

Temperature-dependence of magnetism of free Fe clusters

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Outline

- Introducing finite-temperature magnetism (a bit of theory)

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- Dependence of mean magnetization of clusters on temperature and on cluster size
- Critical (“Curie”) temperature T_c of clusters
- Temperature-dependence of magnetic profiles of clusters

Motivation

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Lowering the coordination number

- **increase** of magnetic moments
- **decrease** of coupling
- **enhanced** magnetization
- **reduced** magnetization

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Rule of thumb for studying different geometries:

follow the *coordination number* !

Lowering the coordination number

- | | |
|---------------------------------------|---------------------------------|
| → increase of magnetic moments | → enhanced magnetization |
| → decrease of coupling | → reduced magnetization |

When comparing surfaces with bulk:

competition between enhancement of magnetic moments
and reduction of their coupling

Bulk, surfaces, clusters, ...

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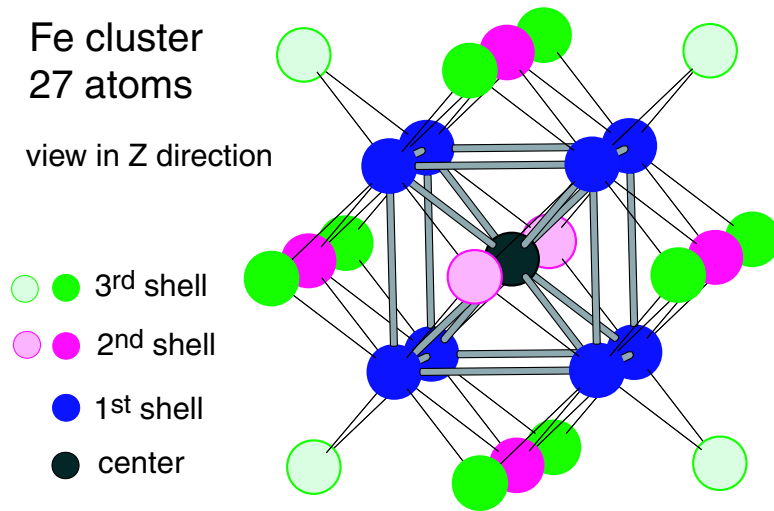
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- However, their properties *cannot* be expressed as a mere linear combination of surface and bulk contributions
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⇒ intuition has a limited role

⇒ one has to perform calculations **for the real stuff**

Systems to be studied

- Free spherical Fe clusters, geometry taken as if cut from a *bcc* Fe crystal
- Cluster sizes: between 9 atoms (1 coordination shell) and 89 atoms (7 coordinations shells)



shells	atoms	radius [a.u.]
1	9	4.70
2	15	5.42
3	27	7.67
4	51	8.99
5	59	9.39
6	65	10.85
7	89	11.82

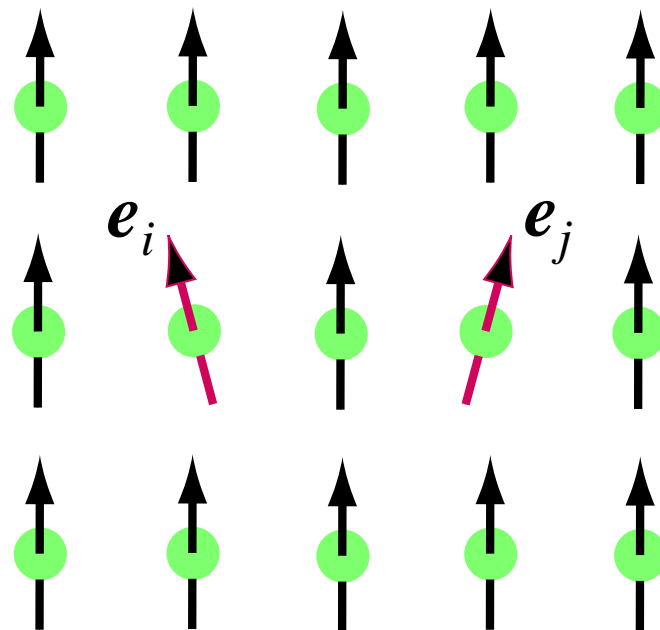
Calculations for $T = 0$

- *Ab-initio* within LDA framework (material specific)
- Scalar-relativistic **real-space** spin-polarized multiple-scattering formalism
- Atomic sphere approximation (ASA)
- Using SPRKKR code
<http://olymp.cup.uni-muenchen.de/ak/ebert/SPRKKR>

Calculations for $T \neq 0$

For localized moments, finite-temperature magnetism can be described by a **classical Heisenberg hamiltonian**

$$H_{\text{eff}} = - \sum_{i \neq j} J_{ij} \mathbf{e}_i \cdot \mathbf{e}_j$$



Mapping DFT onto Heisenberg

Coupling constants J_{ij} can be obtained from **ground-state** electronic properties:

$$J_{ij} = -\frac{1}{4\pi} \text{Im} \int^{E_F} dE \text{Tr} \left[(t_{i\uparrow}^{-1} - t_{i\downarrow}^{-1}) \tau_{\uparrow}^{ij} (t_{j\uparrow}^{-1} - t_{j\downarrow}^{-1}) \tau_{\downarrow}^{ji} \right]$$

[Liechtenstein *et al.* JMMM **67**, 65 (1987)]

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Valid only if magnetism can be described by localized magnetic moments (*fine for Fe*)

From J_{ij} to $M(T)$

- Mean magnetization $M(T)$ of a system described by a classical Heisenberg hamiltonian is

$$M(T) = \frac{\sum_k M_k \exp(-\frac{E_k}{k_B T})}{\sum_k \exp(-\frac{E_k}{k_B T})}$$

M_k is the magnetization of the system for a particular configuration k of the directions of spins
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- Practical evaluation: **Monte Carlo** method with the importance sampling Metropolis algorithm

