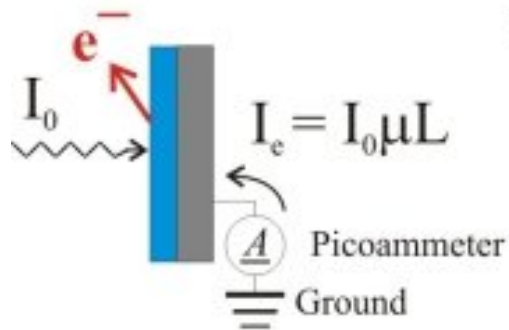
X-ray absorption spectroscopy in a nutshell

X-ray absorption spectroscopy

Transmission

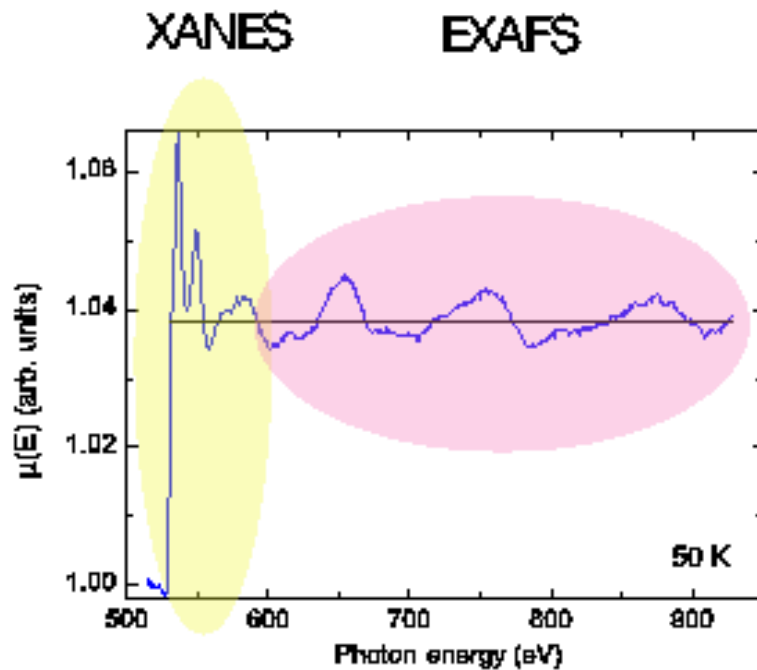


Electron Yield



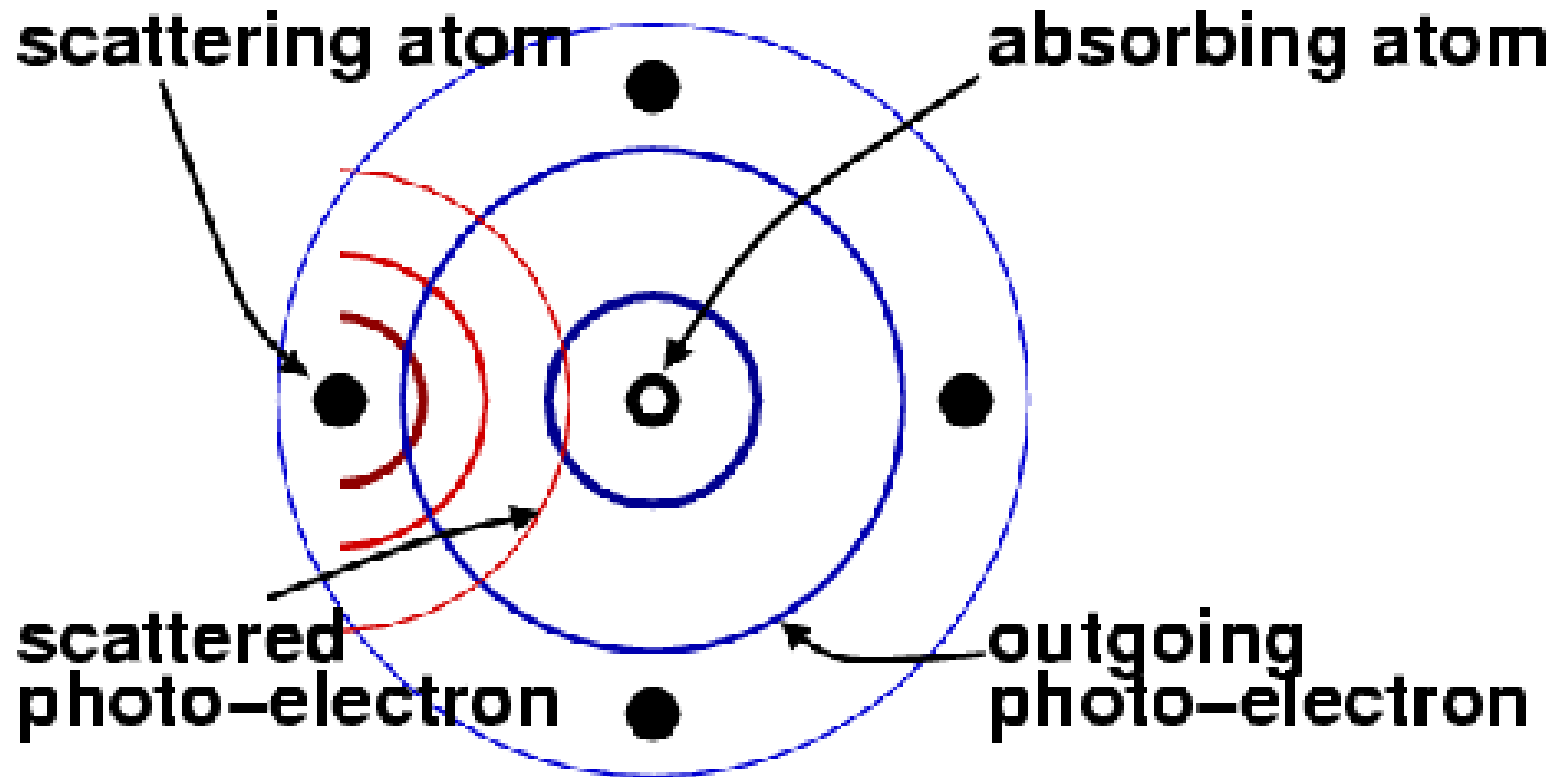
- x-rays are absorbed in the sample via a photoelectron effect
- more detection techniques are possible

Taxonomy



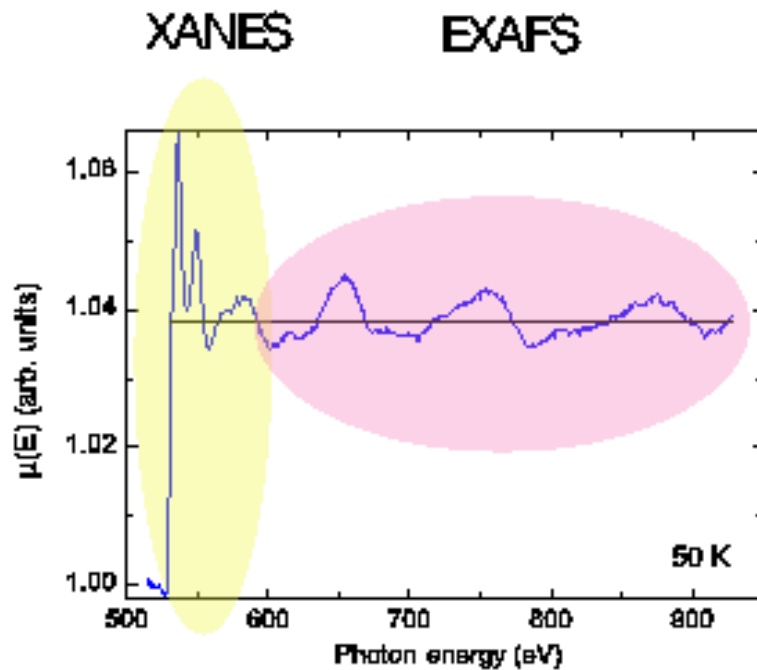
- Low photoelectron energies (≤ 50 eV) \rightarrow XANES
(X-ray Absorption Near Edge Structure)
- High photoelectron energies (100–1000 eV) \rightarrow EXAFS
(Extended X-ray Absorption Fine Structure)

Local probe



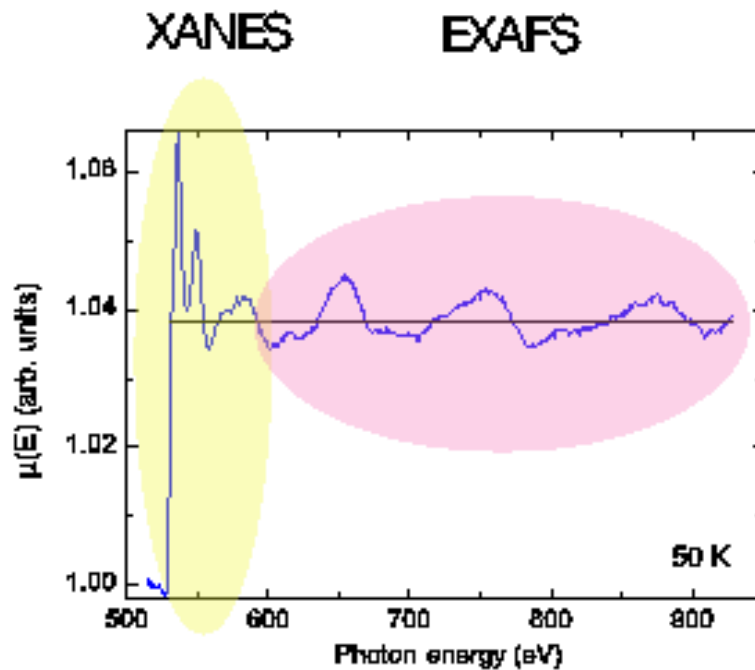
- Offers a view from one particular site (chemically selective)
- Outgoing photoelectron is scattered by the neighbors
- Constructive/destructive interference depending on interatomic distance

EXAFS



- Several approximations possible in the EXAFS region
- Structural information can be “straightforwardly” extracted
- EXAFS oscillations are sometimes too faint to measure

XANES



- Physics more complicated
- Some structural information is there but **difficult to extract**
- “Fingerprinting” may be dangerous (no unique correspondence between structural elements and spectral features)

Theoretical framework

- Spectra calculated in a real space (finite clusters of 100-250 atoms)

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Theoretical framework

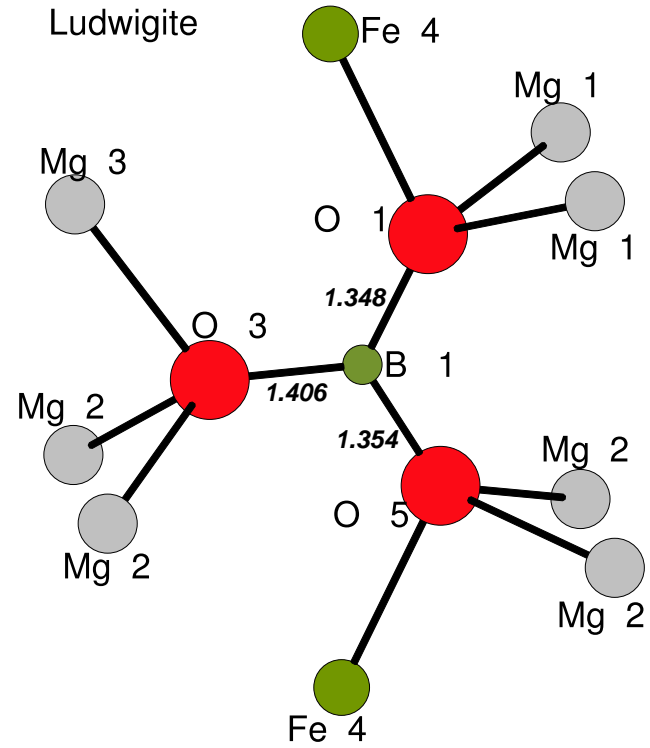
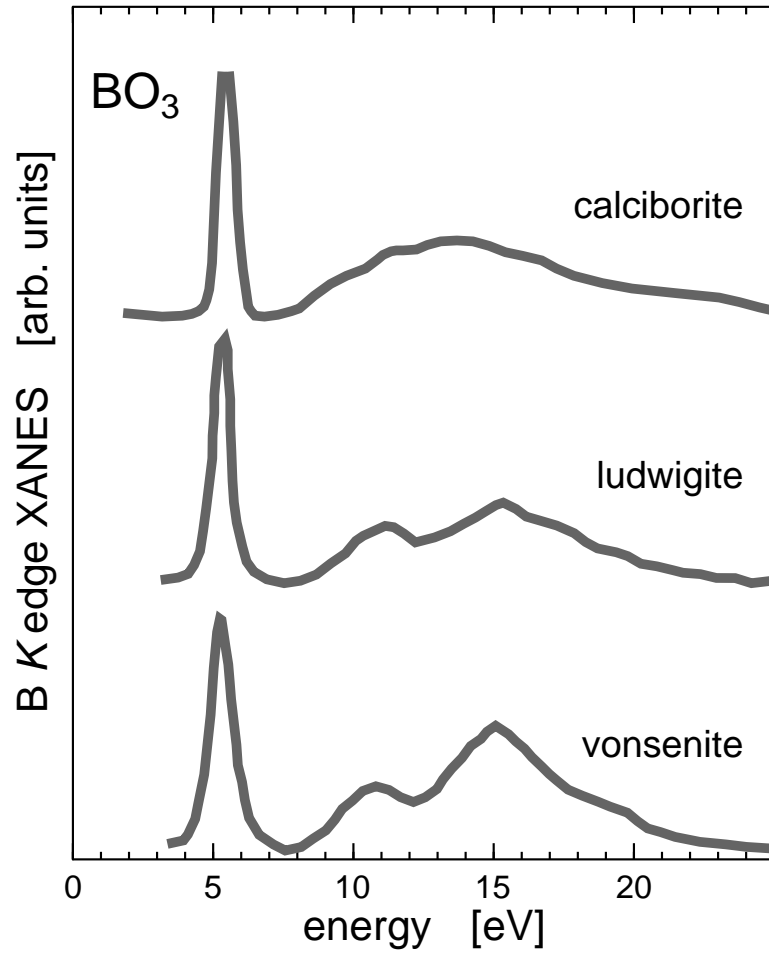
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- Scattering potentials mostly non-self-consistent (Mattheiss prescription) [checked that self-consistent potentials yield similar results]

Theoretical framework

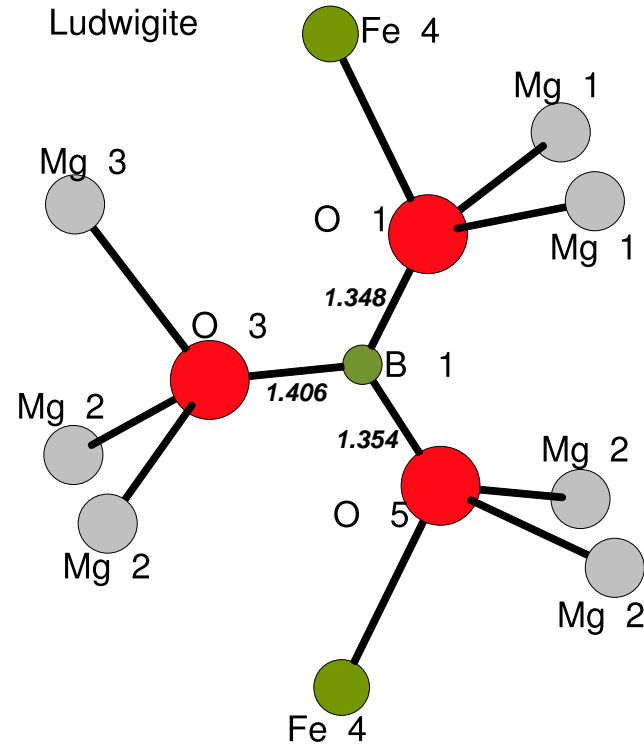
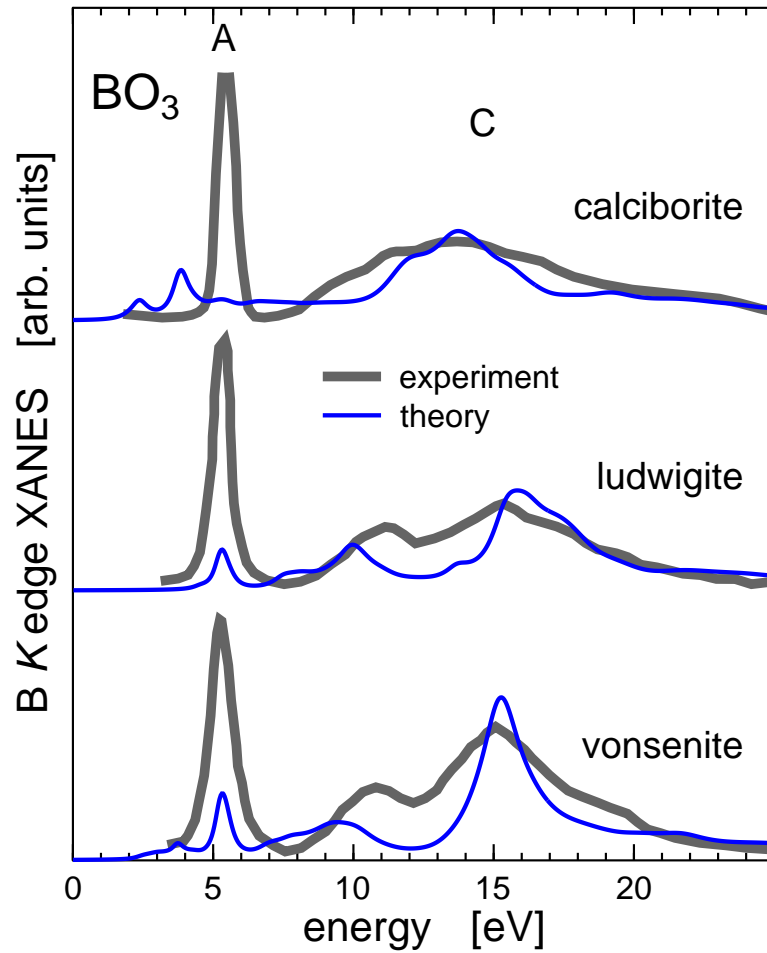
- Spectra calculated in a real space (finite clusters of 100-250 atoms)
- Full multiple scattering included
- True crystal geometry taken from literature, all atoms at correct positions (no simplification of the structure)
- Scattering potentials mostly non-self-consistent (Mattheiss prescription) [checked that self-consistent potentials yield similar results]
- Core hole treated statically (final state rule, “relaxed and screened” model)