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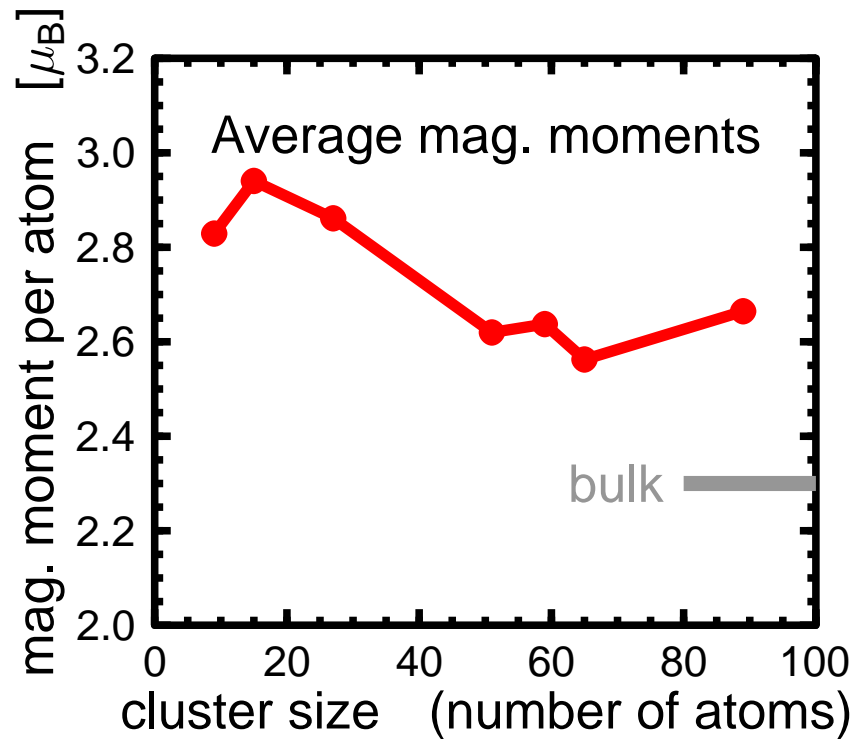
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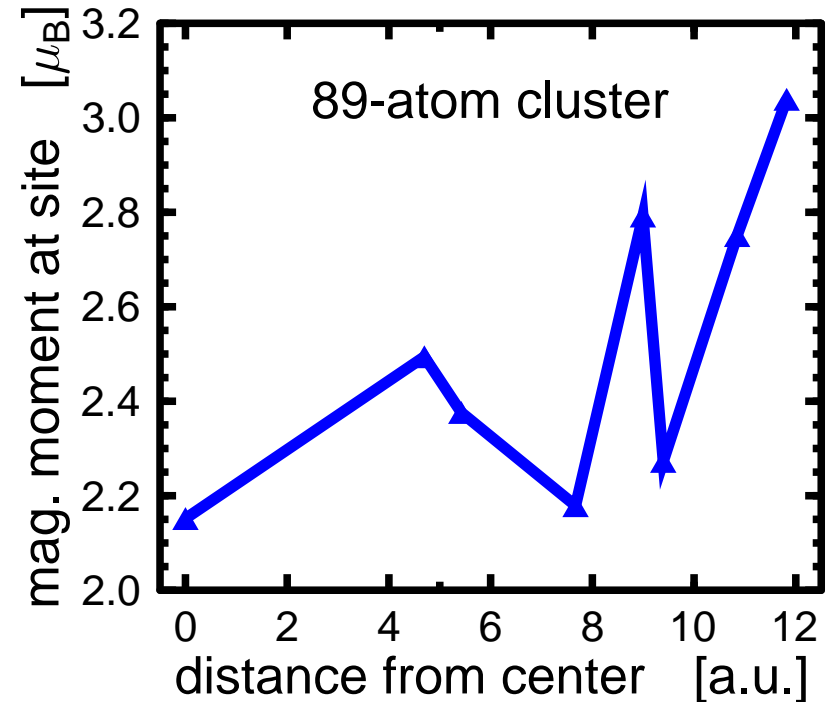
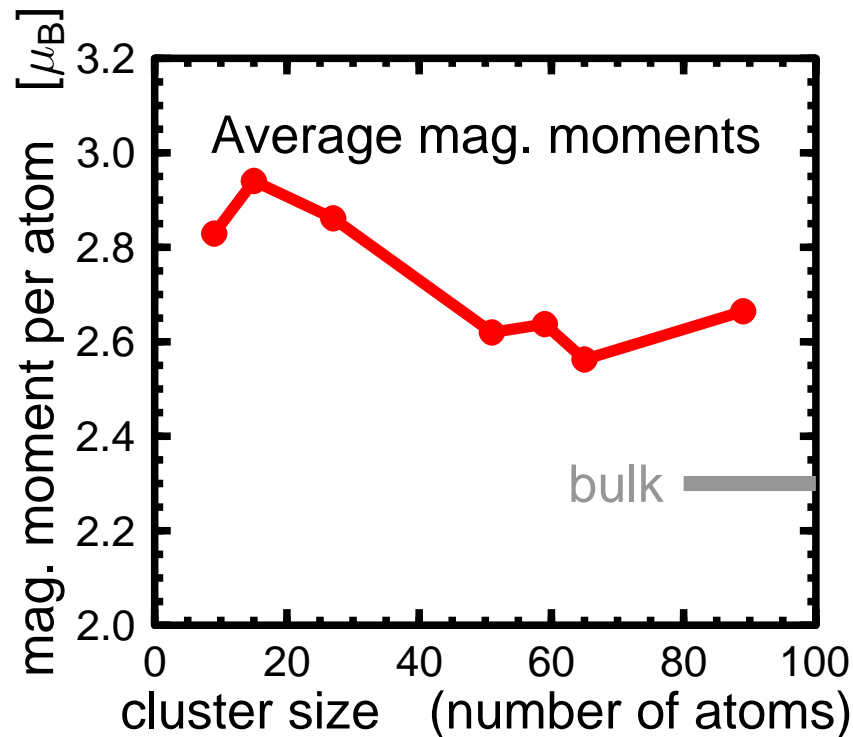
- Practical evaluation: **Monte Carlo** method with the importance sampling Metropolis algorithm
- For **bulk Fe**, this procedure yields finite-temperature results that are in a **good agreement** with experiment [Pajda *et al.* PRB **64**, 174402 (2001)]

Fe clusters at $T = 0$



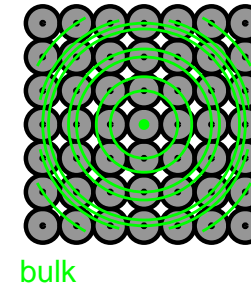
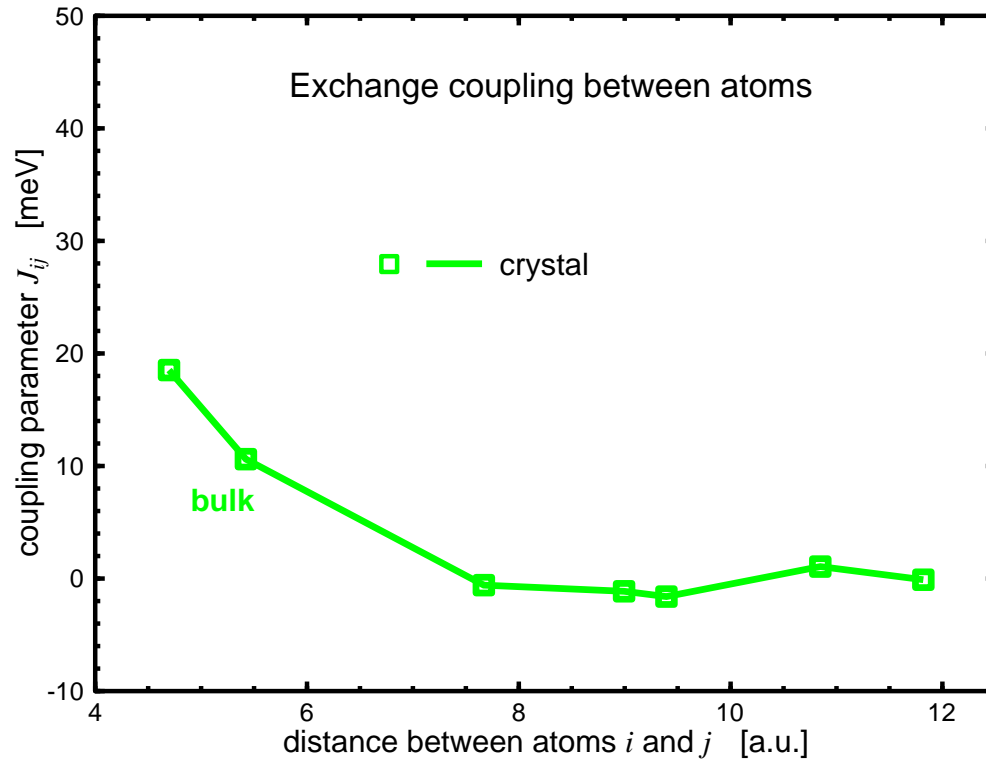
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- Further reading: O. Šipr *et al.* Phys. Rev. B **70**, 174423 (2004)

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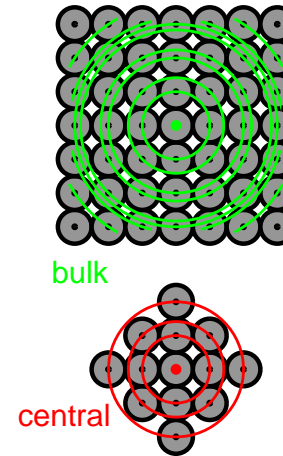
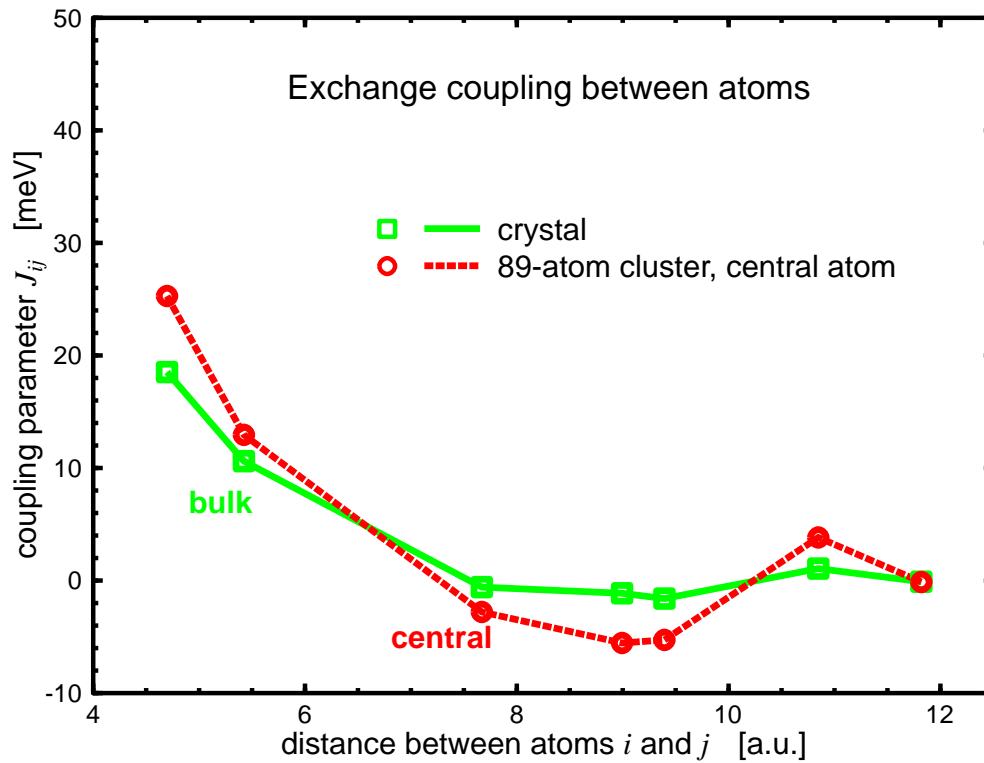
- Average magnetic moment of clusters **oscillates** with cluster size
- Local magnetic moments increase when going from the center outwards in an **oscillatory** way
- Further reading: O. Šipr *et al.* Phys. Rev. B **70**, 174423 (2004)