Minerals with only one boron site

Minerals with only BO_3 units

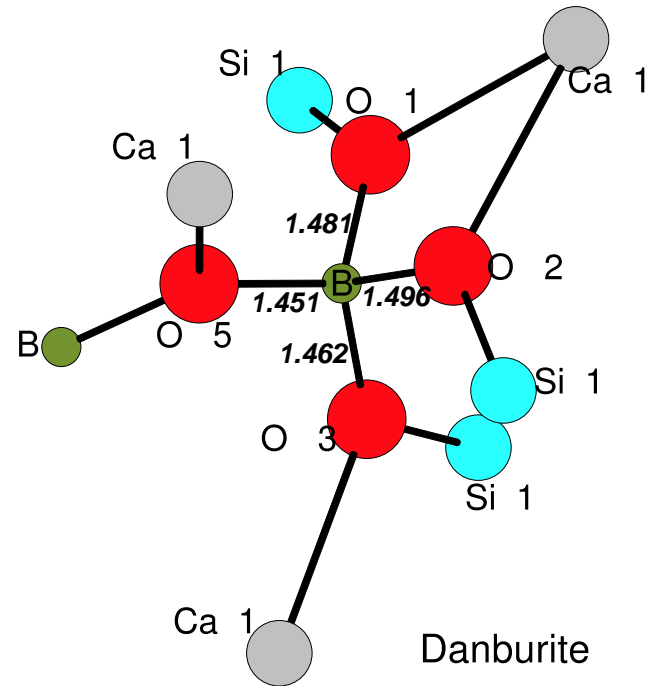
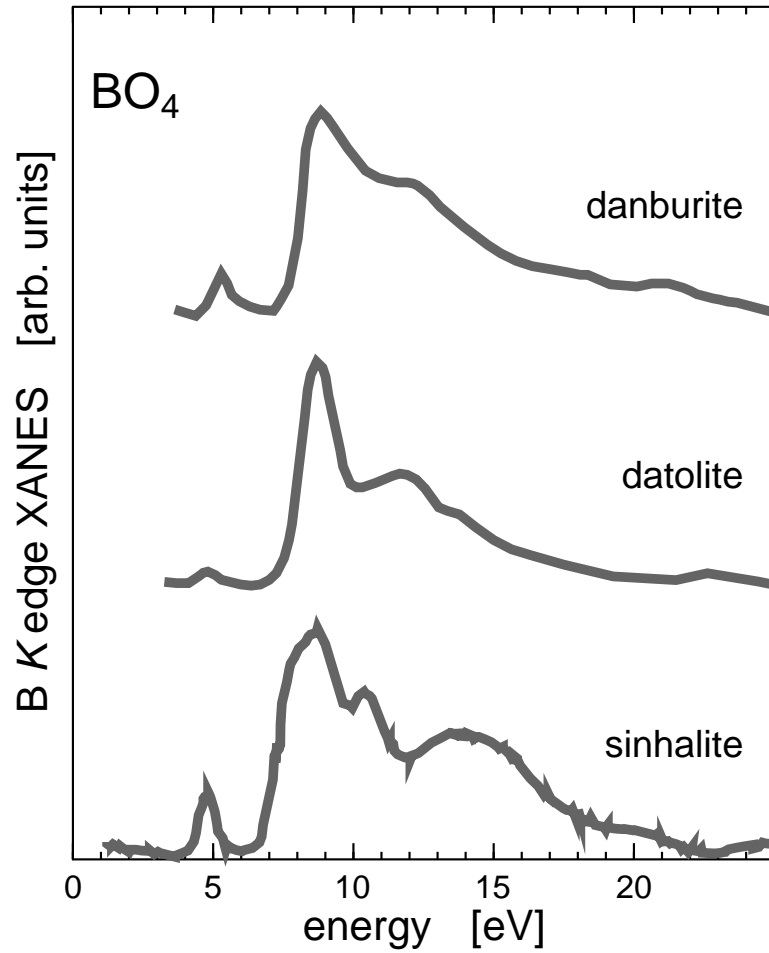


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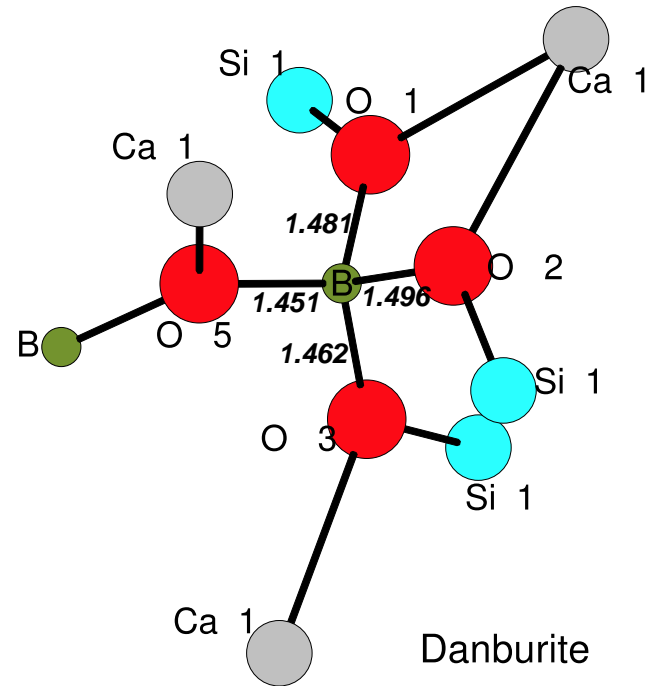
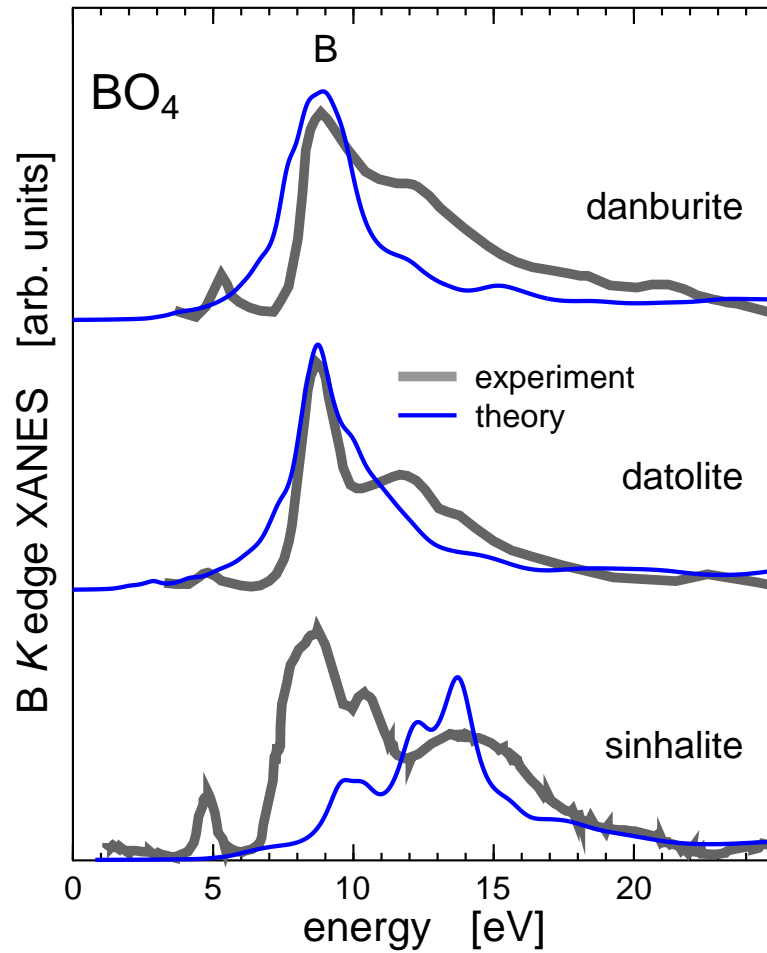


- Pre-peak followed by a main peak, about 10 eV apart

Minerals with only BO_4 units

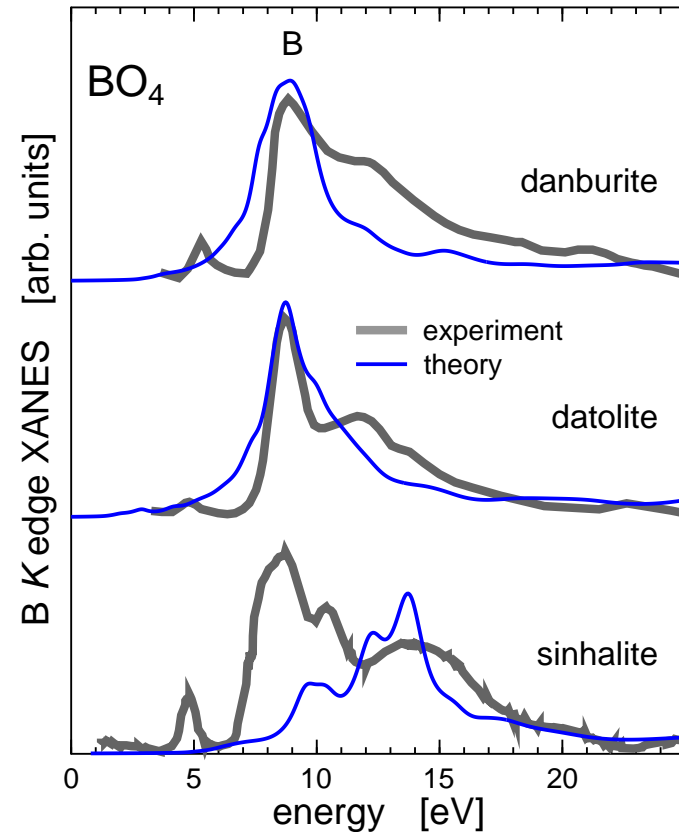
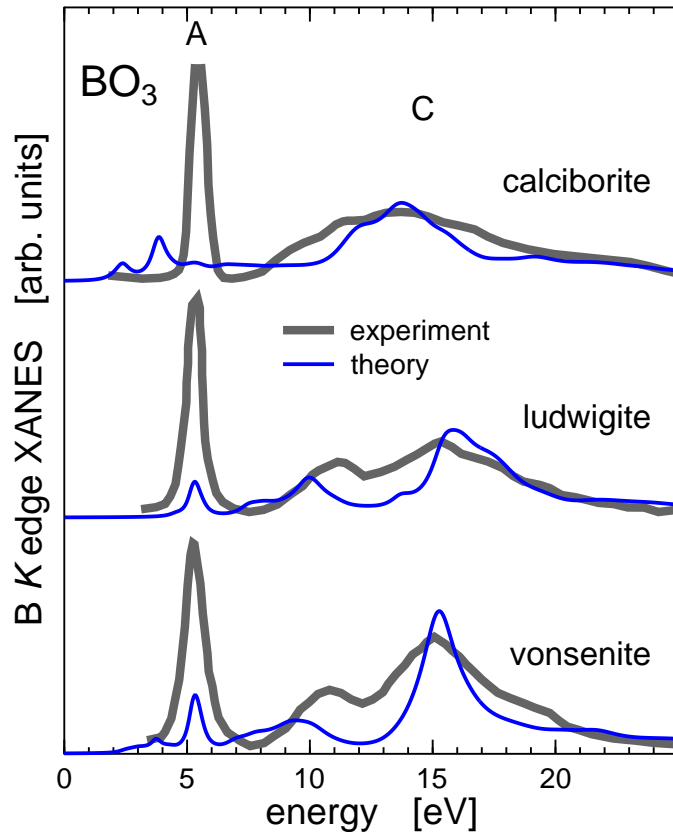


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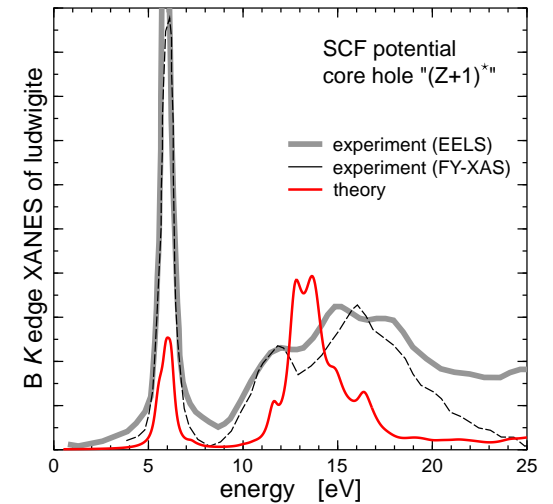
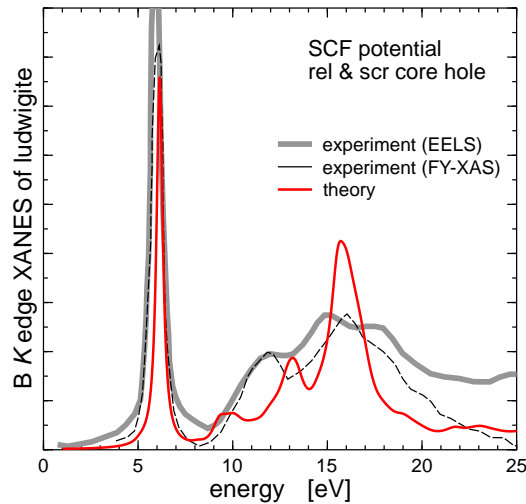
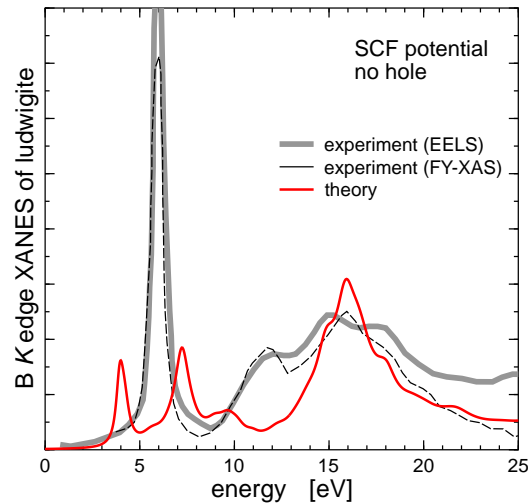
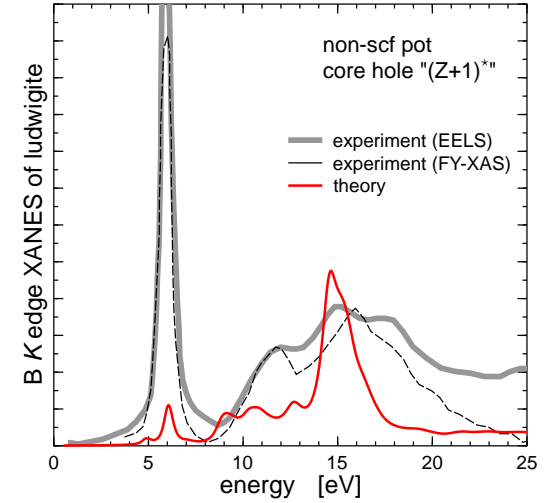
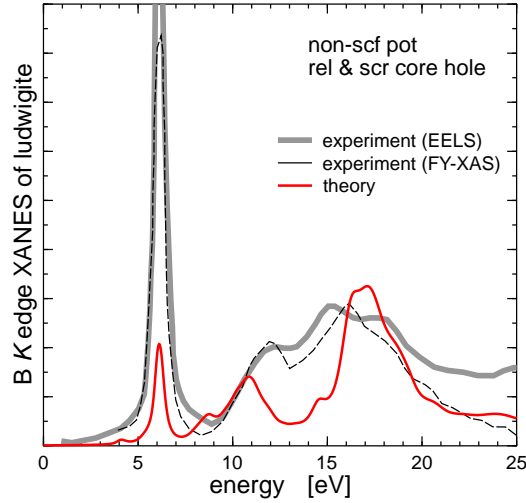
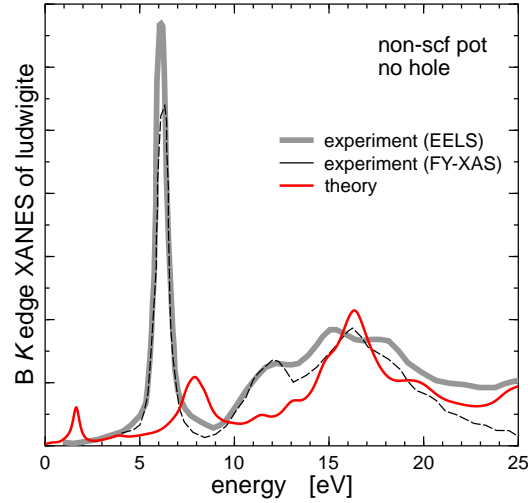
- Experiment: Main peak with a shoulder
- Theory: Single peak

Basic typology

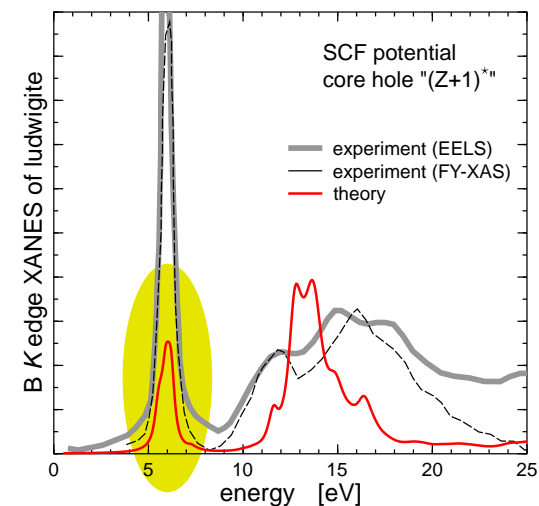
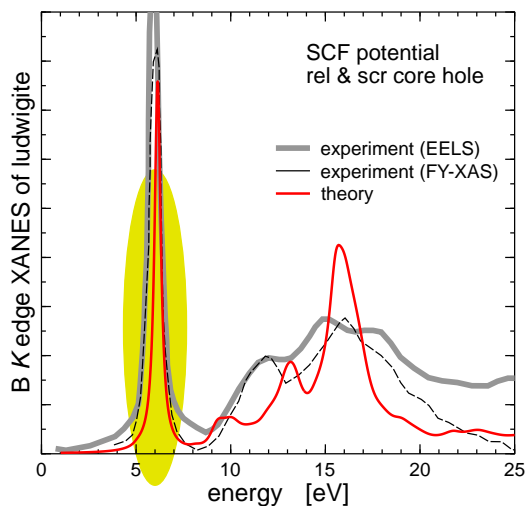
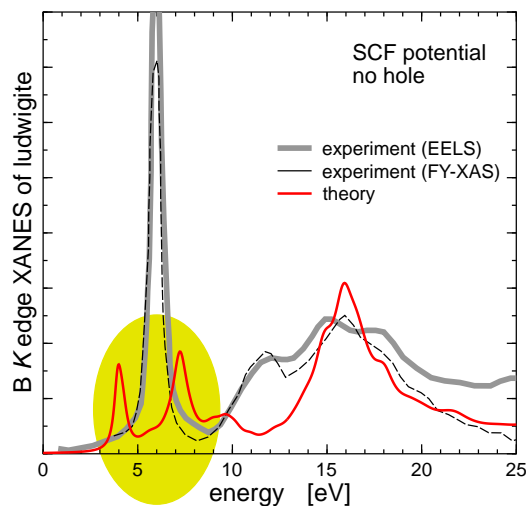
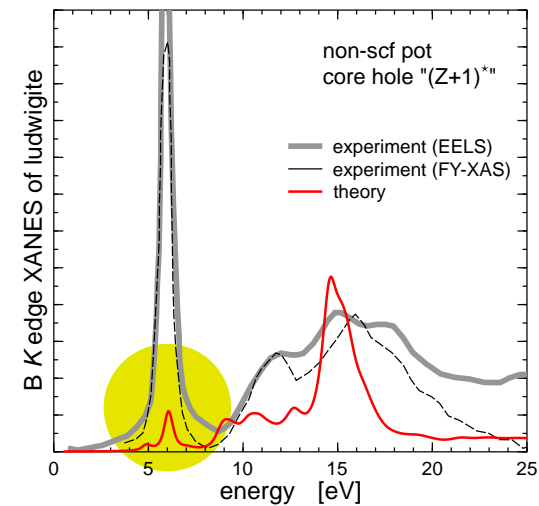
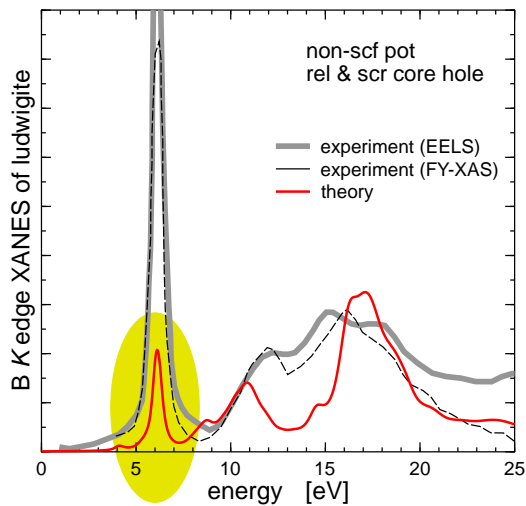
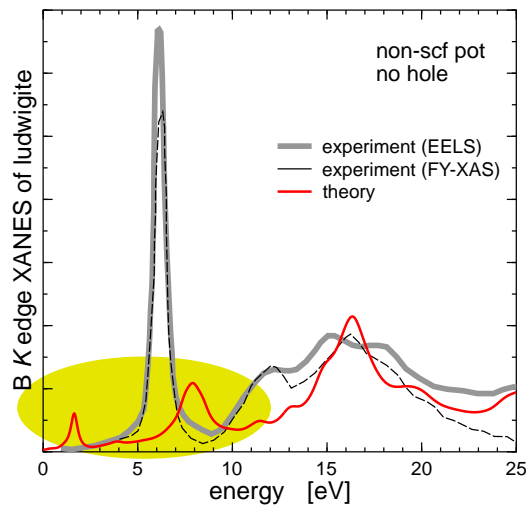


- Characteristic shapes of XANES spectra depend on the presence of either BO₃ or BO₄ unit

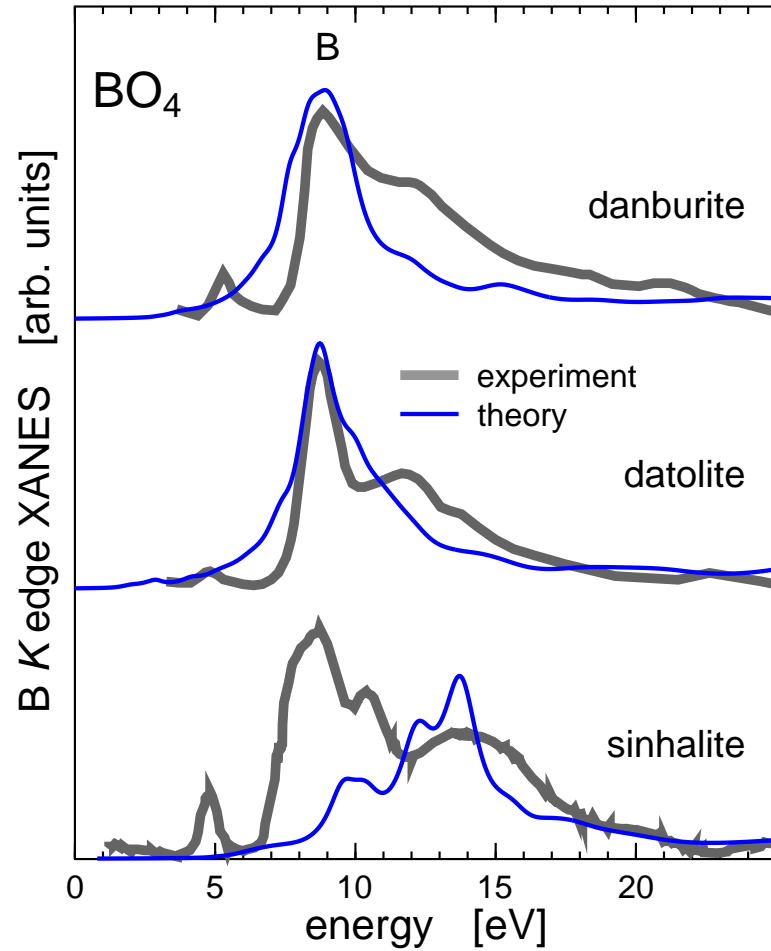
Using various scattering potentials



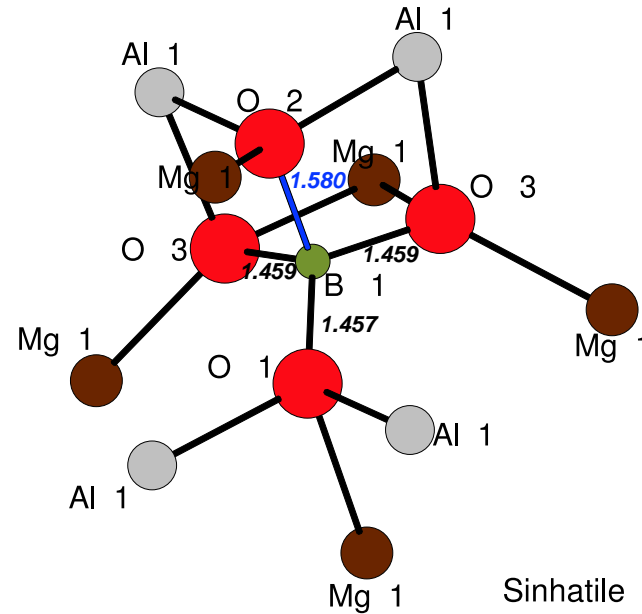
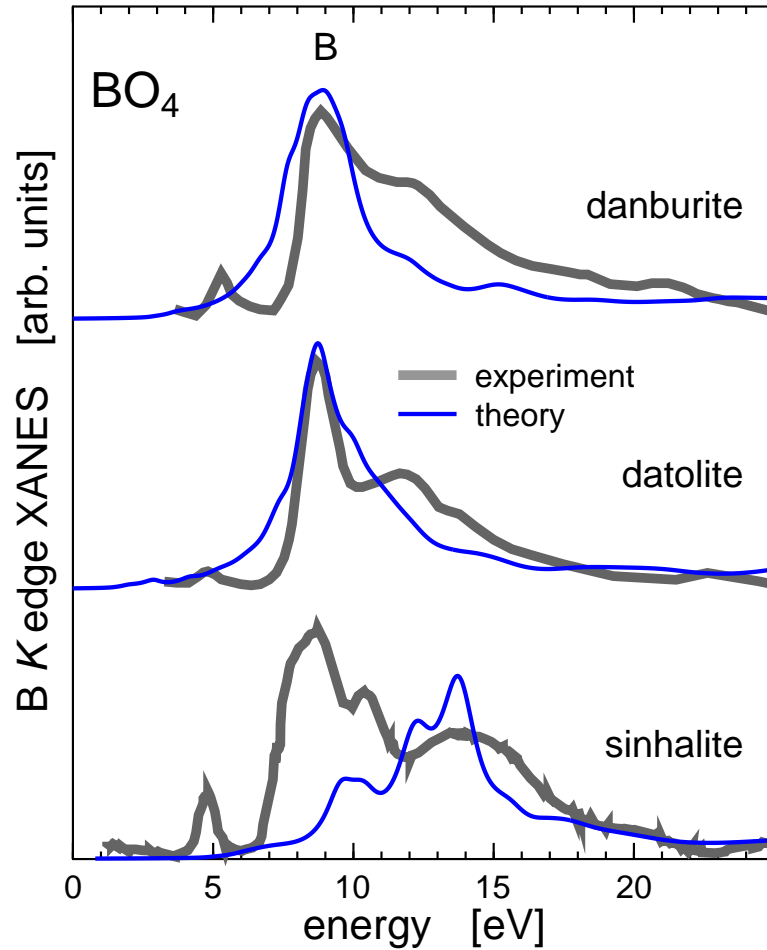
Core hole effect at the pre-edge



Sinhalite does not quite follow the herd

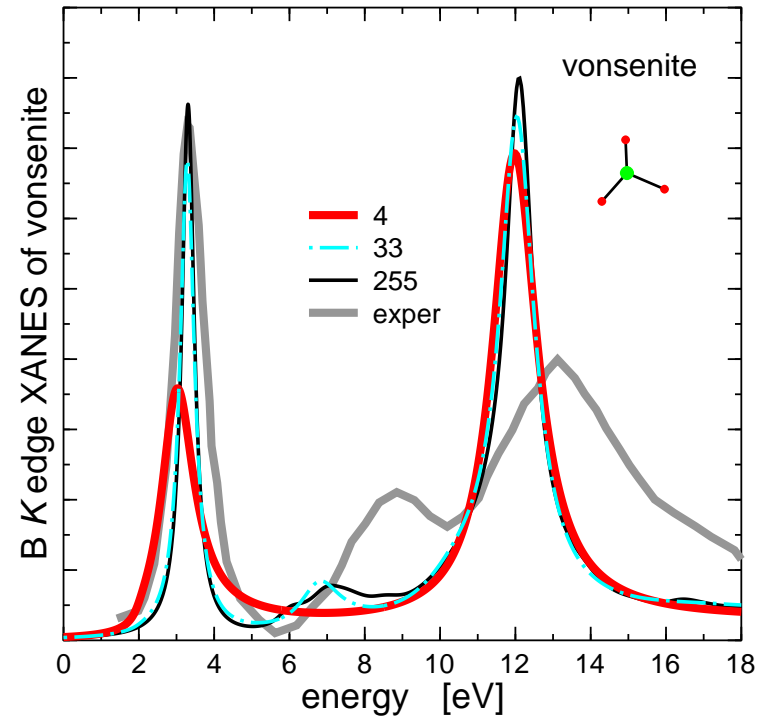
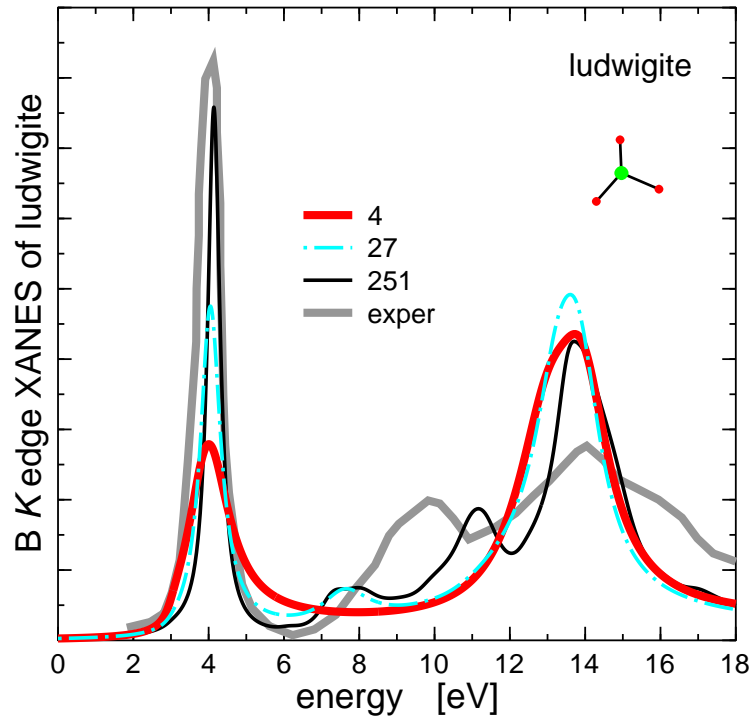


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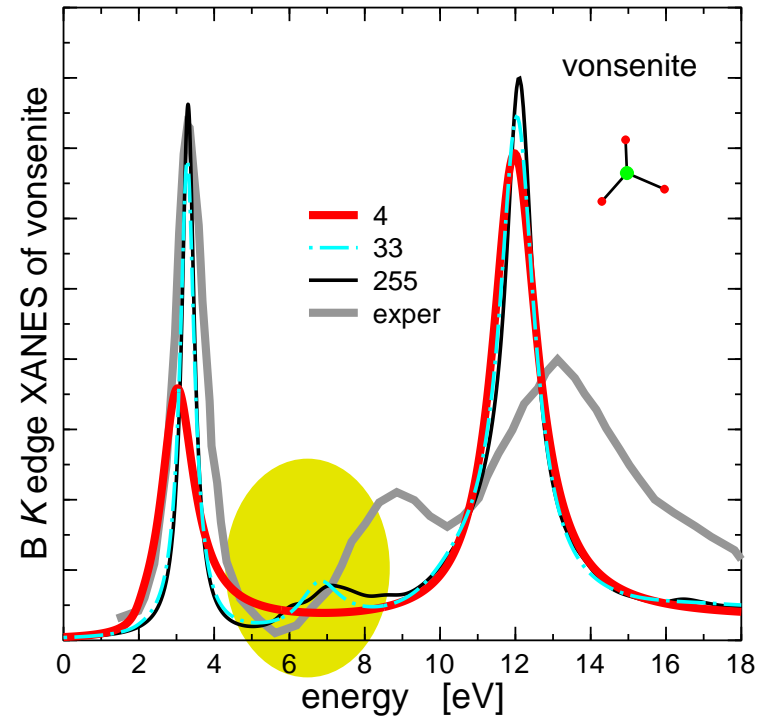
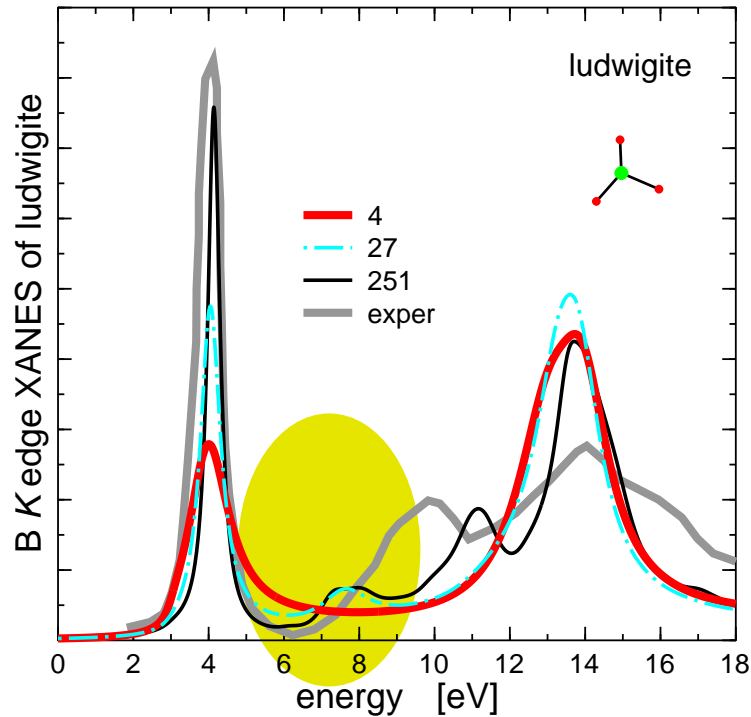
- Three B-O bonds of 1.46 Å, one bond of 1.58 Å
⇒ it is rather a **3+1** coordination

Cluster size effect — BO_3 units



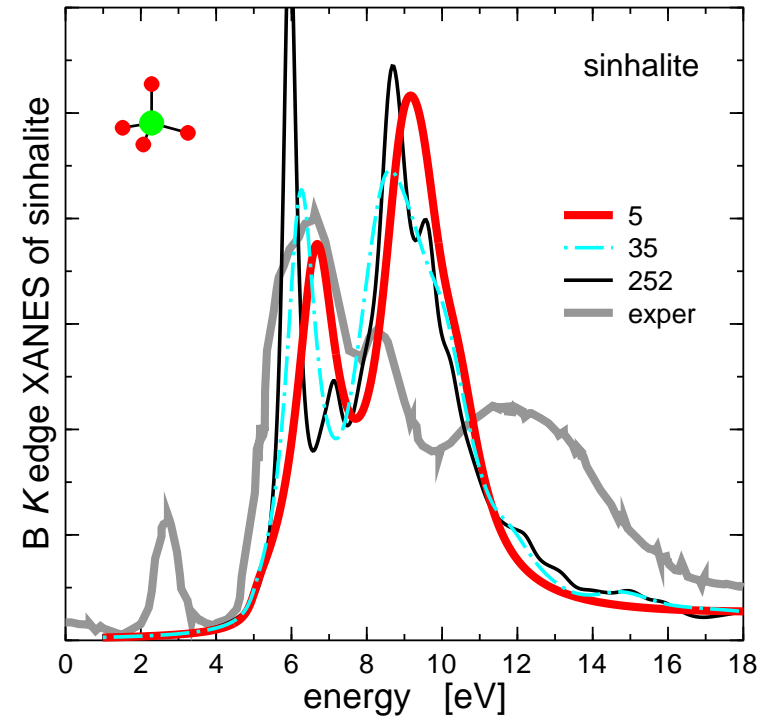
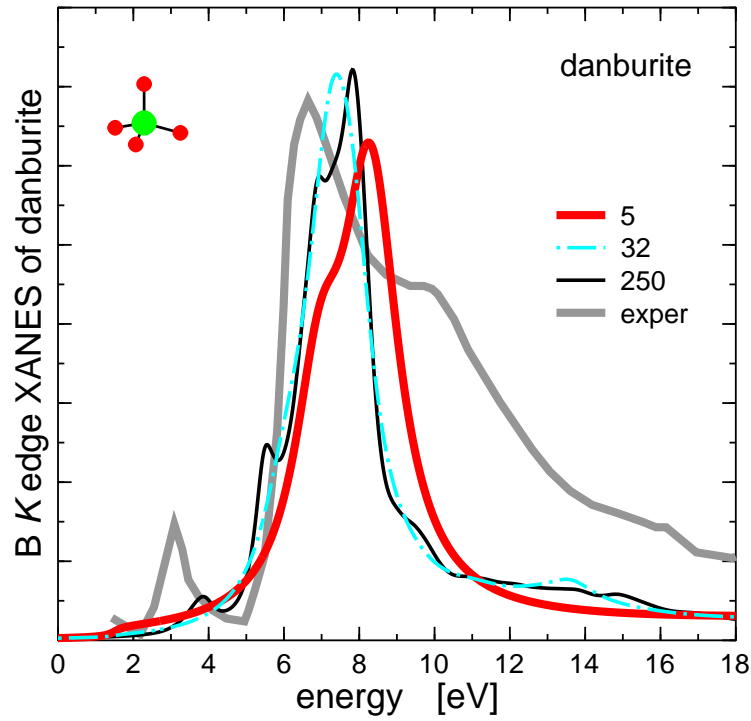
- Spectra for clusters of 4 atoms and of 250 atoms are very similar

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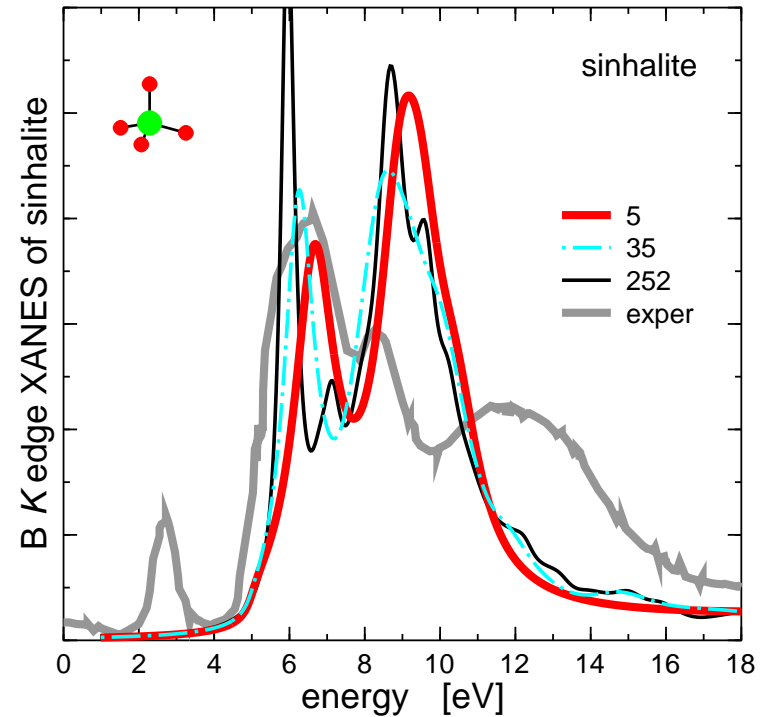
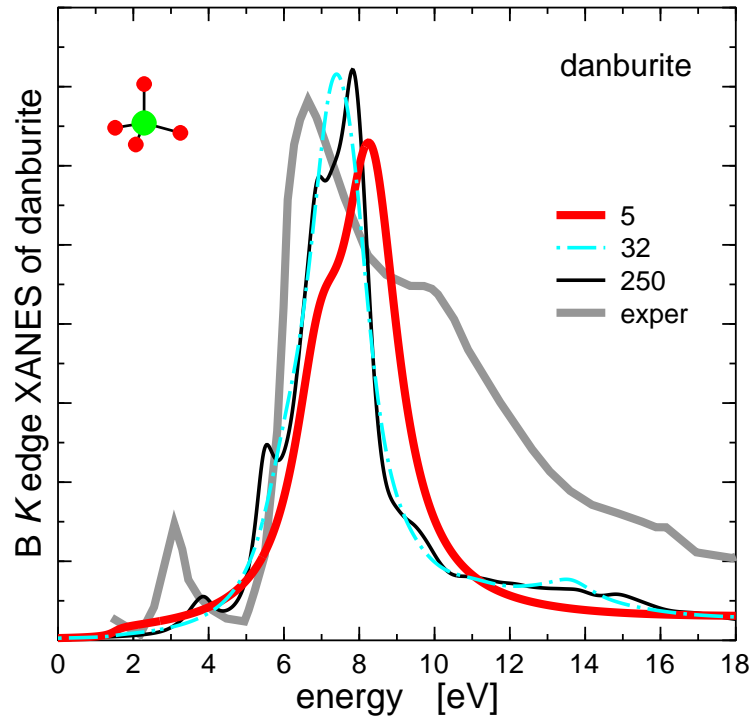
- Spectra for clusters of 4 atoms and of 250 atoms are very similar
- Fine structure between the pre-peak and the main peak is due to medium- and long-range order