J_{ij} in bulk and in clusters



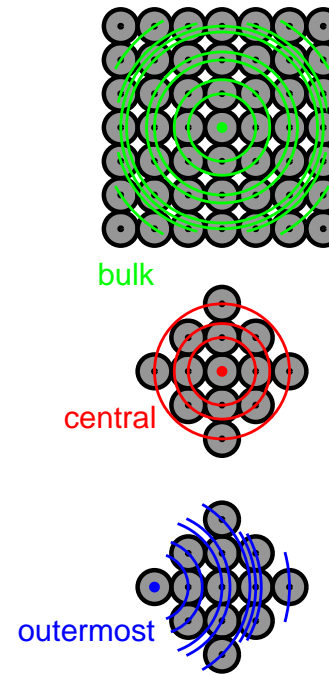
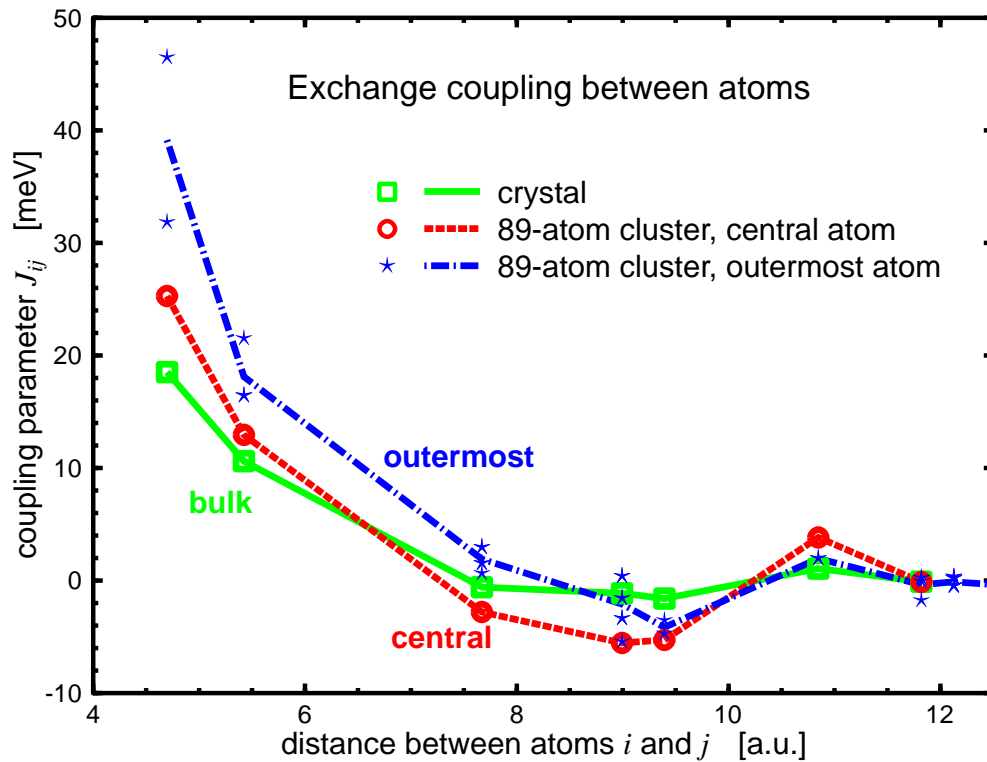
Atom i is fixed, atom j scans coordination shells around i

J_{ij} in bulk and in clusters



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Atom i is fixed, atom j scans coordination shells around i

- Oscillatory decay of J_{ij} with distance
- J_{ij} for a given distance **differs** a lot between clusters and crystals

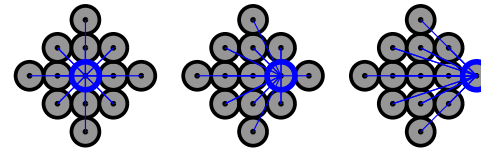
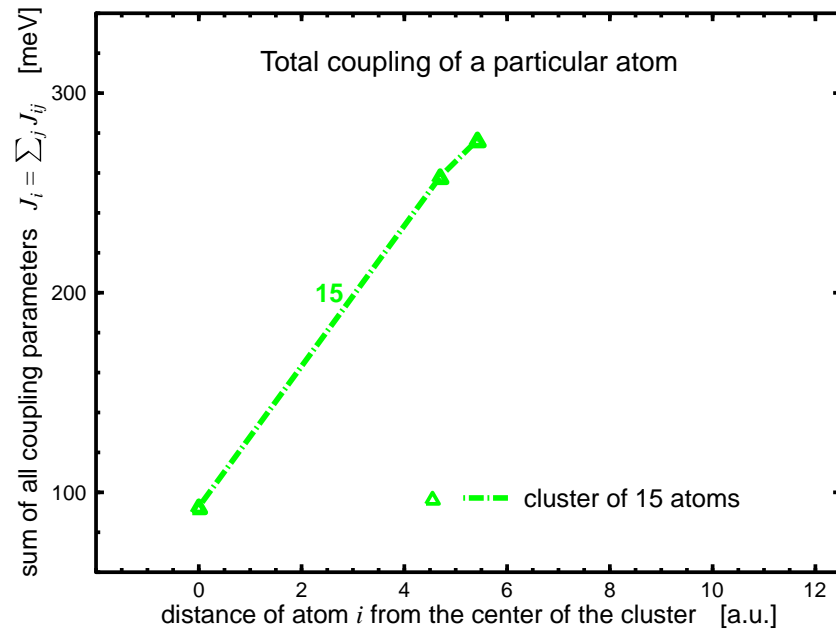
Site-dependence of $\sum_j J_{ij}$

Total strength with which one spin (at site i) is **held in its direction**:

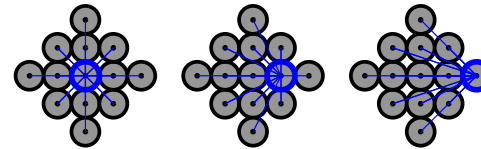
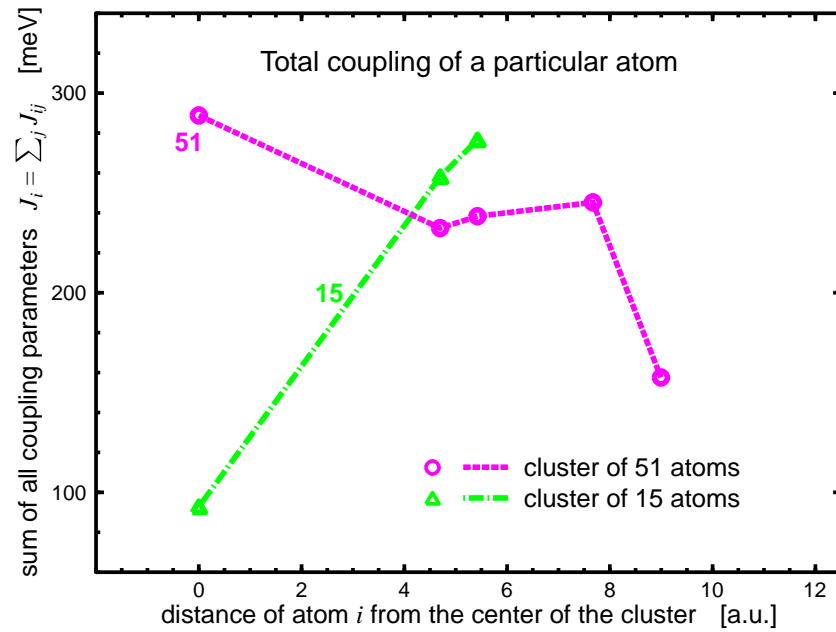
Energy needed to flip the spin of atom i while keeping all the remaining spins collinear:

$$J_i = \sum_{j \neq i} J_{ij}$$

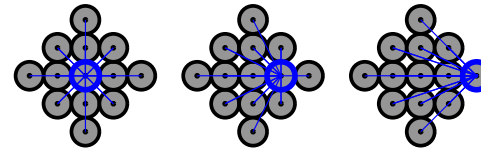
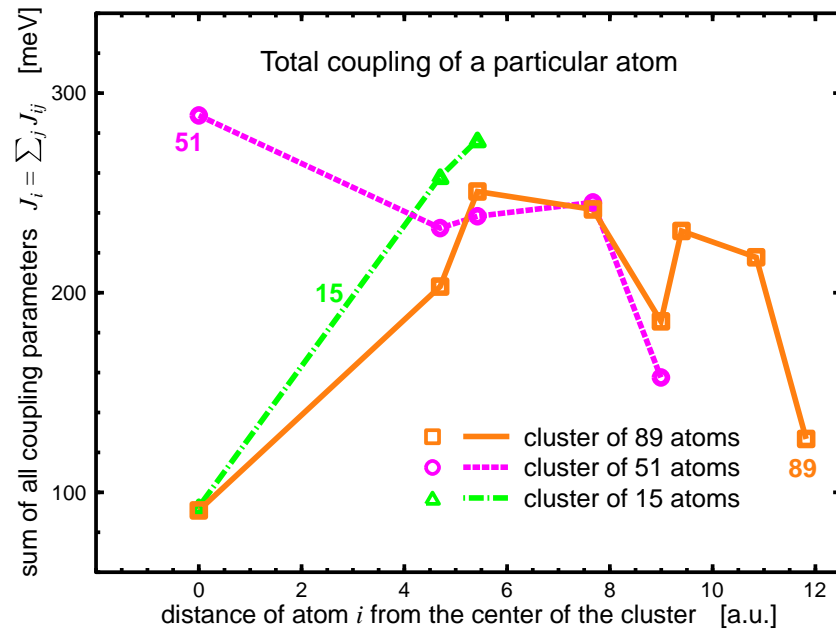
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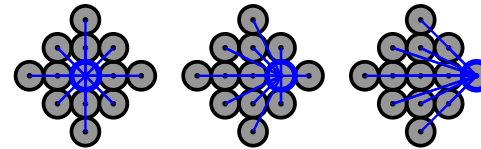
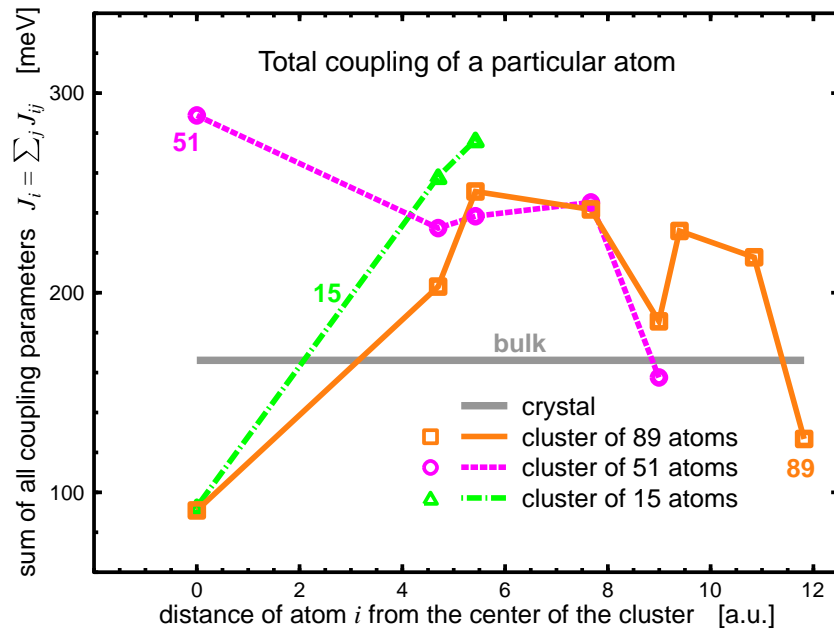
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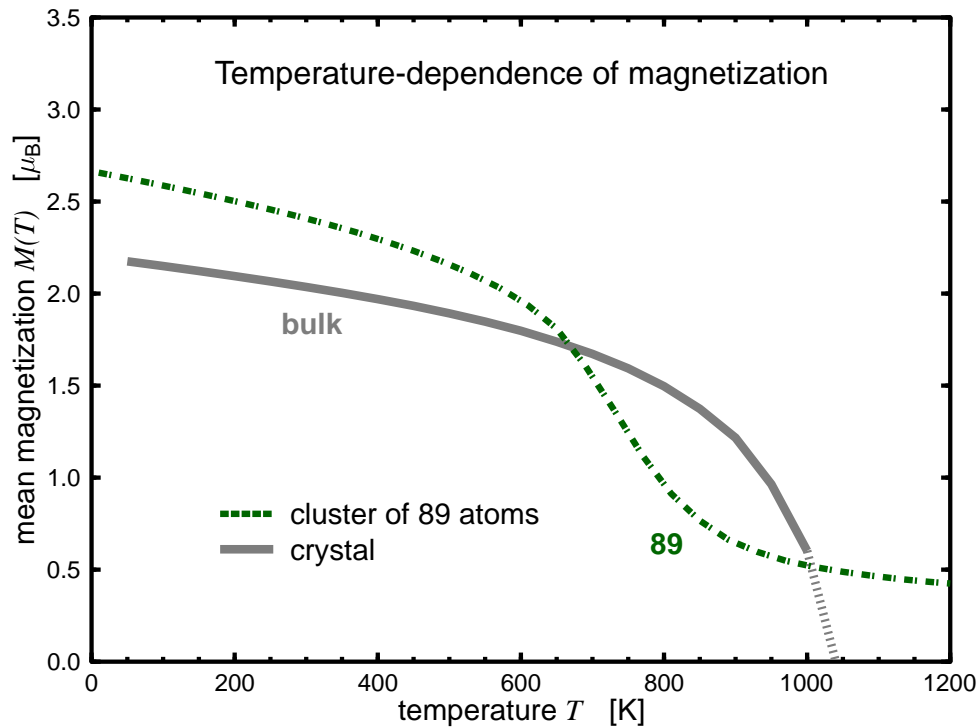


Site-dependence of $\sum_j J_{ij}$



- Mild differences in J_{ij} translate into large differences in $\sum_j J_{ij}$
- No systematics in cluster size,
no systematics in the position of atom within a cluster

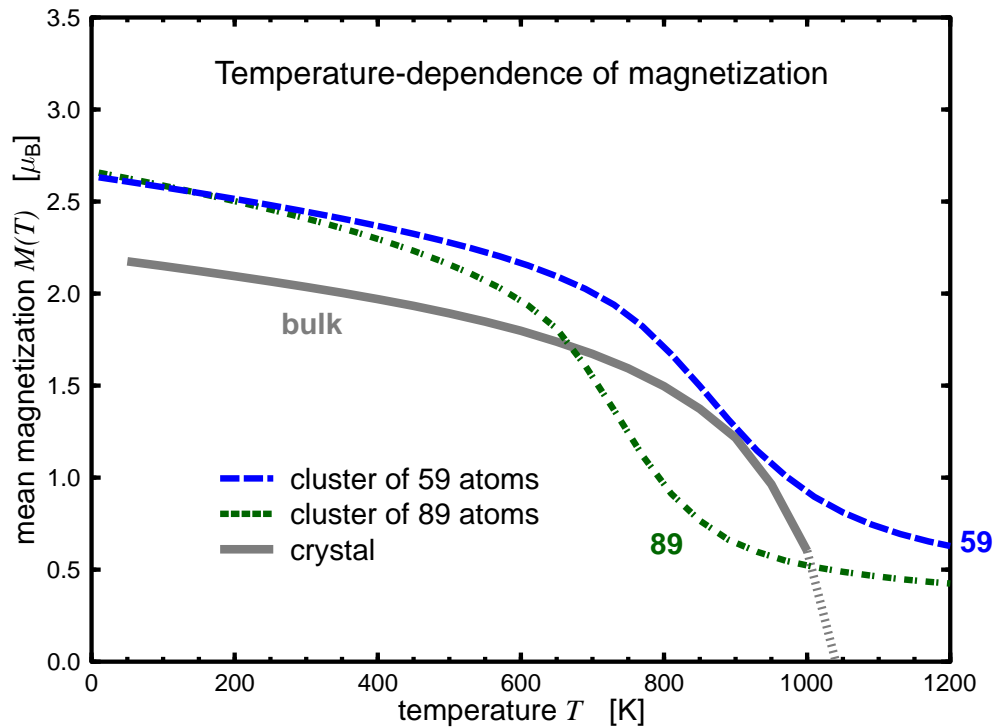
Decay of magnetization with T



[Bulk $M(T)$ curve was extrapolated to calculated T_C]