Cluster size effect — BO_4 units



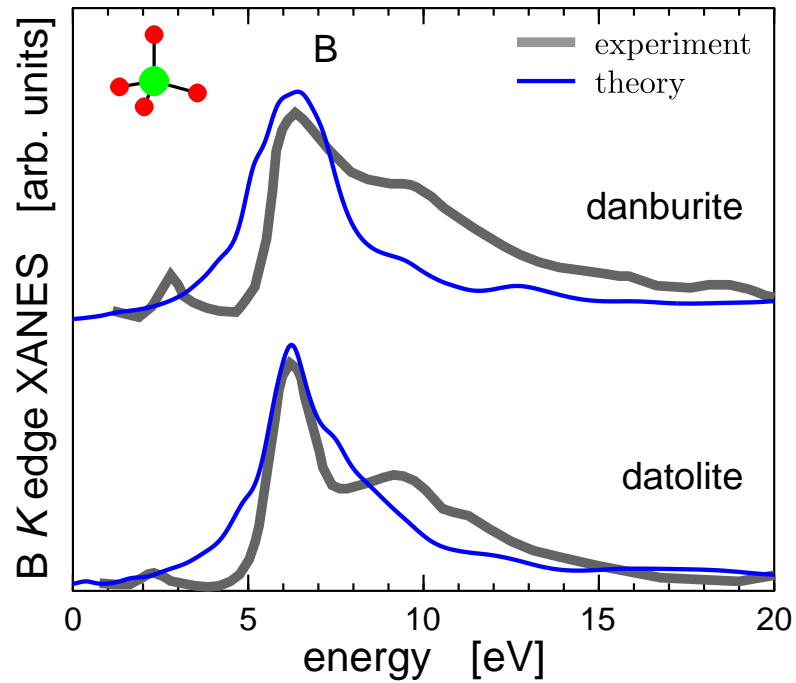
- Spectra for clusters of 5 atoms and of 250 atoms again very similar

Cluster size effect — BO_4 units



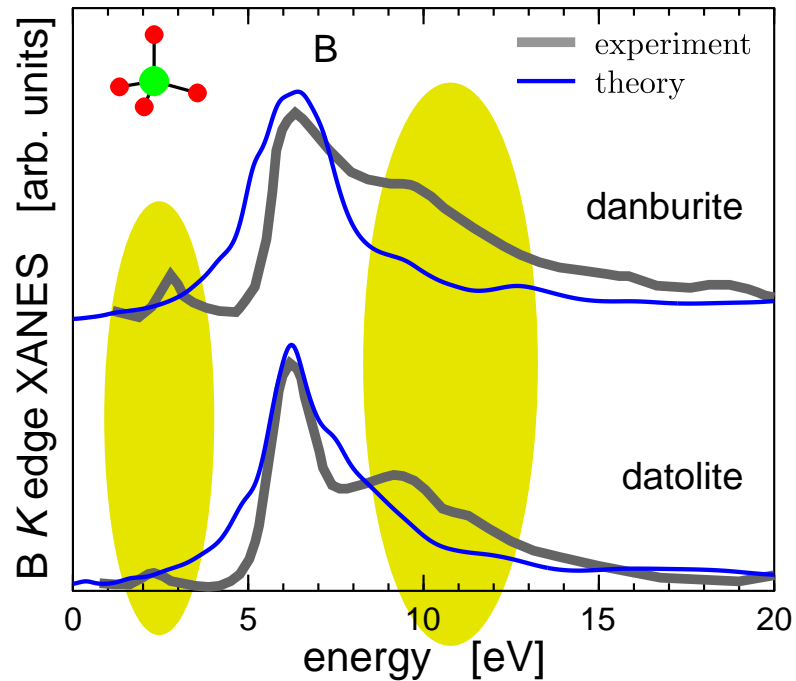
- Spectra for clusters of 5 atoms and of 250 atoms again very similar
- Pre-peak and shoulder do not appear for any size of cluster

Pre-peak and shoulder for BO_4 units



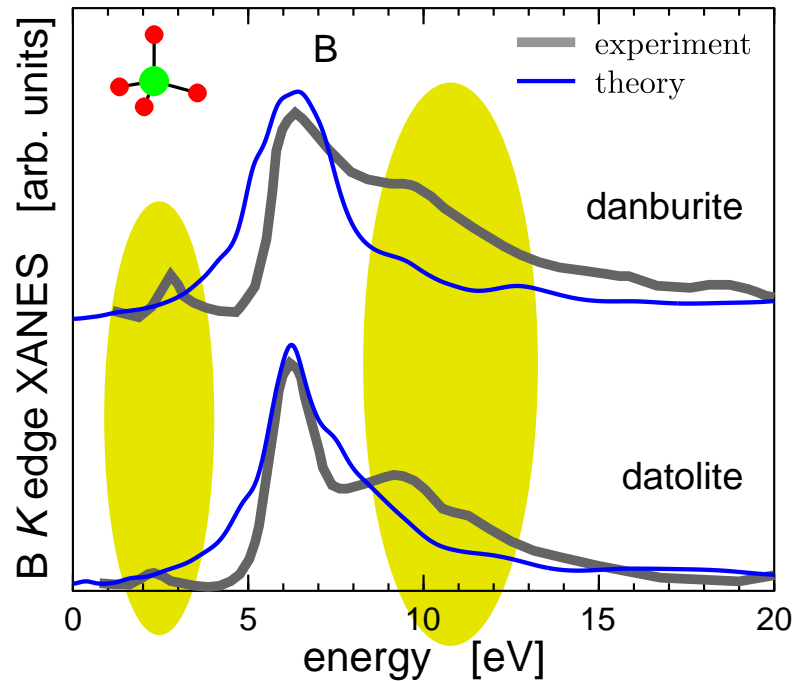
● “Systematic” deviations between theory and experiment

Pre-peak and shoulder for BO_4 units



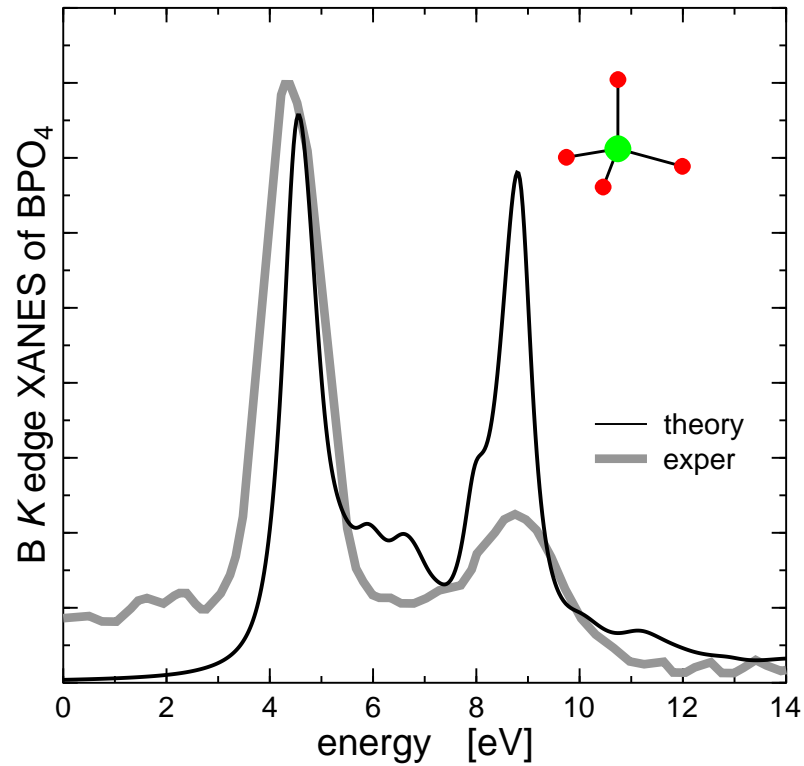
- “Systematic” deviations between theory and experiment
- Pre-edge region XANES is prone to radiation damage — just consequence of BO_3 defects?

Pre-peak and shoulder for BO_4 units



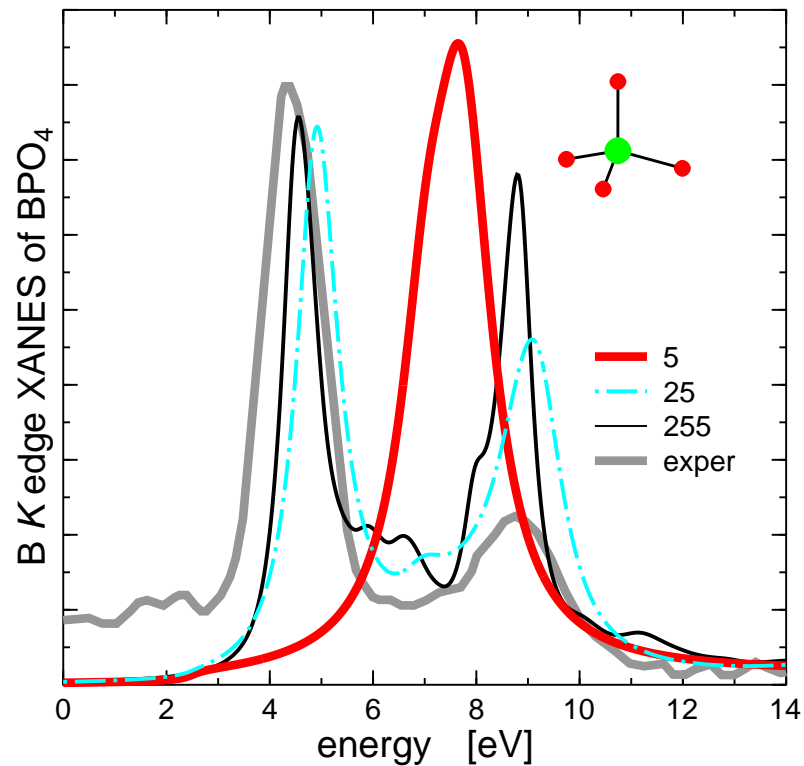
- “Systematic” deviations between theory and experiment
- Pre-edge region XANES is prone to radiation damage — just consequence of BO_3 defects?
- Shoulder region: Displayed by **none** of the theoretical spectra at the BO_4 sites. Disorder, impurities, main peak of BO_3 units, ... ?

BPO₄ is peculiar



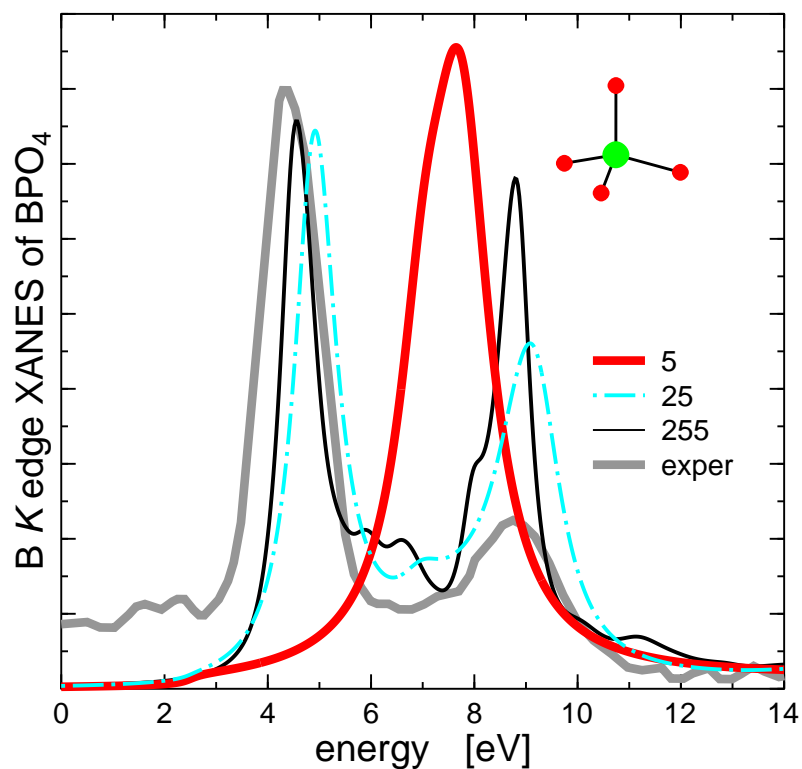
- XANES of BPO₄ does not fit into the typology

BPO₄ is peculiar



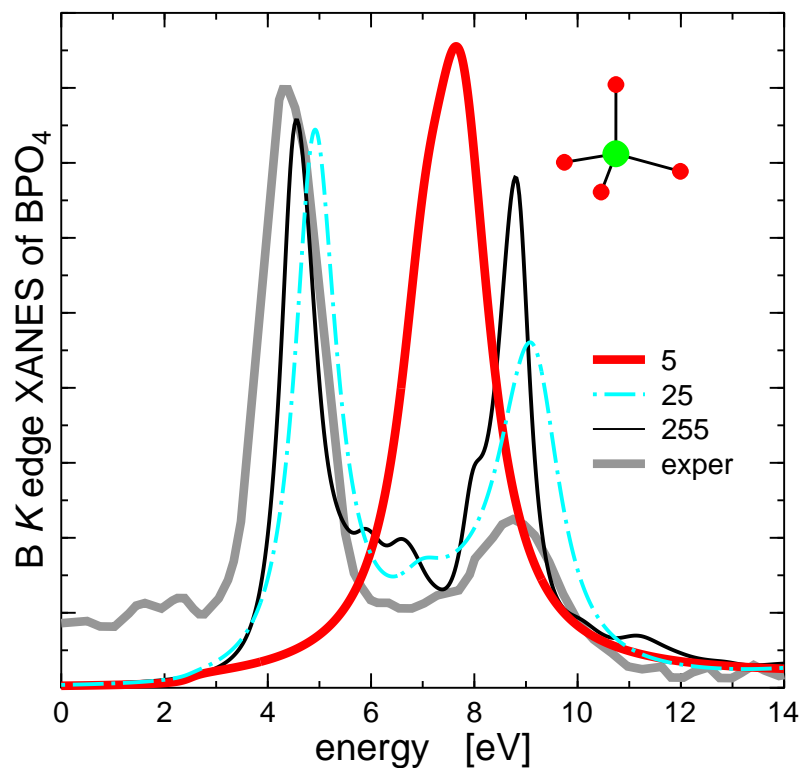
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- Spectra for small and large clusters differ considerably

BPO₄ is peculiar (and not useful)



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- Spectra for small and large clusters differ considerably
- XANES governed by **medium- and long-range order**
- Too symmetric to smooth out the contributions from distant atoms

BPO₄ is peculiar (and not useful)



- XANES of BPO₄ does not fit into the typology
- Spectra for small and large clusters differ considerably
- XANES governed by **medium- and long-range order**
- Too symmetric to smooth out the contributions from distant atoms
- Not useful for fingerprinting XANES of **glasses**

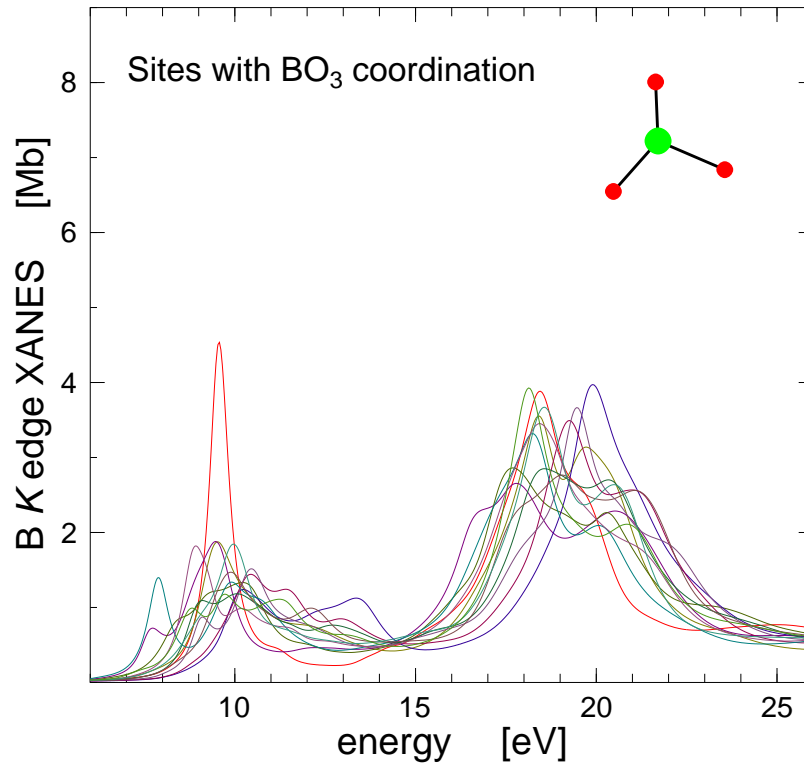
Minerals with borons in both BO_3 and BO_4 units


Minerals with both BO_3 and BO_4

name	formula	BO_3	BO_4
boracite	$\text{Mg}_3\text{ClB}_7\text{O}_{13}$	1	6
borax	$\text{Na}_2\text{B}_4\text{O}_5(\text{OH})_4 \cdot 8(\text{H}_2\text{O})$	1	1
colemanite	$\text{CaB}_3\text{O}_4(\text{OH})_3 \cdot \text{H}_2\text{O}$	1	2
howlite	$\text{Ca}_2\text{SiB}_5\text{O}_9(\text{OH})_5$	1	4
kernite	$\text{Na}_2\text{B}_4\text{O}_6(\text{OH})_2 \cdot 3(\text{H}_2\text{O})$	2	2
kurnakovite	$\text{MgB}_3\text{O}_3(\text{OH})_5 \cdot 5(\text{H}_2\text{O})$	1	2
meyerhofferite	$\text{Ca}_2\text{B}_6\text{O}_6(\text{OH})_{10} \cdot 2(\text{H}_2\text{O})$	1	2
probertite	$\text{NaCaB}_5\text{O}_7(\text{OH})_4 \cdot 3(\text{H}_2\text{O})$	2	3
tincalconite	$\text{Na}_2\text{B}_4\text{O}_5(\text{OH})_4 \cdot 3(\text{H}_2\text{O})$	1	1
ulexite	$\text{NaCaB}_5\text{O}_6(\text{OH})_6 \cdot 5(\text{H}_2\text{O})$	2	3

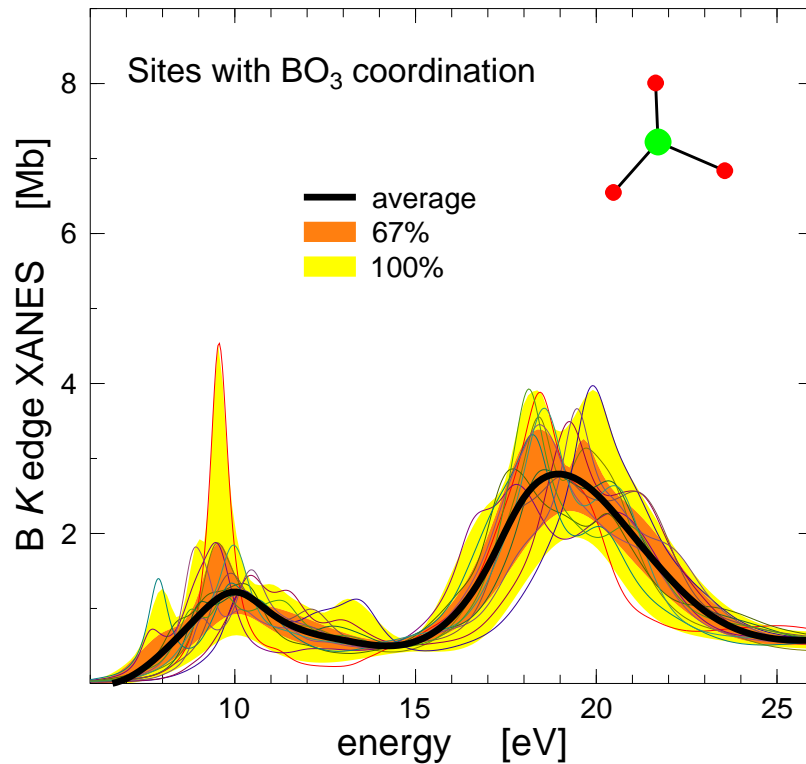
- Spectra generated at inequivalent sites of the same system are aligned one to another by the theory

Spectra of borons in BO_3 units



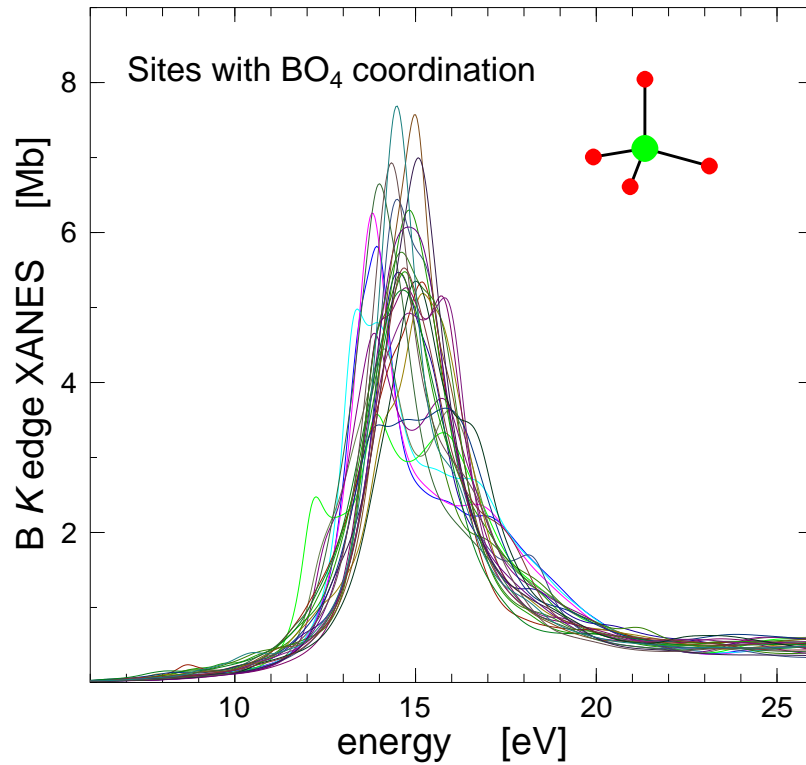
 13 sites, 10 minerals

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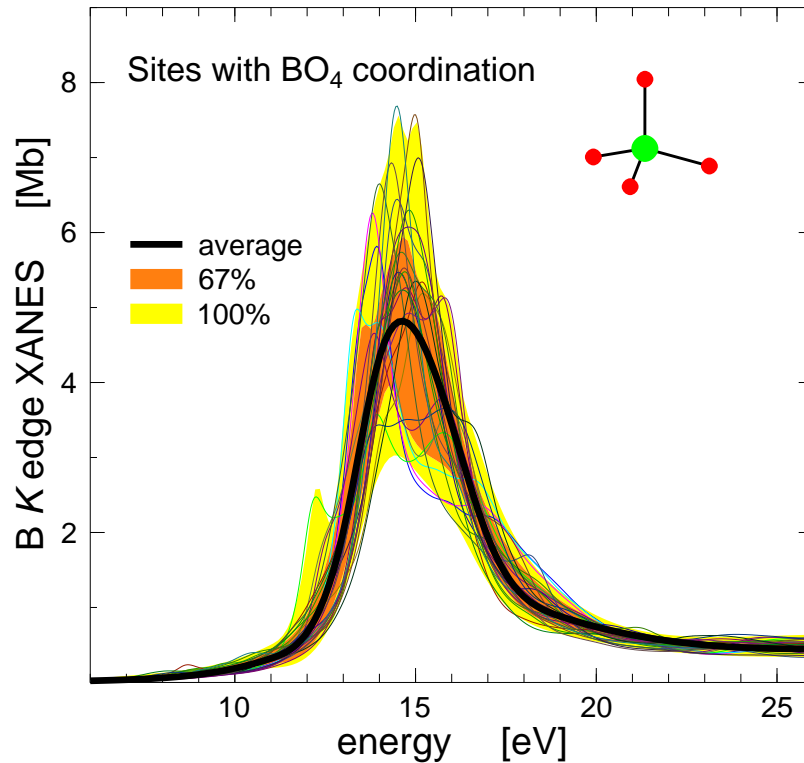
- 13 sites, 10 minerals
- Confidence intervals — either 67% or 100% of all curves fall within these limits

Spectra of borons in BO_4 units



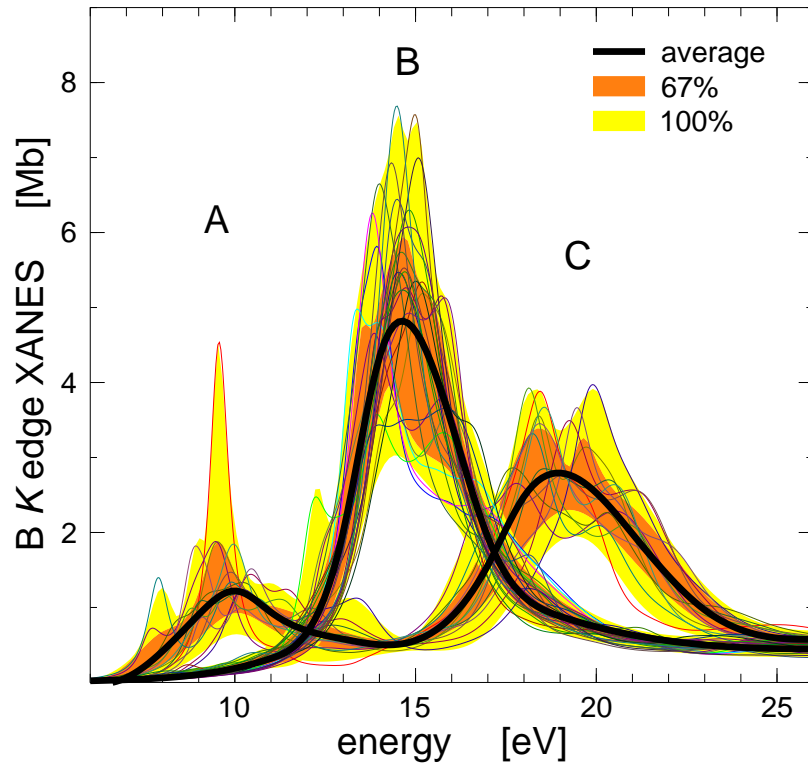
● 26 sites, 10 minerals

Spectra of borons in BO_4 units



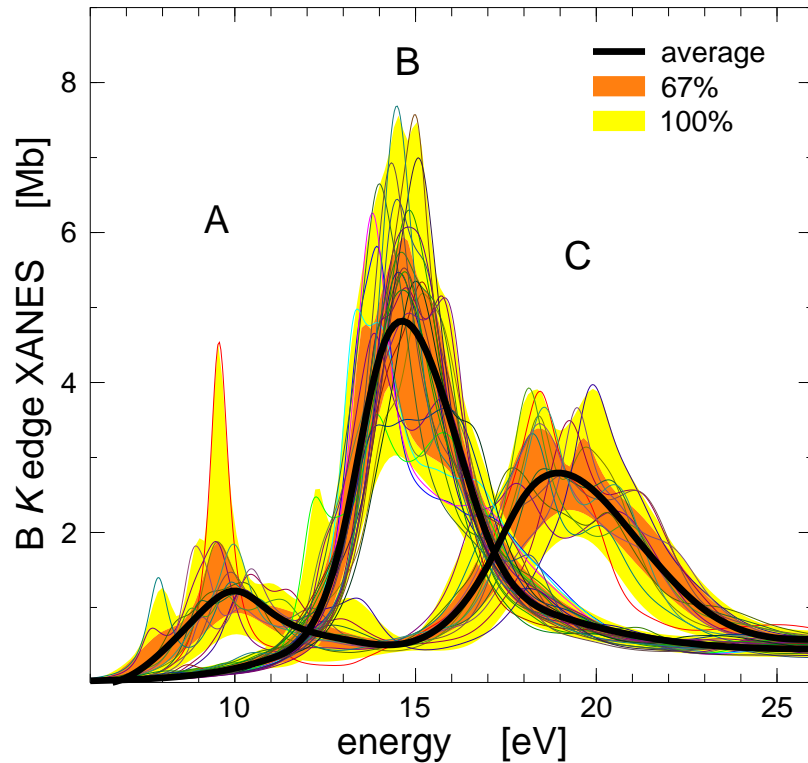
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Markers of BO_3 and BO_4



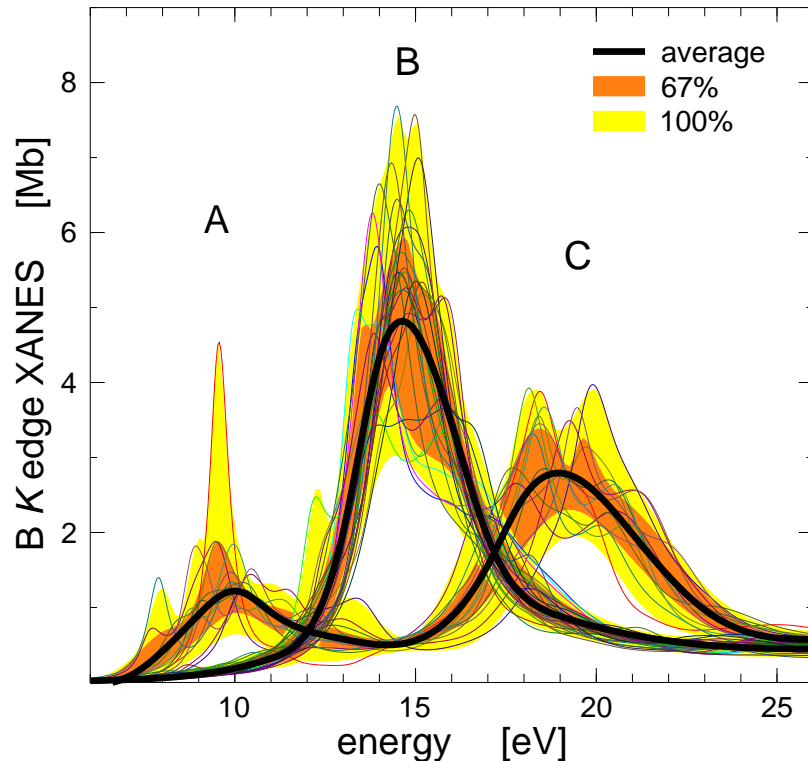
● Features characteristic for BO_3 or BO_4 coordinations well separated

Markers of BO_3 and BO_4



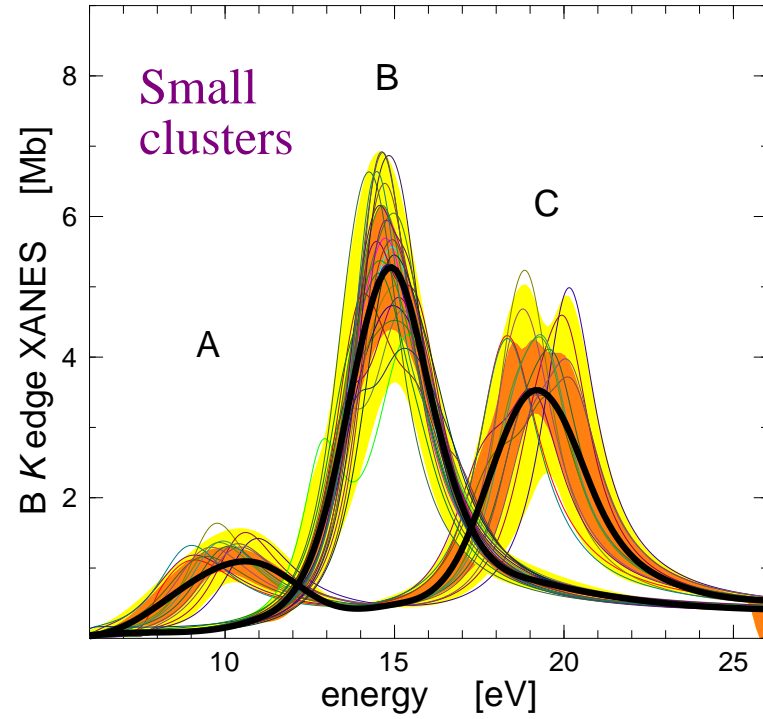
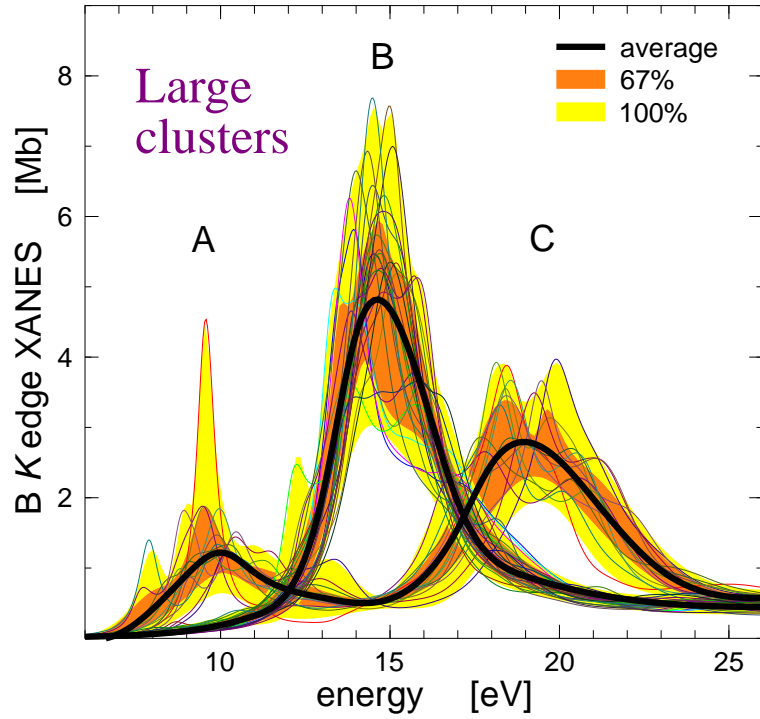
- Features characteristic for BO_3 or BO_4 coordinations well separated
- Similar picture obtained no matter what scattering potential is used

Markers of BO_3 and BO_4



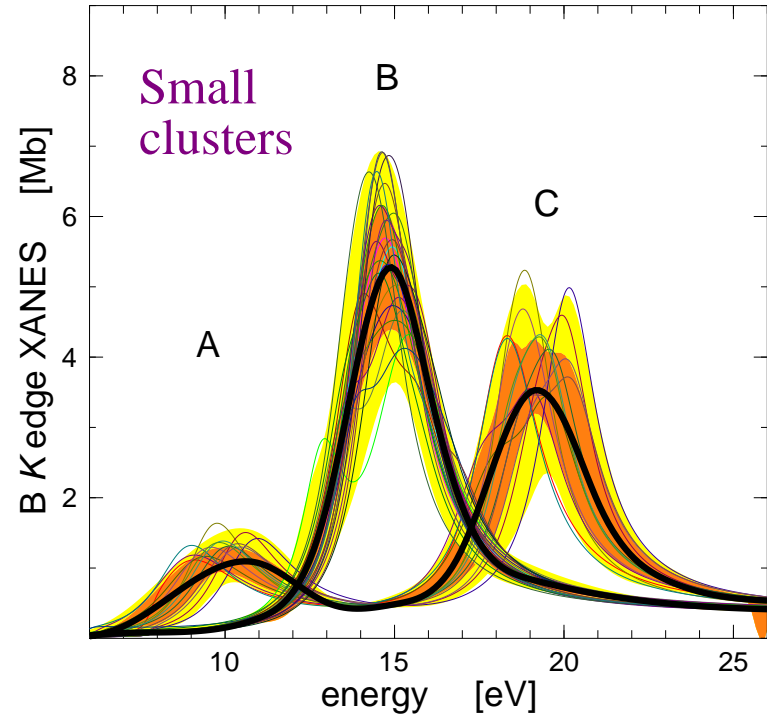
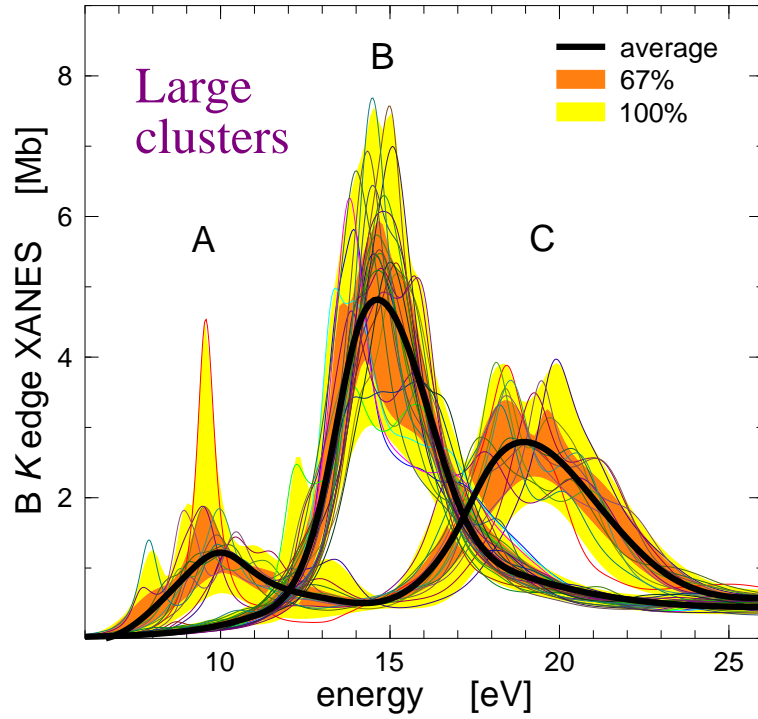
- Features characteristic for BO_3 or BO_4 coordinations well separated
- Similar picture obtained no matter what scattering potential is used
- B K edge is **well-suited for structural studies**