● $M(T)$ curves are more shallow in clusters than in bulk

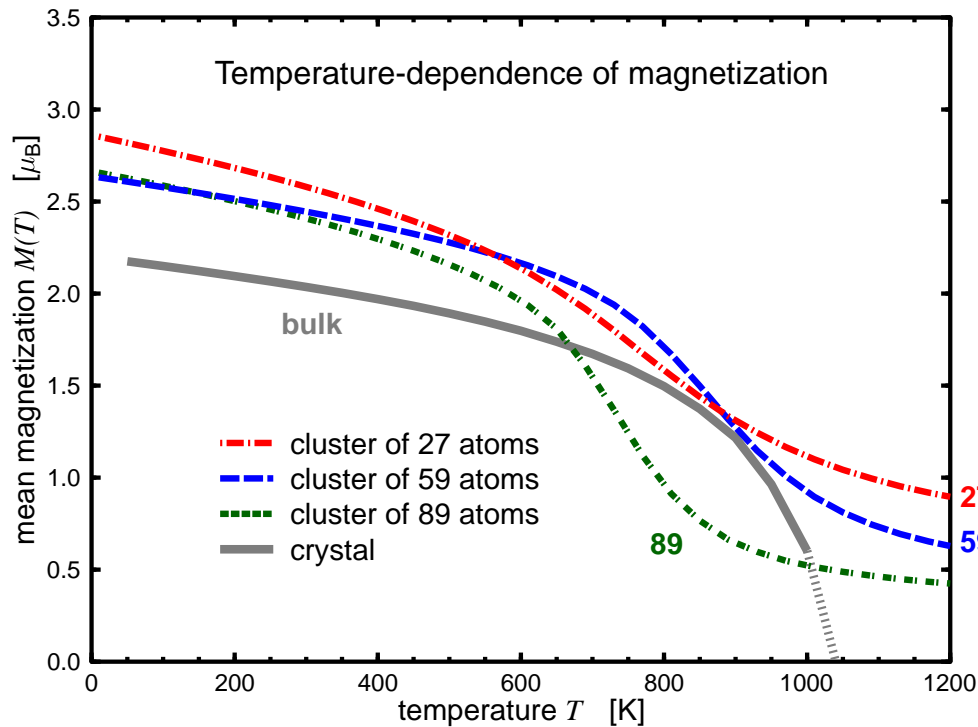
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- Small clusters — more shallow $M(T)$ curves than large clusters

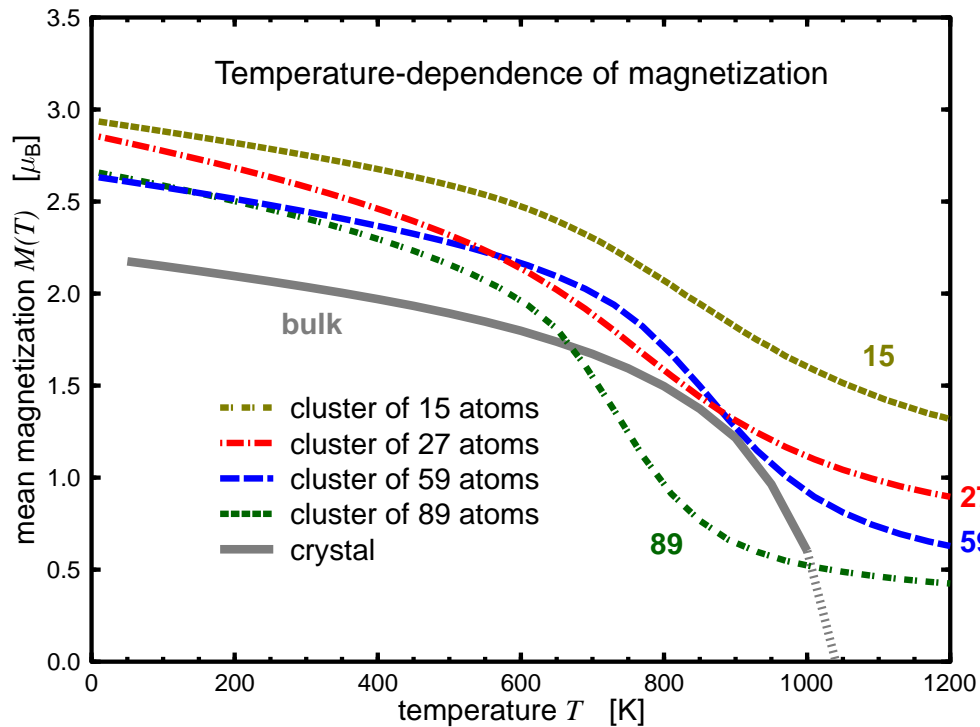
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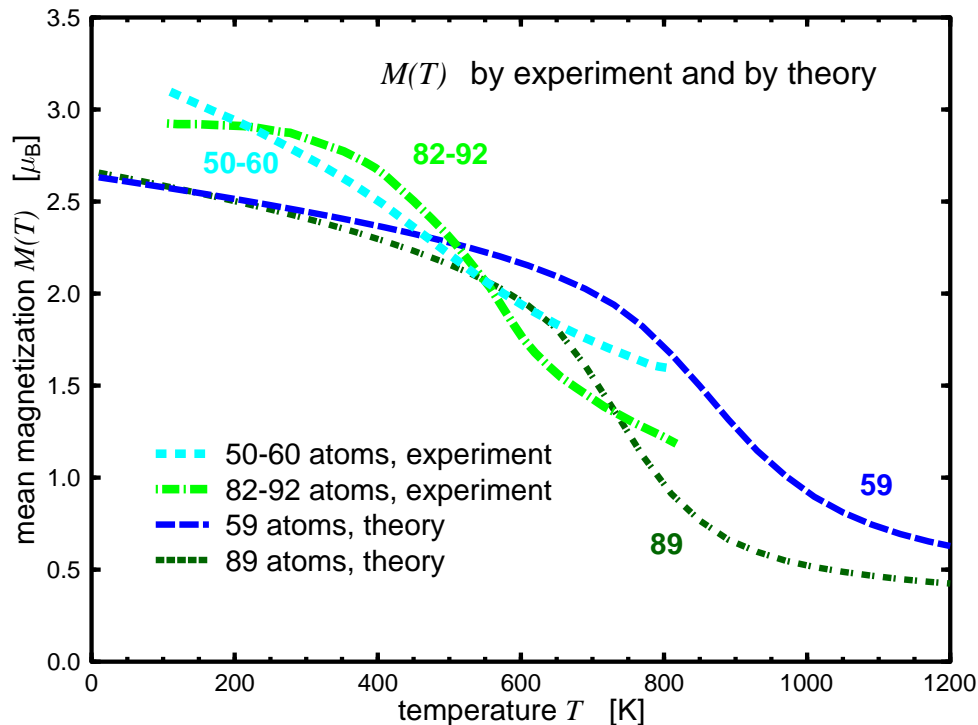
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Experimental and theoretical $M(T)$

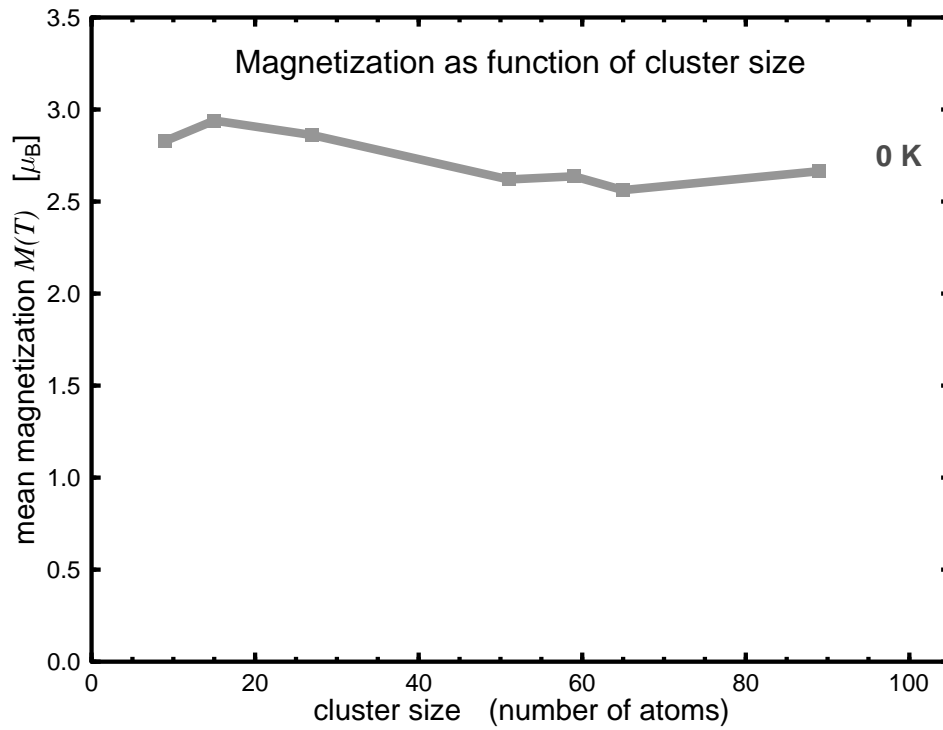


Experiment from Billas *et al.*
PRL **71**, 4067 (1993)

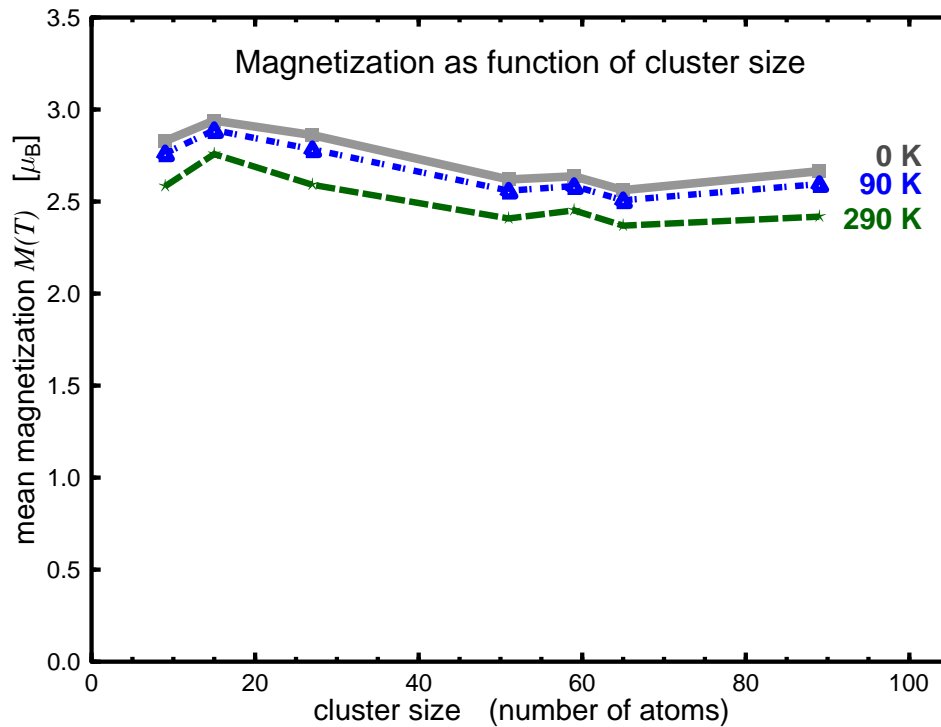
Caution:

Each experimental curve corresponds to a *range of cluster sizes* (it represents an average over several $M(T)$ curves which may differ quite a lot one from another)

M as function of cluster size

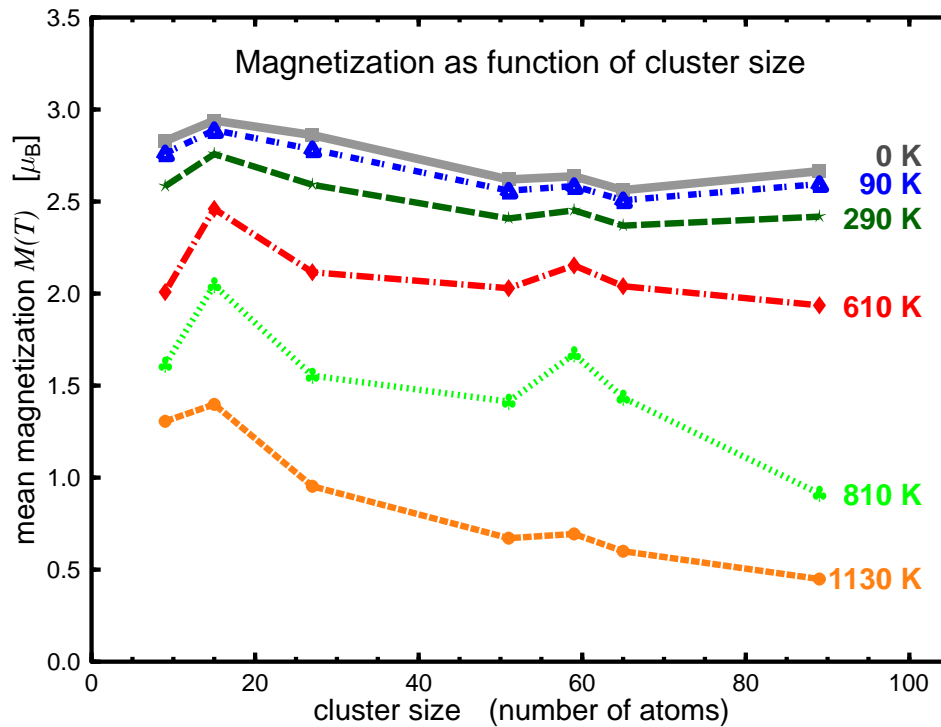


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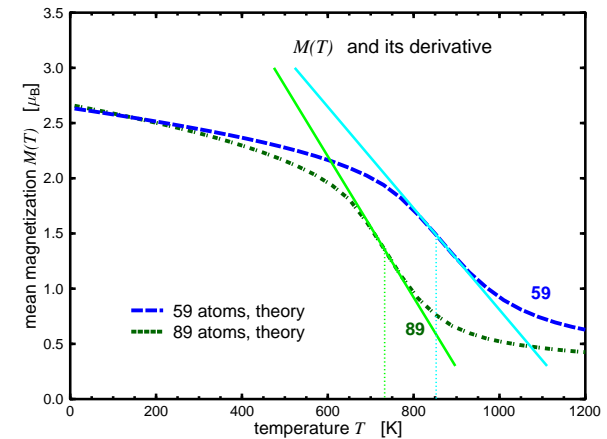
- Dependence of M on cluster size does not really vary with T for low (“experimental”) temperatures

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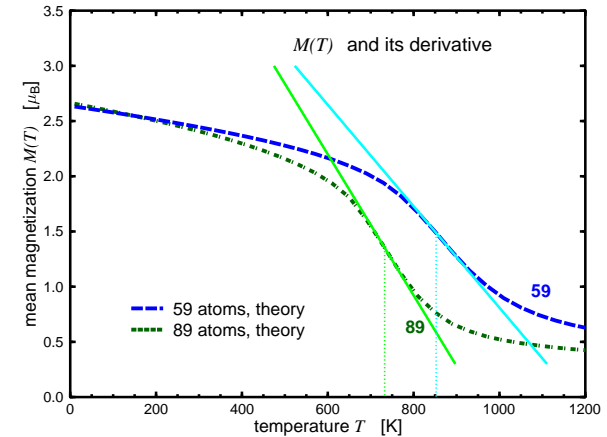
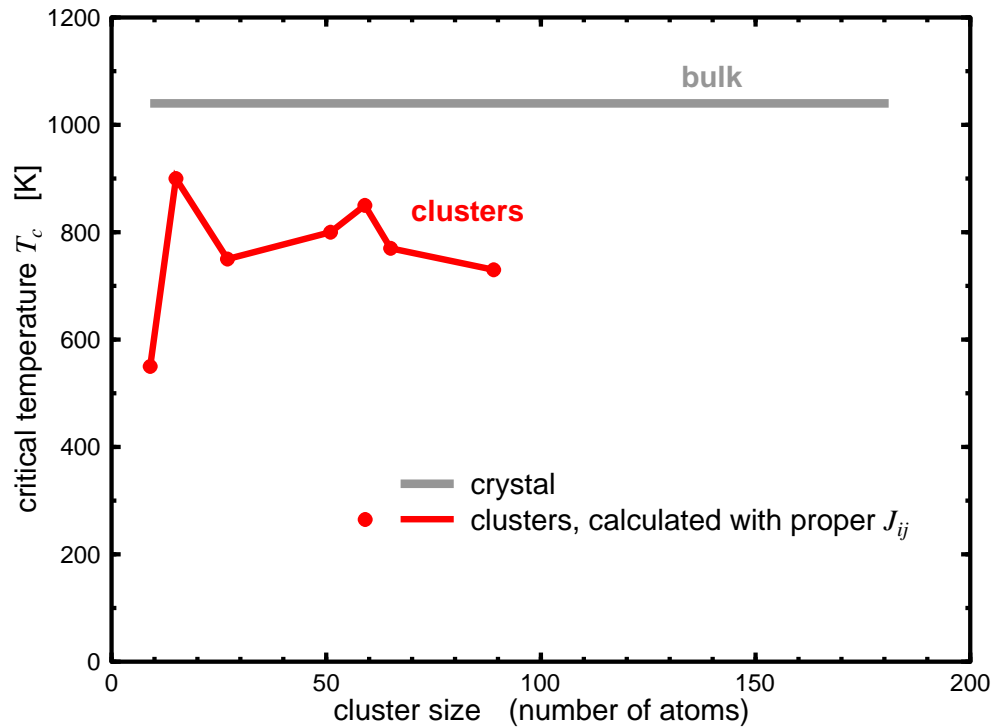
- Dependence of M on cluster size does not really vary with T for low (“experimental”) temperatures
- For large T , magnetization of large clusters is significantly reduced