Short-range order is dominant



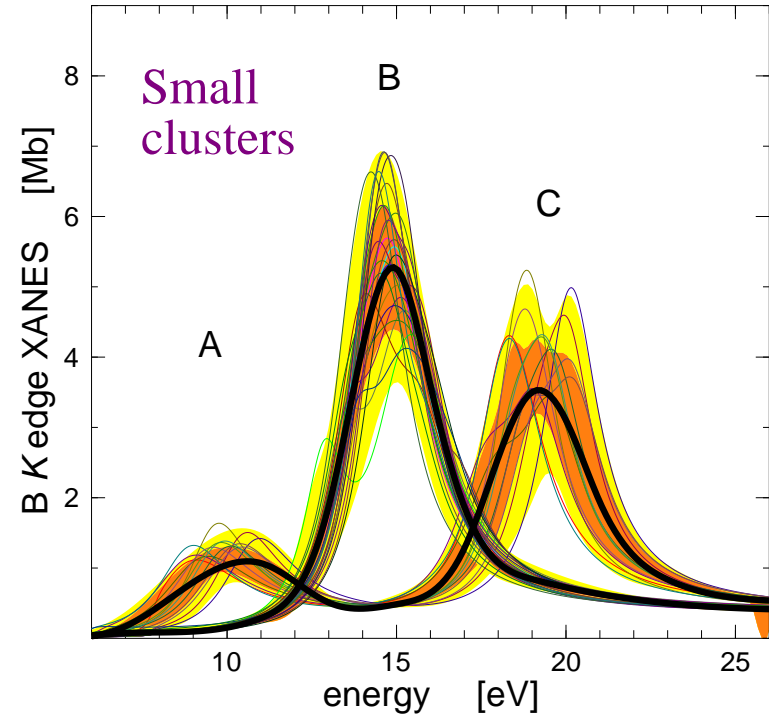
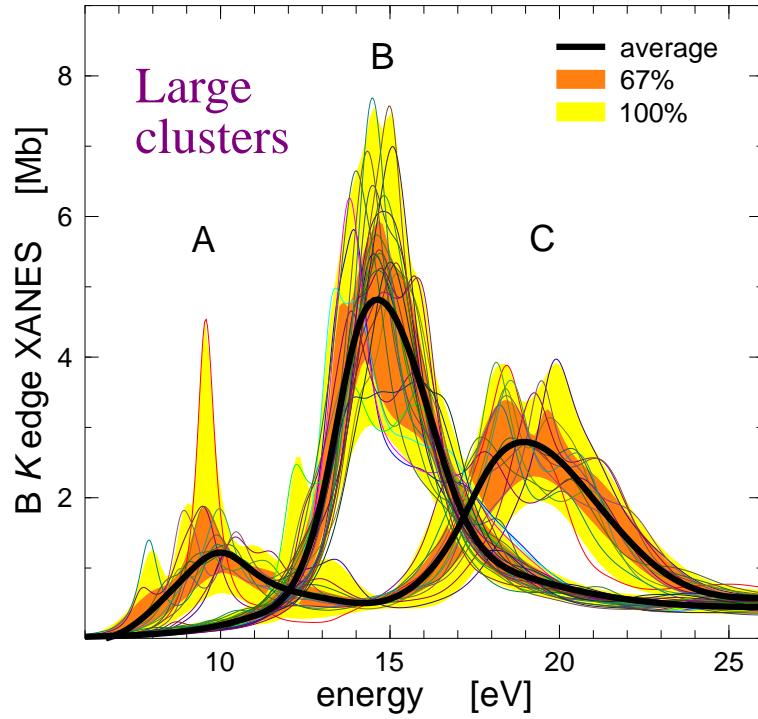
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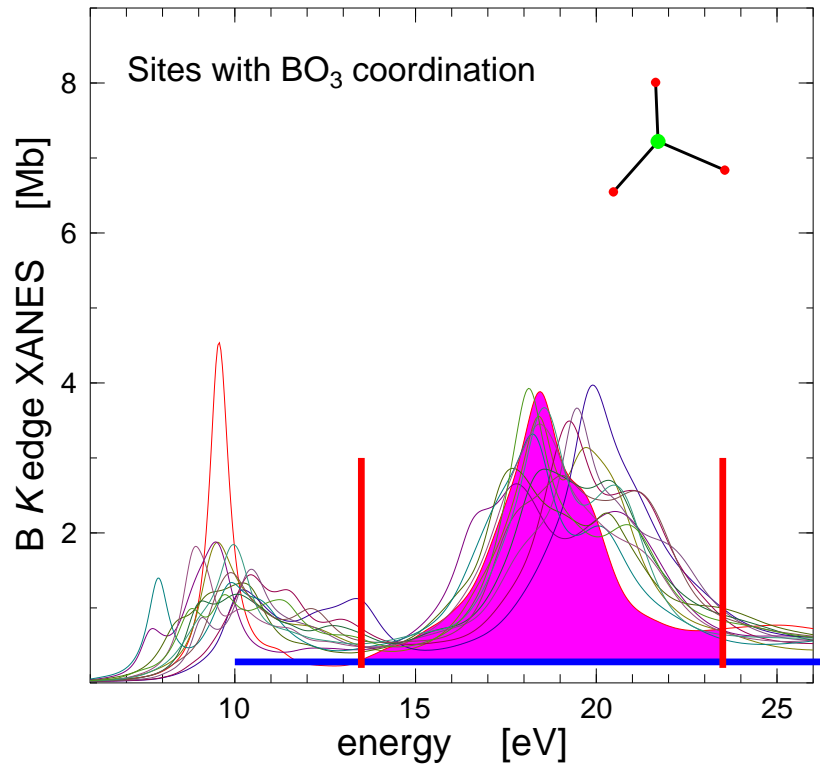


- Clusters of 140 atoms and of 4 or 5 atoms yield similar picture
- XANES shape is governed by short-range order
- Results may be transferred **from crystal to glasses**

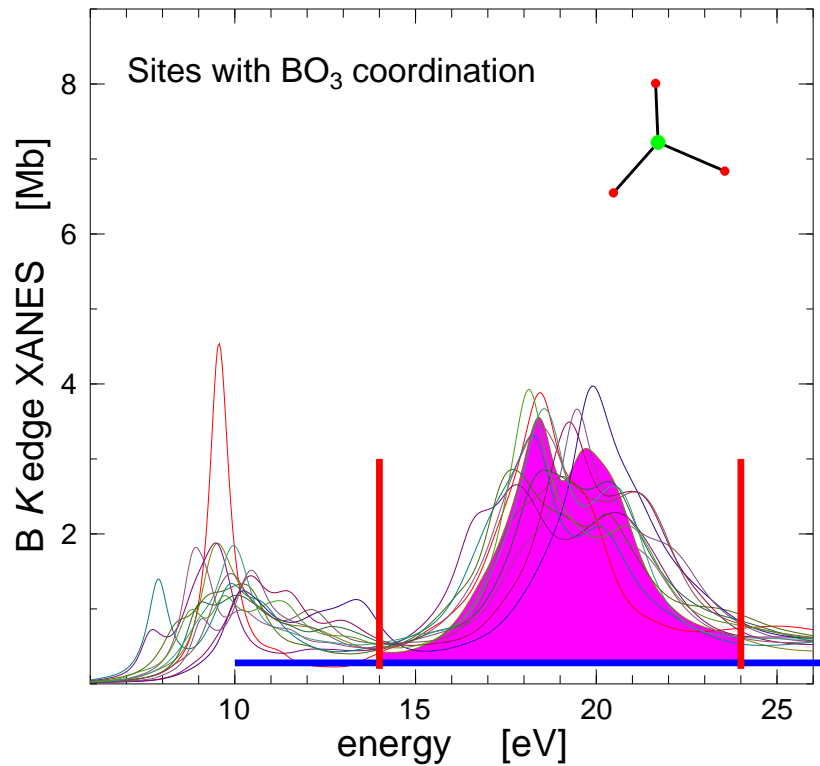
Trying to make
quantitative estimates

Variations in peak areas (BO₃)

- Measuring peak area over a 10 eV range

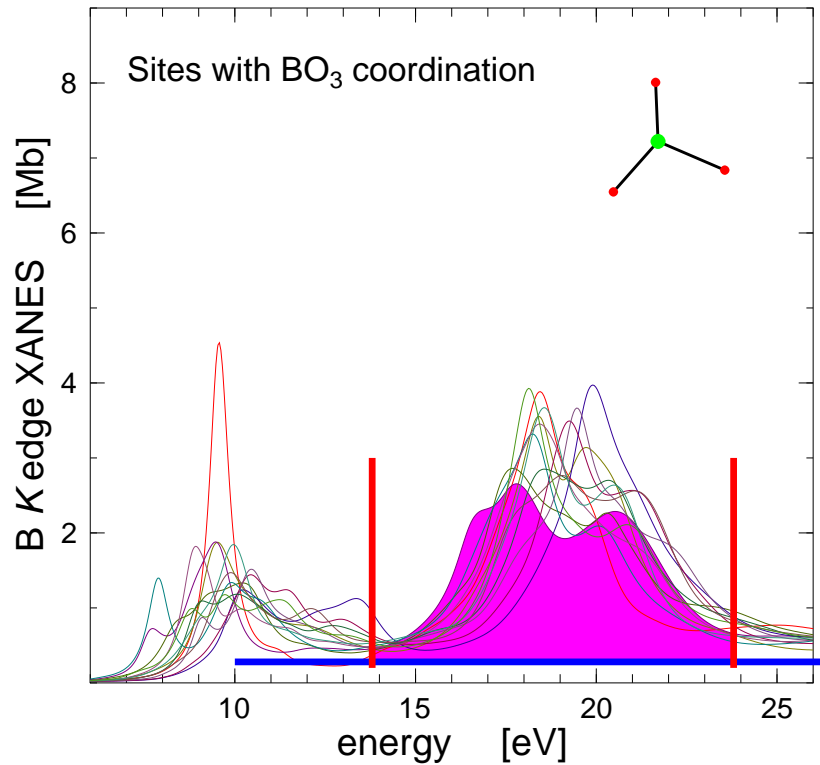


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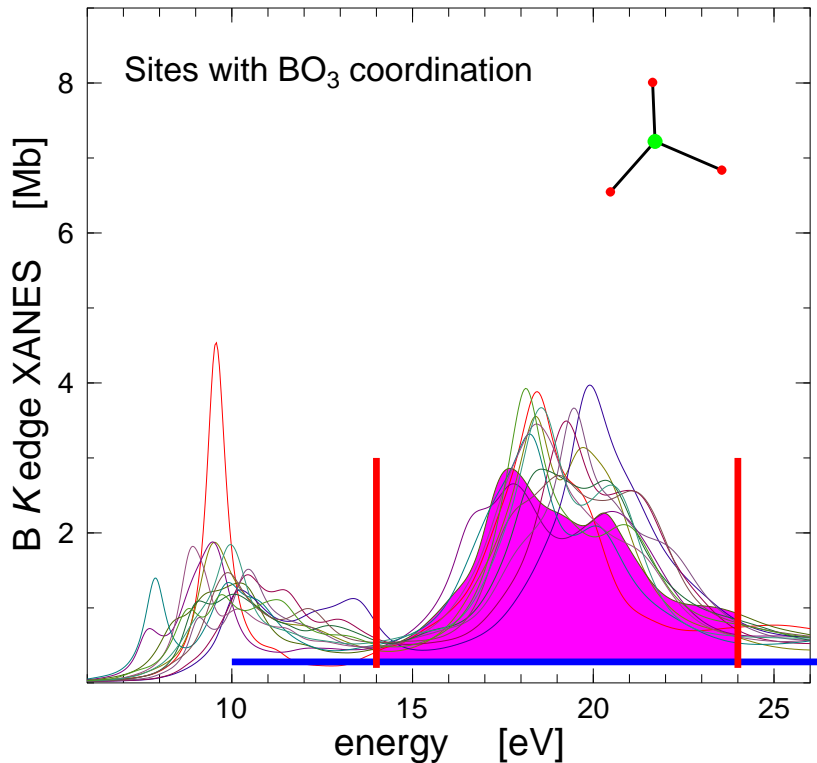
- Measuring peak area over a 10 eV range
- For each peak, find deviation of its area from the average

Variations in peak areas (BO₃)



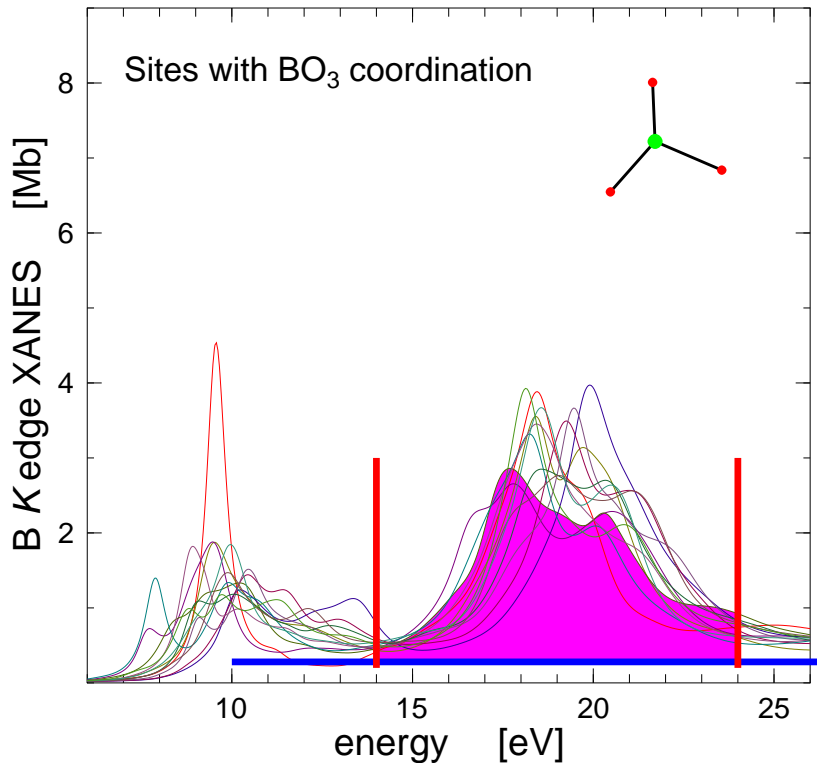
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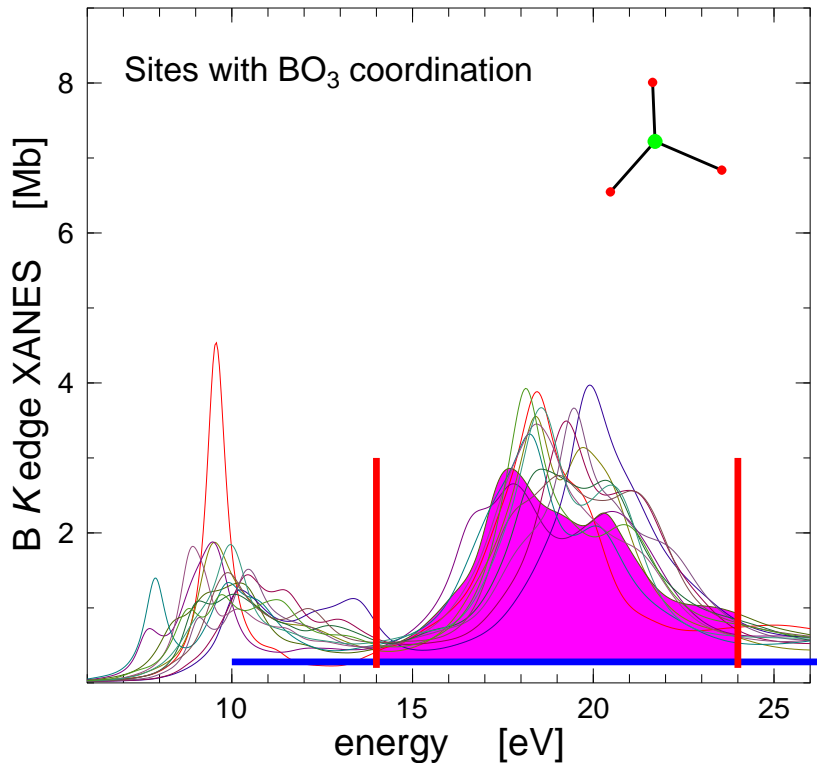
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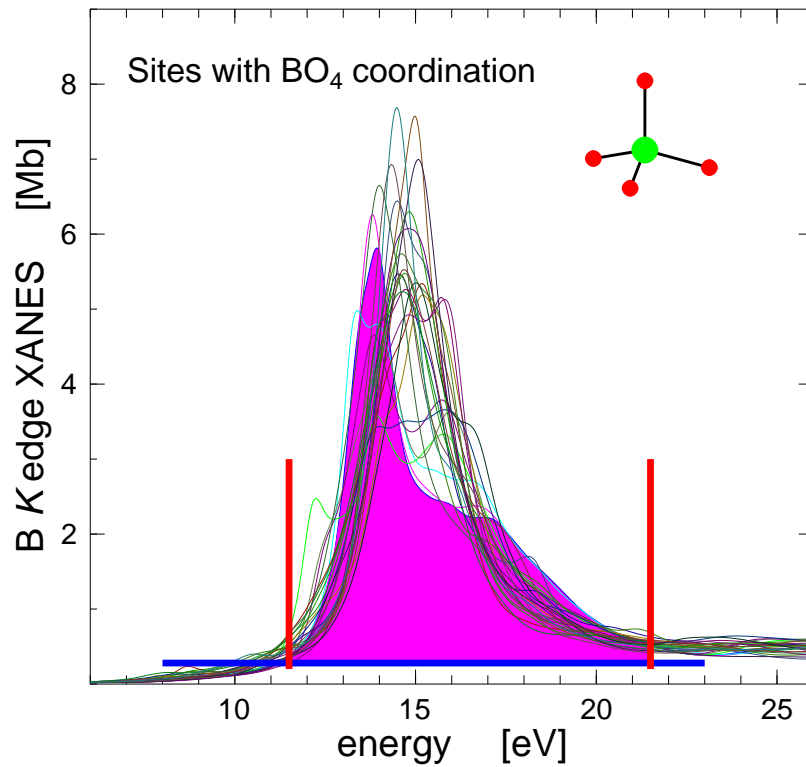
Variations in peak areas (BO₃)



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- Maximum deviation from the average is about 12%
- Choice of scattering potential and other “technical” parameters does not matter