Dependence of T_c on cluster size



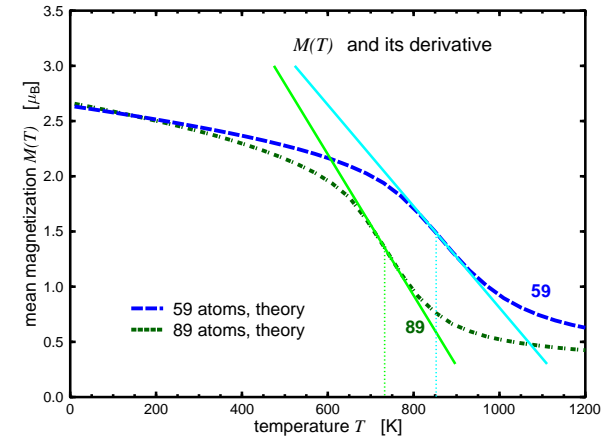
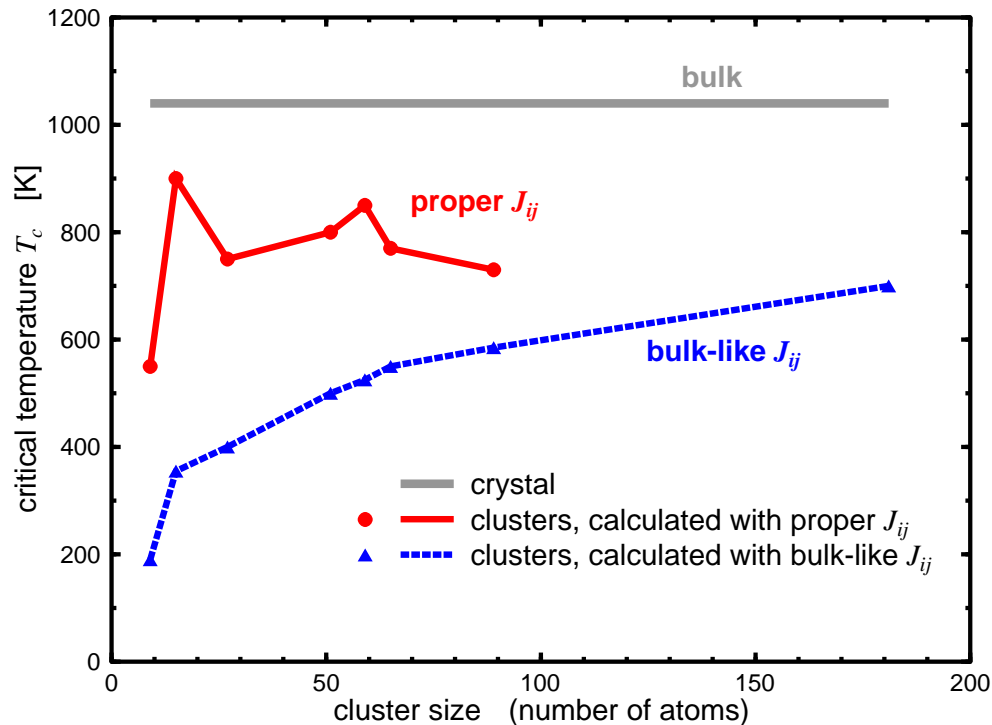
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Dependence of T_c on cluster size



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- T_c oscillates with cluster size
- Proper cluster-adjusted J_{ij} have to be taken into account

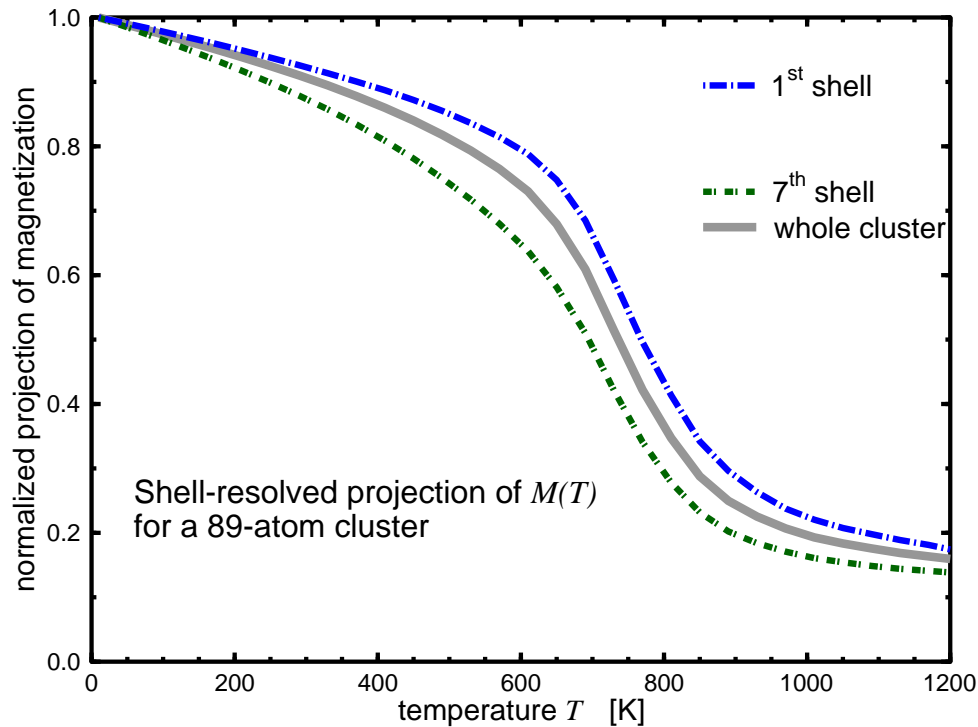
Shell-resolved magnetization

Expectations:

outer shells have smaller coordination numbers than inner shells

⇒ M in outer shells should decay more quickly with T
than M of inner shells

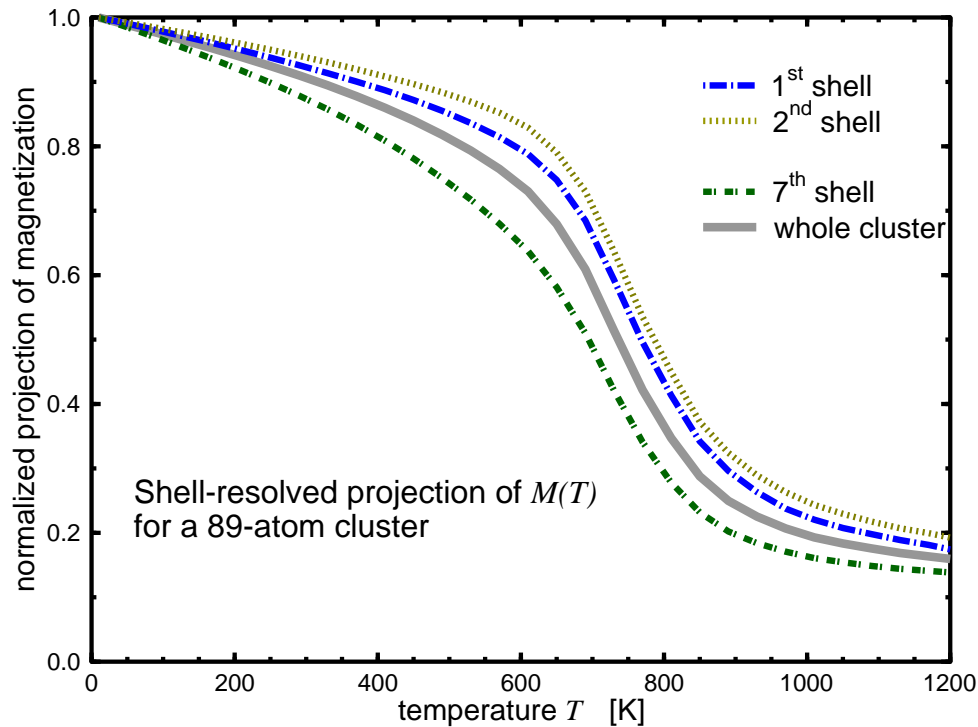
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Projecting M of a shell onto the direction of the total M of the 89-atom cluster

(Projections are normalized to $T = 0$)

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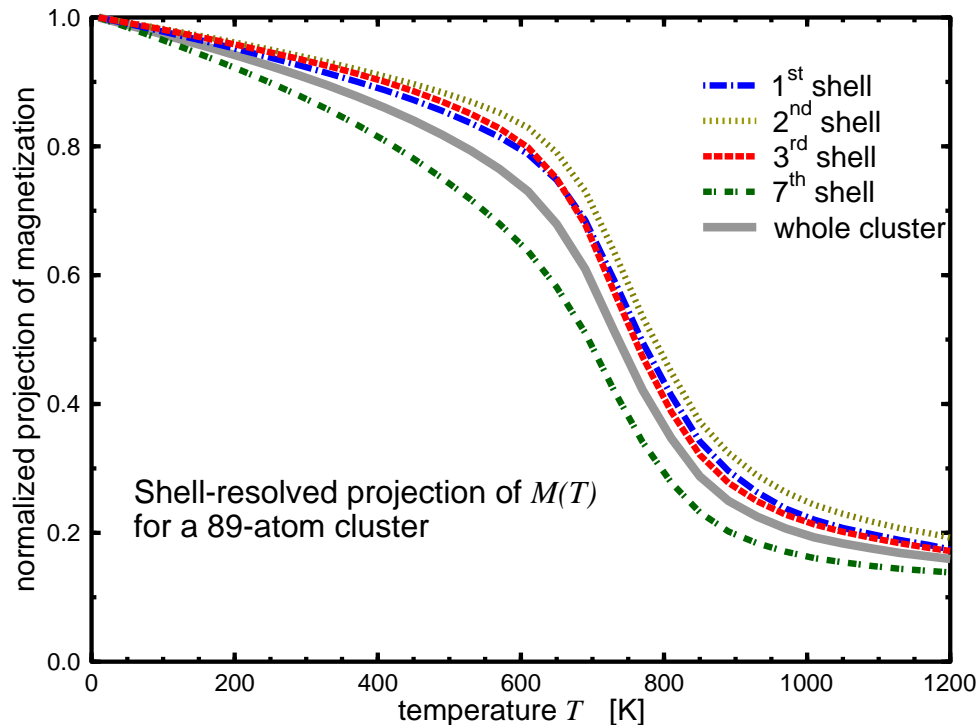


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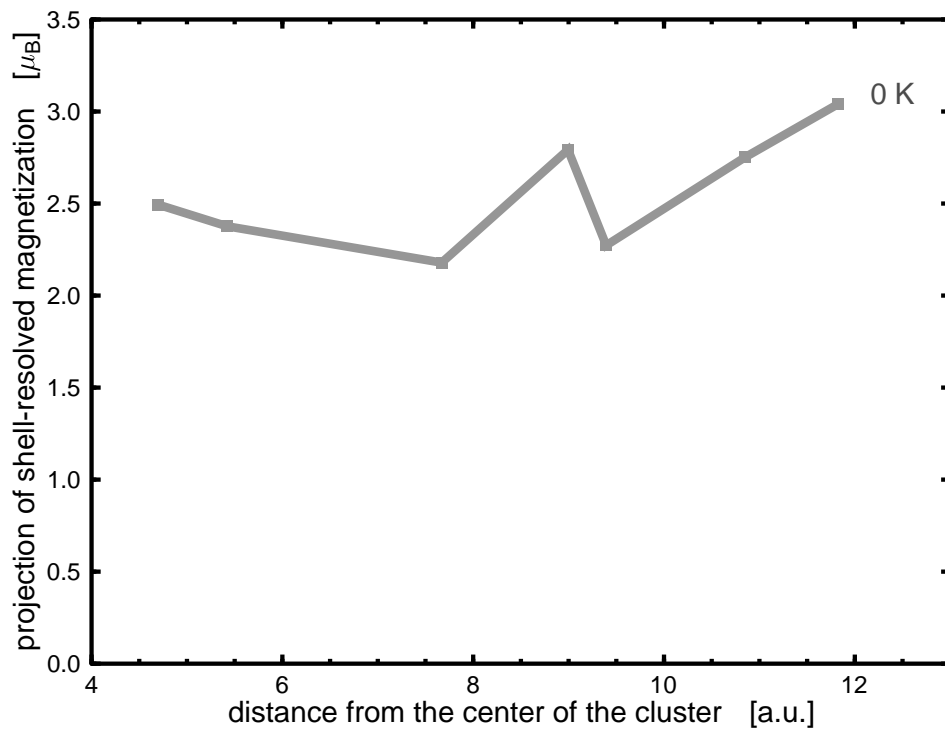


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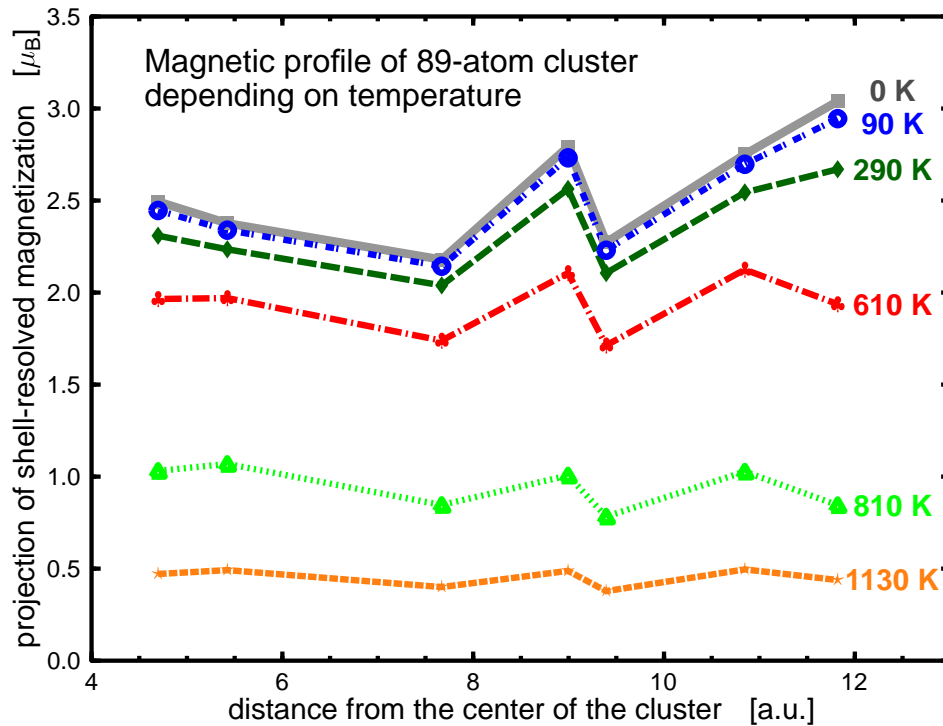
- Not monotonous in order of shells
- Although M of outer shells *usually* decays faster than M of inner shells, **no systematics** can be found.

Magnetic profile for $T \neq 0$



Cluster of 89 atoms
(7 coordination shells)

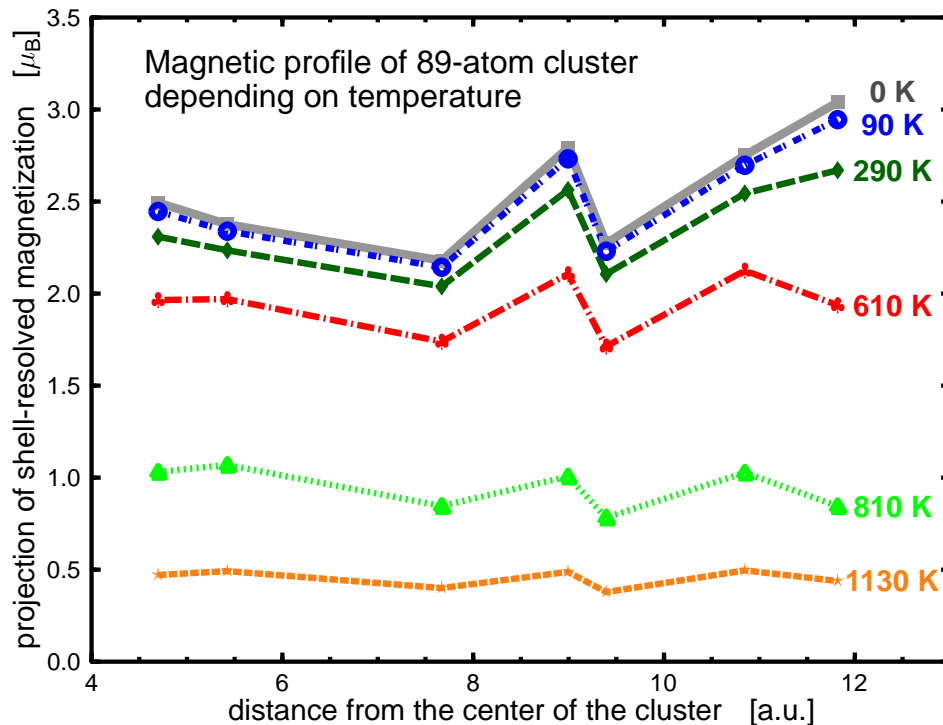
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- Magnetic profile gets **more flat** if temperature increases
- M of outermost layers is similar in magnitude to M of inner layers even for large T (i.e., no drastic decrease of surface M)

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- Critical temperature T_c **oscillates** with cluster size
- (Normalized) M of the outer shells *usually* decreases with T more quickly than M of inner shells
- Simple models (such as taking J_{ij} from bulk) do not work, systematical trends cannot be guessed beforehand
⇒ one really **has to calculate** all the quantities of interest