Variations in peak areas

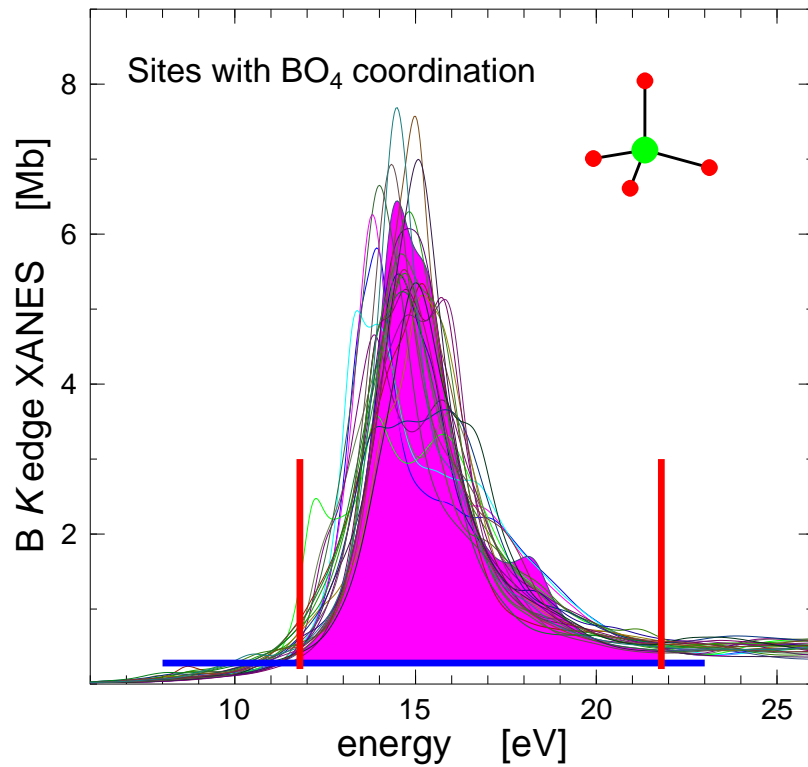
BO₄



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Variations in peak areas

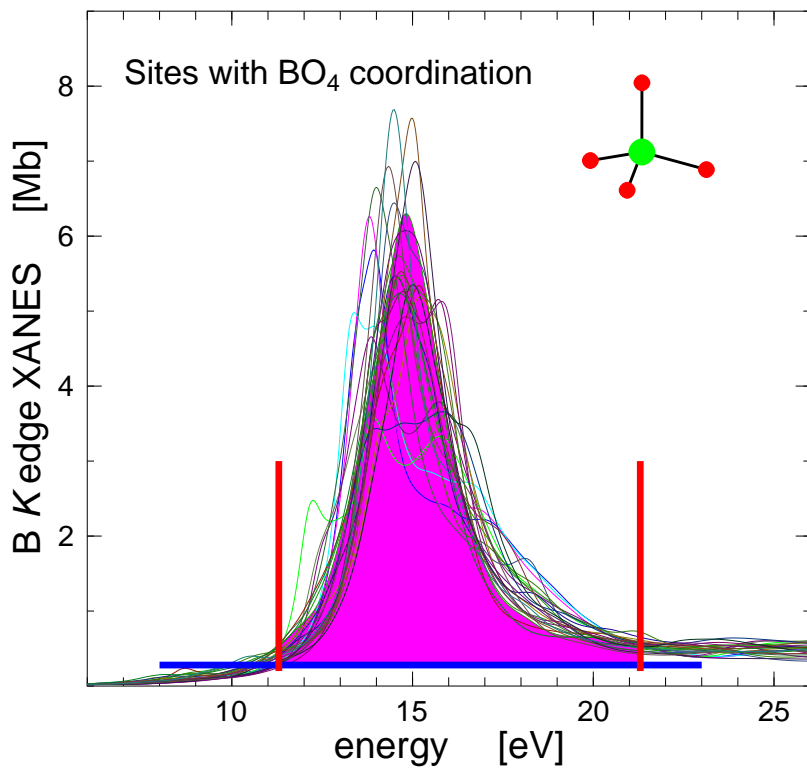
BO₄



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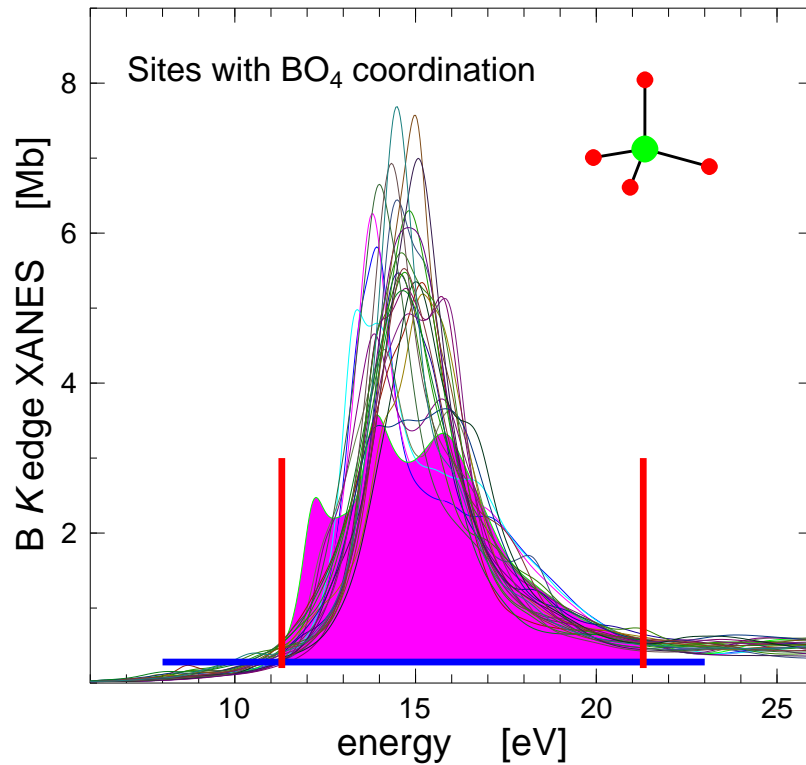
Variations in peak areas

BO₄



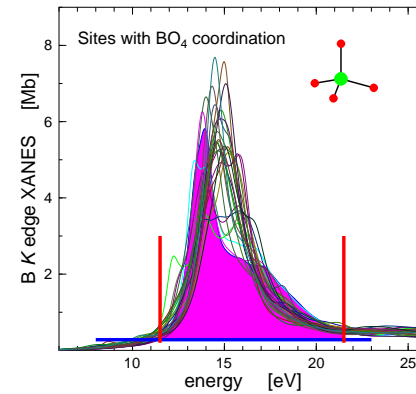
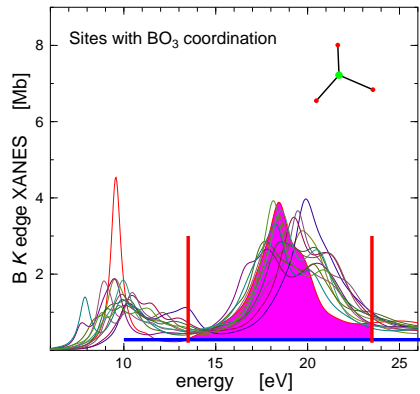
- Measuring peak area
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Variations in peak areas BO_4



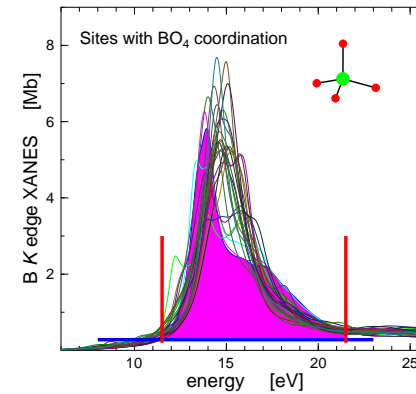
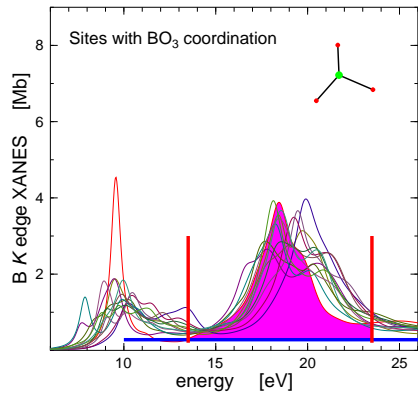
- Measuring peak area
- Find deviations from the average
- Statistics similar as in the case of BO_3 sites
- Standard deviation of the area is 4%, maximum deviation from the average is 12%

Quantifying ratio of BO_3 and BO_4



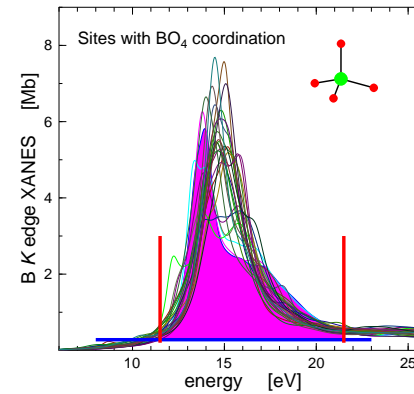
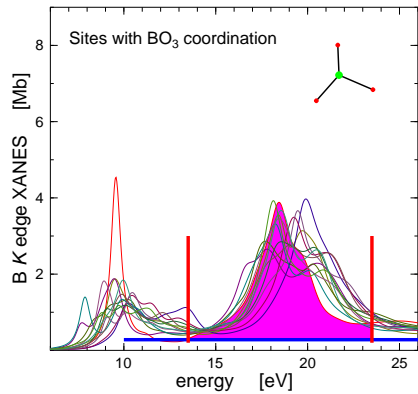
- Area of the main peak depends only on the number of nearest oxygens

Quantifying ratio of BO_3 and BO_4



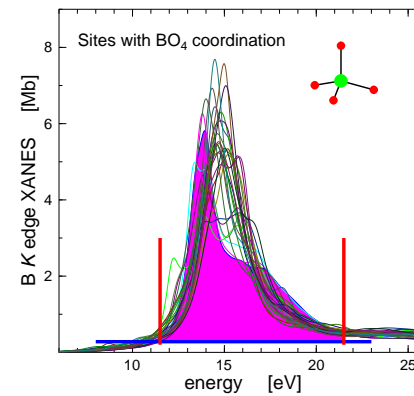
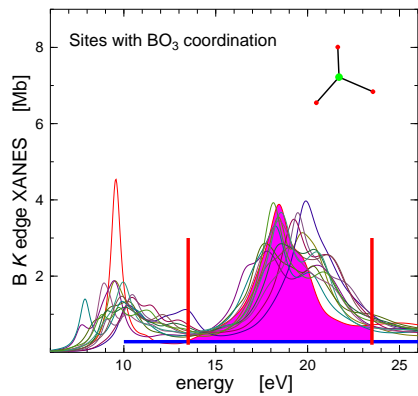
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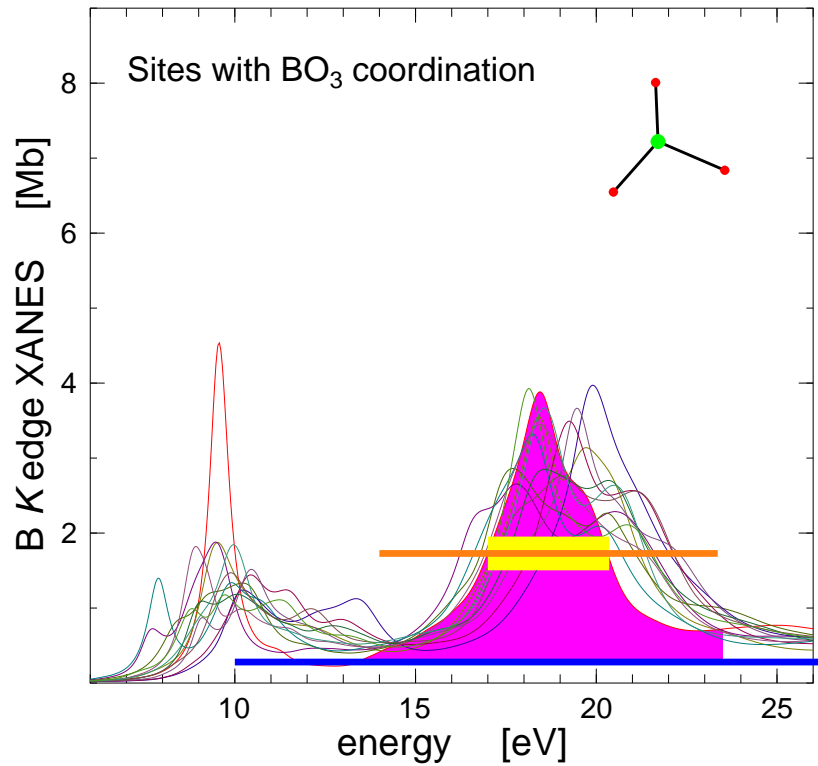
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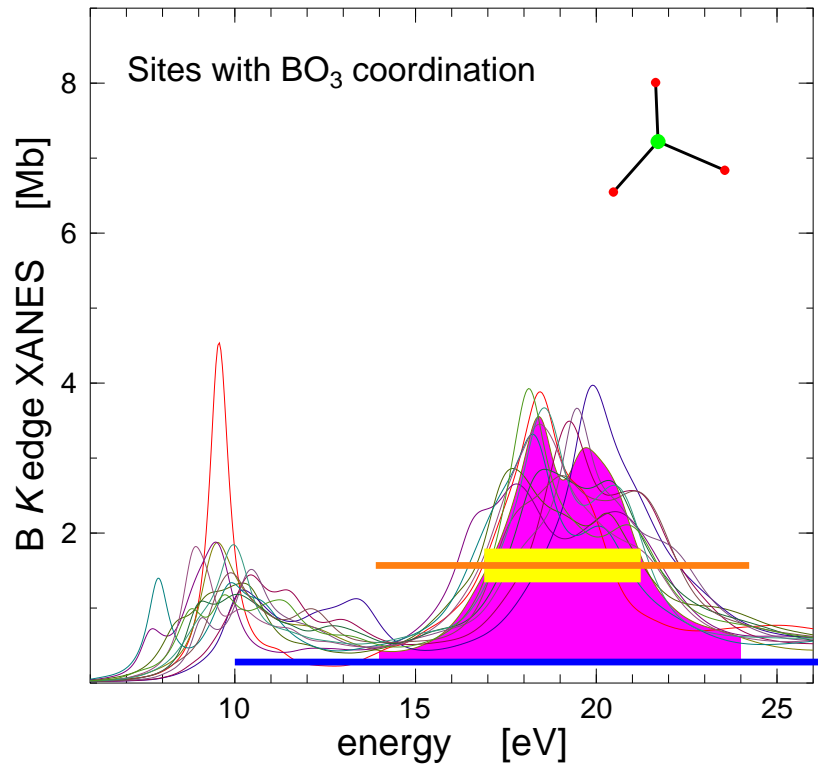
- Area of the main peak depends only on the **number of nearest oxygens** (it does not depend on compound, distances, middle-range order etc.)
- Ratio of areas of main peaks is a measure of the ratio of three-fold and four-fold boron sites
- Normalization: Area of main spectral peak at a BO_3 site constitutes $\sim 75\%$ of area of main spectral peak at a BO_4 site

Widths of main peaks — BO_3 sites



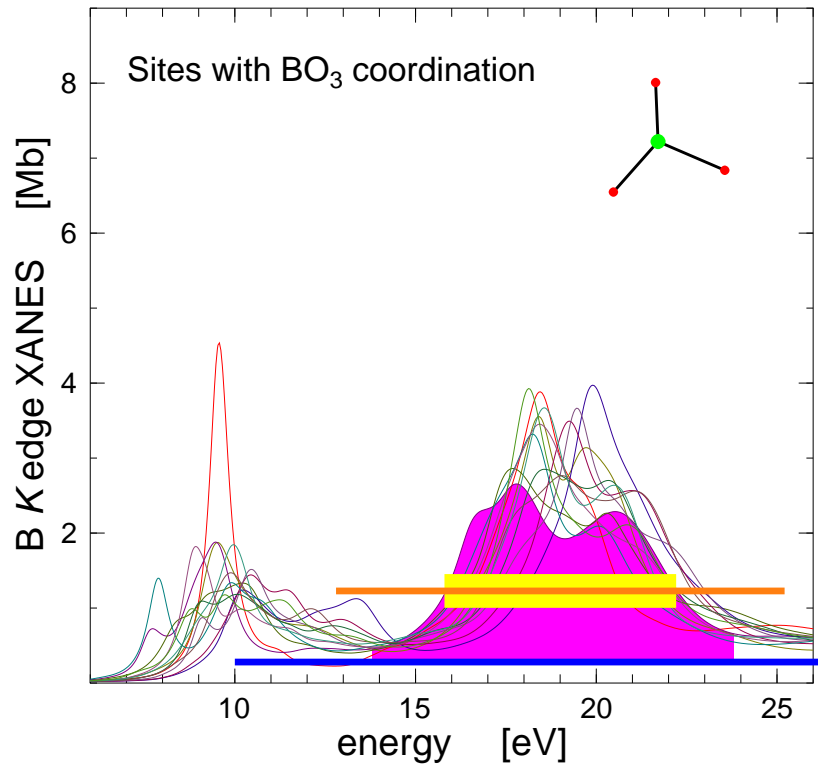
● Measuring width of the peak at 40% of its maximum height

Widths of main peaks — BO_3 sites



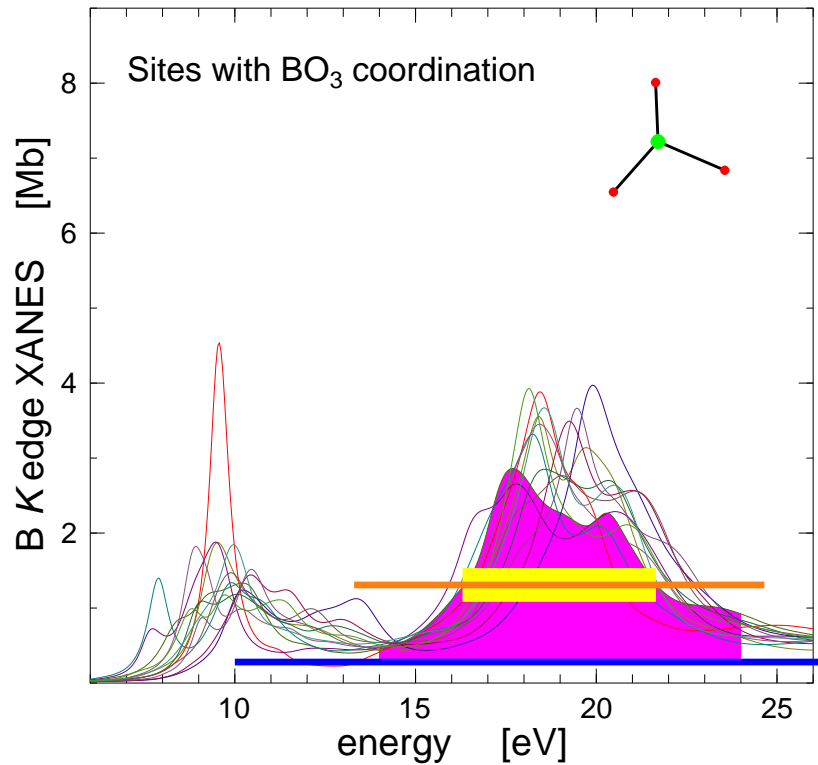
- Measuring width of the peak at 40% of its maximum height (full width at 0.4 of maximum)

Widths of main peaks — BO_3 sites



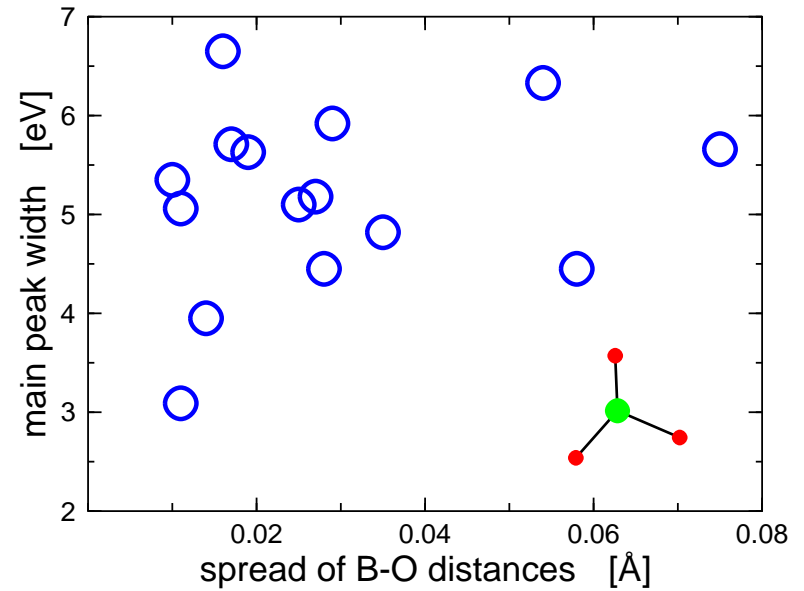
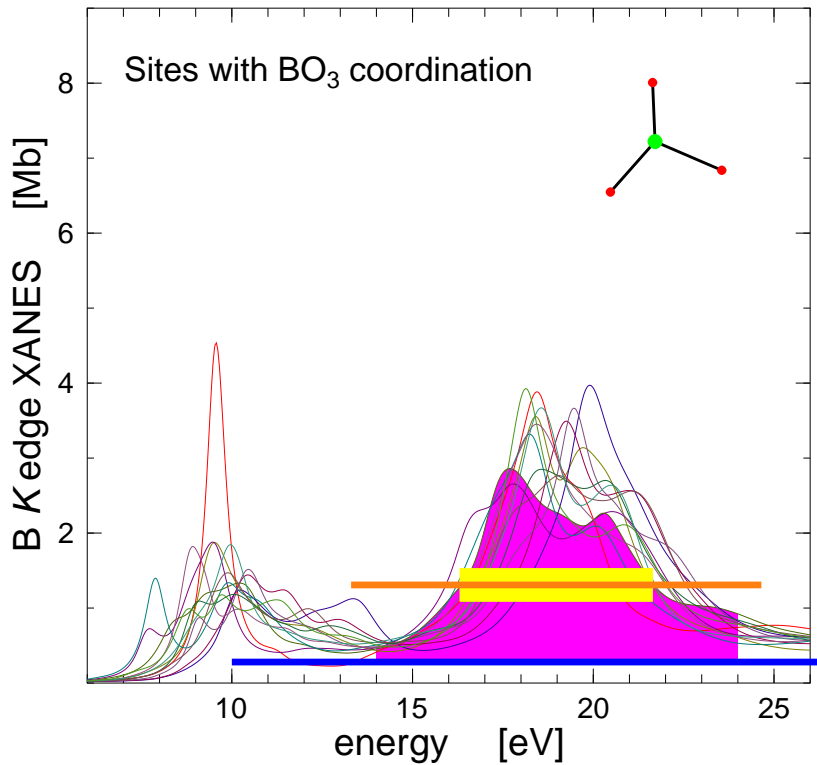
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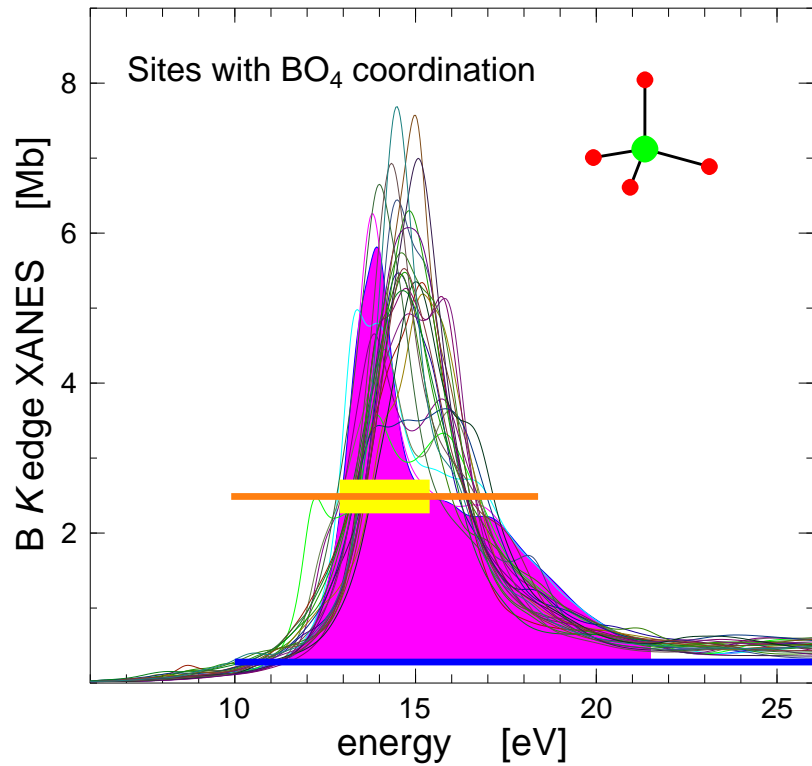
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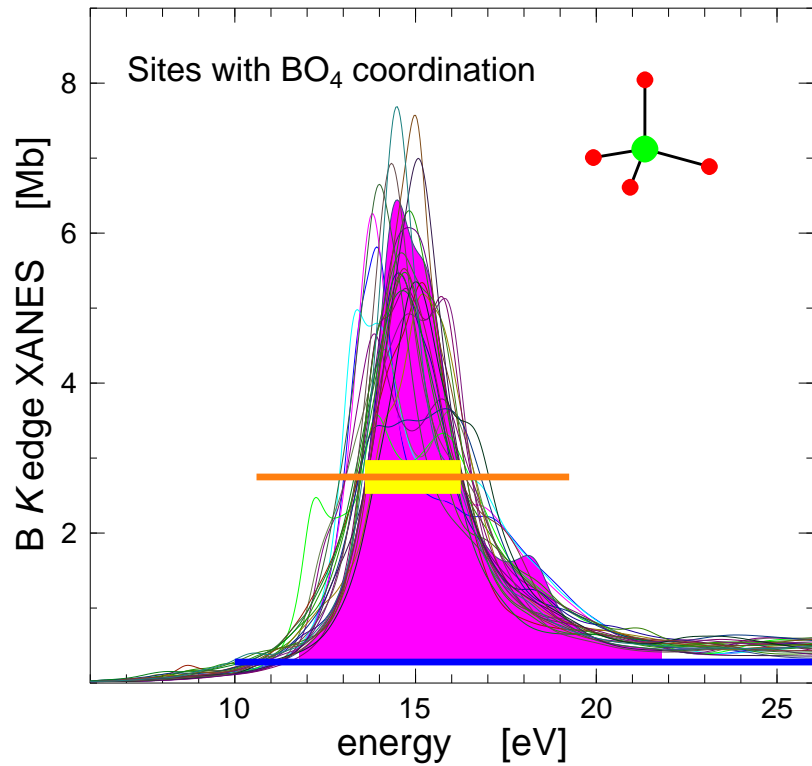
- No obvious relation between the spread of B–O distances and the width of the main peak

Widths of main peaks — BO_4 sites



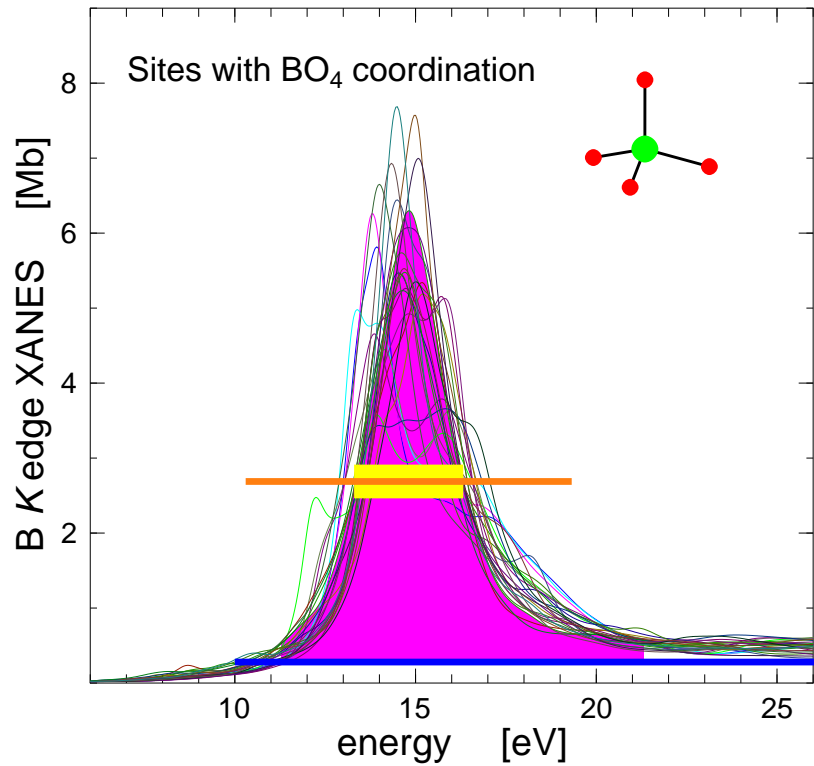
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Widths of main peaks — BO_4 sites



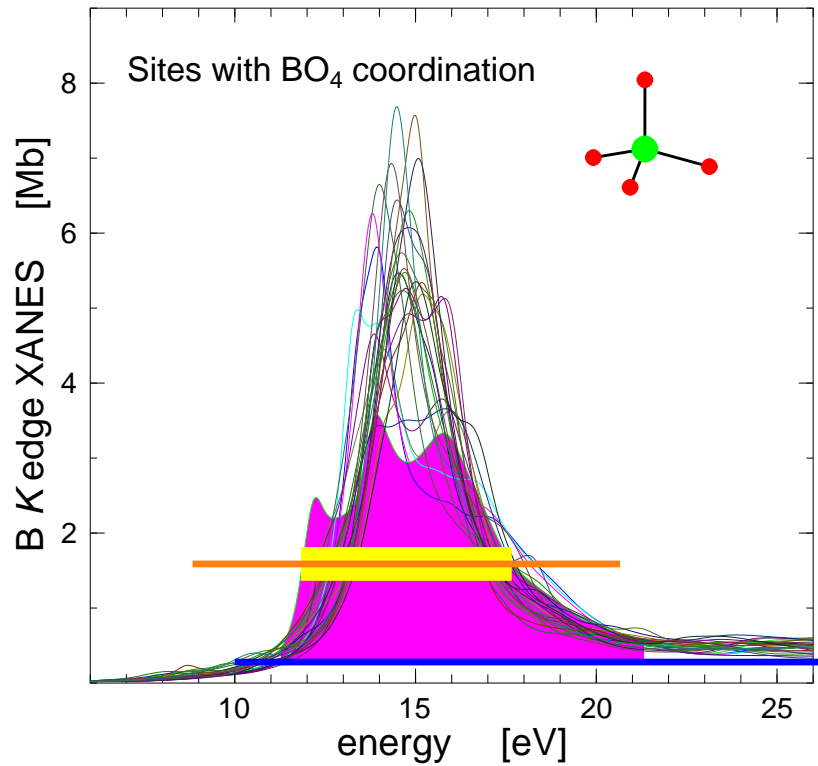
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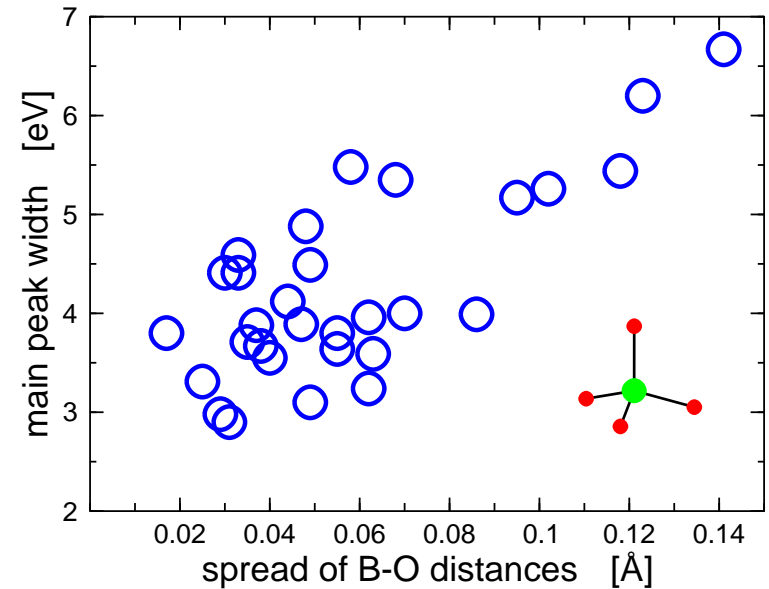
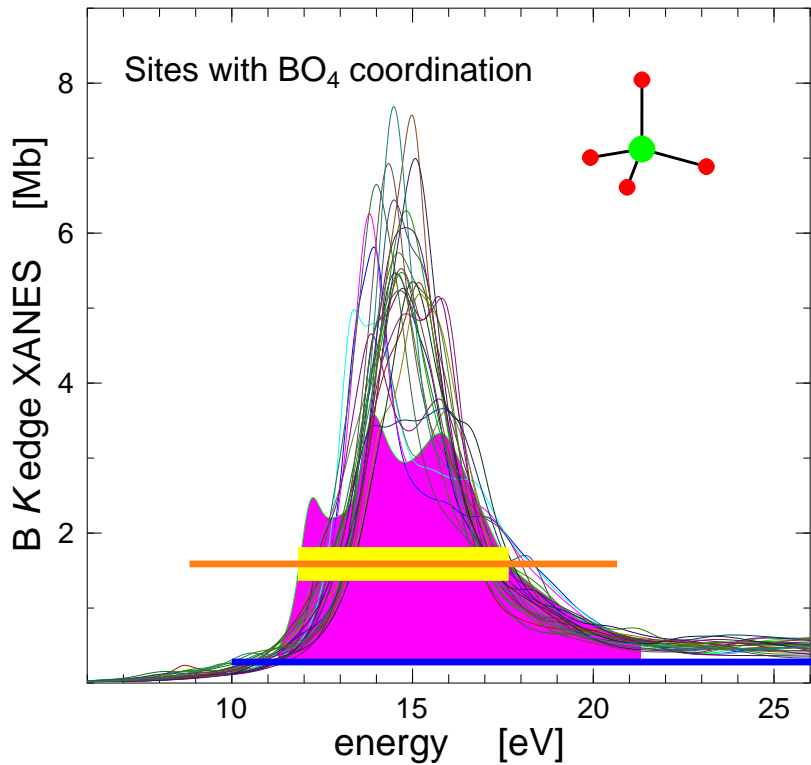
● Measuring width of the peak
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Widths of main peaks — BO_4 sites



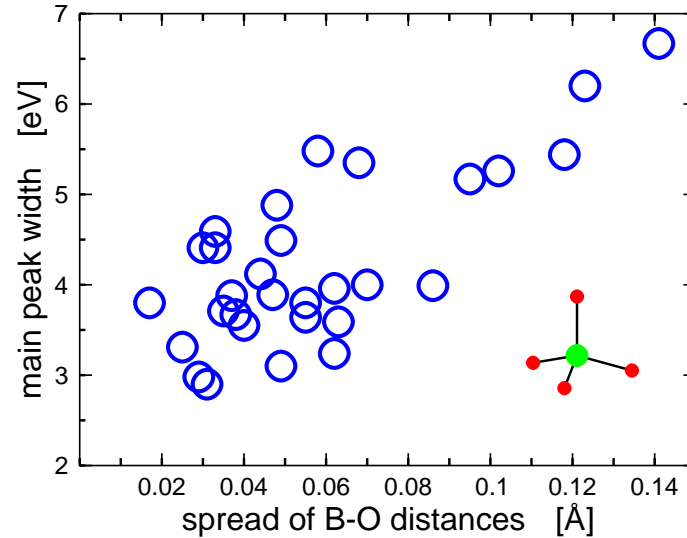
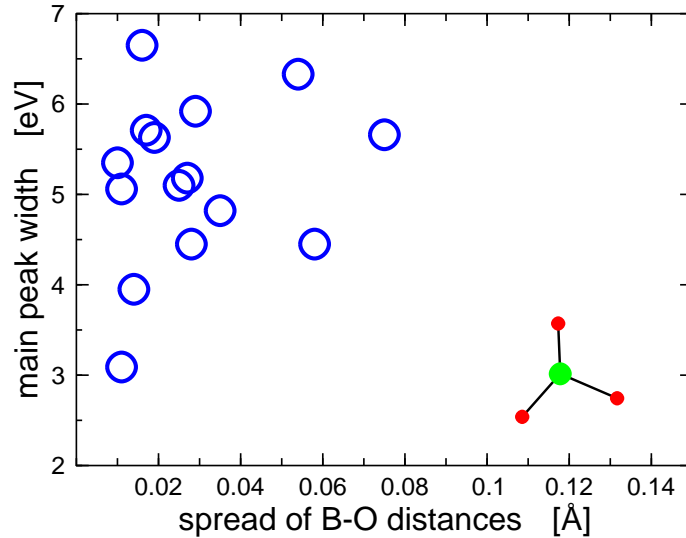
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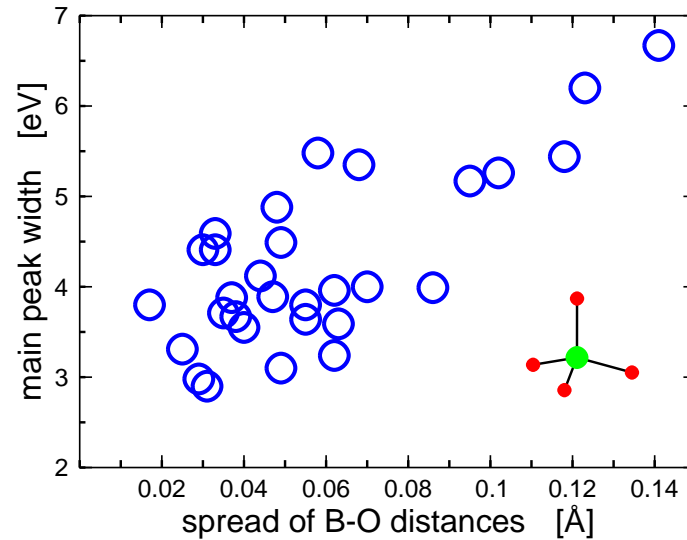
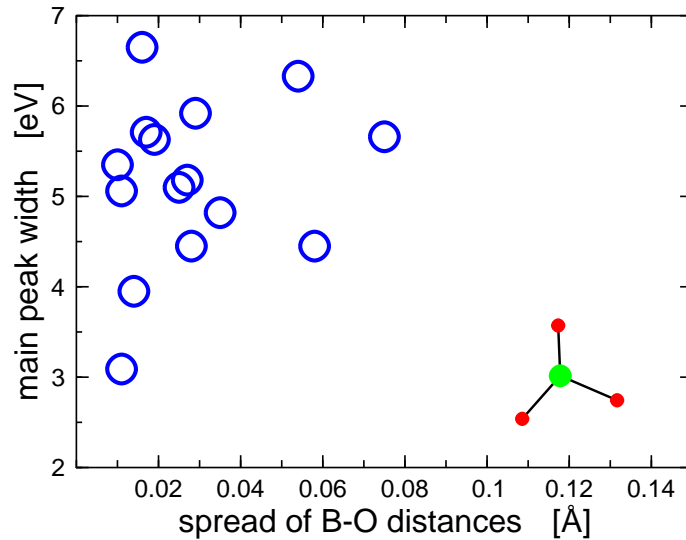
- There is *some relation* between spread of the B–O distances in the BO_4 tetrahedron and the width of the main peak

Peak widths and spread of distances



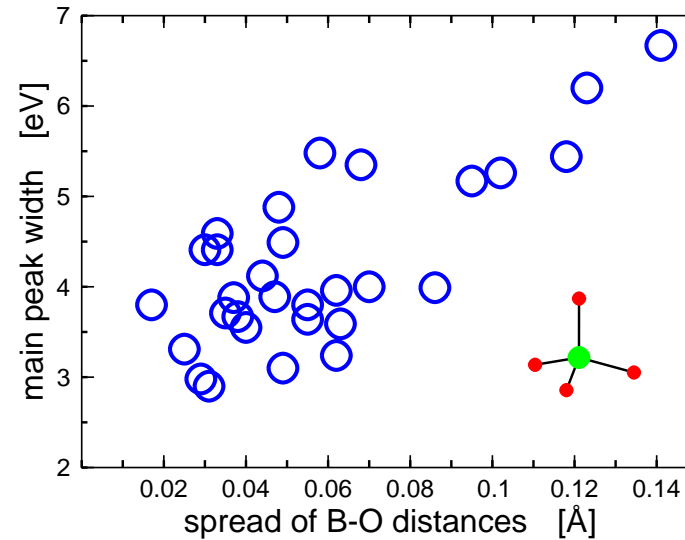
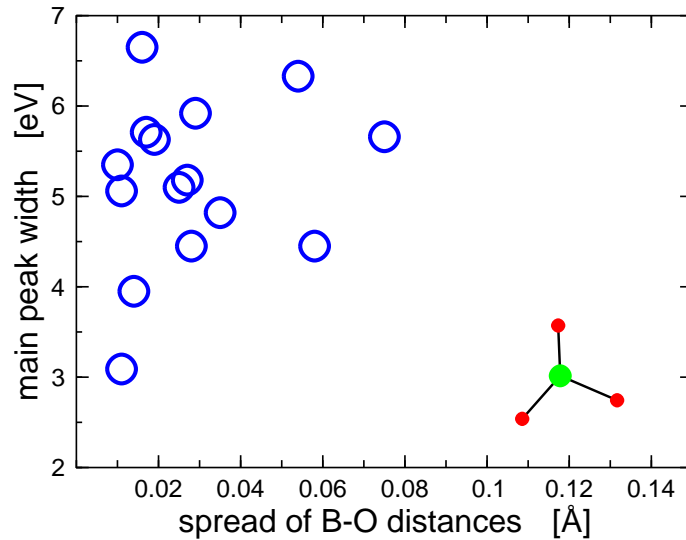
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- Even for spectra at BO_4 sites, there are significant deviations from the statistical relation
- Exceptionally large spread of B–O distances yields exceptionally broad peak

The end is getting near...

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- Areas of main peaks depend only on the number of nearest oxygens — can be used for **quantifying ratio of borons in BO_3 or BO_4 units**
- Width of main peak at BO_4 site is related to the spread of B–O distances (with a significant statistical noise for typical situations)